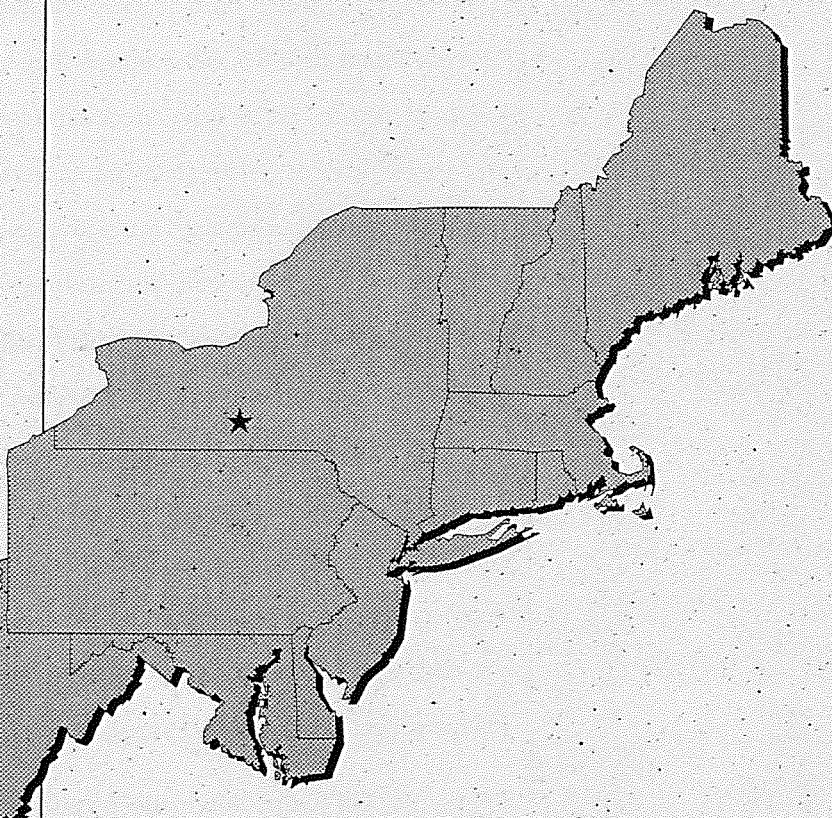


# NORTHEAST REGIONAL CLIMATE CENTER

## Gamma Distribution Probability Tables for Use in Climatology

Daniel S. Wilks



Cornell University  
Ithaca, New York  
Publication No. RR 91-2  
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# **Gamma Distribution Probability Tables for Use in Climatology**

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Atmospheric Sciences  
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## INTRODUCTION

The gamma distribution is widely used in climatological applications for representing variations in precipitation, ranging from seasonal and monthly totals (e.g., Ropelewski et al. 1985, Waggoner 1989) to nonzero daily values (e.g., Stern and Coe 1984, Wilks 1989). In addition, it can be used to interpret the 30- and 90-day precipitation forecasts issued by the Climate Analysis Center (Wilks and Eggleston 1992).

The probability density function for this distribution can be written as

$$f(x; \alpha, \beta) = \frac{(x/\beta)^{\alpha-1} \exp(-x/\beta)}{\beta \Gamma(\alpha)} ; \quad x \geq 0; \alpha, \beta > 0 .$$

Here  $x$  is the random variable (e.g., the precipitation amount),  $\alpha$  and  $\beta$  are the two distribution parameters, and  $\Gamma(\bullet)$  denotes the gamma function. The gamma distribution is characterized by mean  $\mu = \alpha\beta$  and variance  $\sigma^2 = \alpha\beta^2$ .

The shape parameter  $\alpha$  controls the basic form of the distribution. For values of  $\alpha \leq 1$ , the distribution exhibits a mode at  $x = 0$ , and is strongly skewed to the right. As  $\alpha$  increases above this value, the mode increases and the skewness decreases. For very large values of  $\alpha$  (greater than about 50), the gamma distribution approaches the Gaussian (normal) distribution, with  $\alpha = \mu^2/\sigma^2$  and  $\beta = \sigma^2/\mu$ .

The scale parameter  $\beta$  serves, as its name implies, only to scale the distribution. This can be appreciated by noting that everywhere the random variable  $x$  appears in the probability density it is divided by  $\beta$ . Since the scale parameter carries the dimensional information, it is sometimes useful to work with the "standard" gamma distribution, i.e., with  $\beta \equiv 1$ .

Gamma distribution probabilities are calculated by integrating the probability density function. In particular, cumulative probability, i.e., the probability that the random variable  $x$  will be no larger than a specific value,  $r$ , is given by

$$\Pr(x \leq r) = \int_0^r f(x; \alpha, \beta) dx .$$

This integration cannot be performed analytically, and numerical methods are required to evaluate the integral. Extensive results of such integrations are tabulated in this publication. The probability that the random variable  $x$  will fall within any interval can be obtained by finding the difference between the cumulative probabilities:

$$\Pr(a < x \leq b) = \Pr(x \leq b) - \Pr(x \leq a) .$$

## PARAMETER FITTING

Gamma distribution parameters characterizing some precipitation climatologies are available in the literature. For example, maps of the shape parameter for monthly total precipitation over the conterminous United States are given by Wilks and Eggleston (1992), and Ropelewski and Jalickee (1983) provide this information for seasonal (3-month) totals. For these cases, the scale parameter can be obtained using the (generally readily available) mean precipitation amount,  $\mu$ ; together with the relationship  $\beta = \mu/\alpha$ .

If the distribution parameters are to be fit to a sample of data, the preferred method is maximum likelihood (Choi and Wette 1969). This requires an iterative calculation that is not practical without a computer. Direct application of maximum likelihood techniques requires summing the logarithms of the data, so that special methods are necessary for records containing some zero precipitation amounts (Wilks 1990).

Two simple approximations to the maximum likelihood estimators are available, and may be of value to some users. The first, due to Thom (1958), uses

$$\hat{\alpha} = \frac{1 + \sqrt{1 + \frac{4A}{3}}}{4A}$$

where

$$A = \ln(\bar{X}) - \frac{1}{N} \sum_{i=1}^N \ln(X_i)$$

is the difference between the logarithm of the mean and the mean of the logarithms. The second approximation, given by Greenwood and Durand (1960), uses the polynomial and rational approximations

$$\hat{\alpha} = \frac{1}{A} [ .5000876 + .1648852 A - .0544274 A^2 ], \quad 0 \leq A \leq 0.5772,$$

or

$$\hat{\alpha} = \frac{8.898919 + 9.059950 A + .9775373 A^2}{A ( 17.79728 + 11.968477 A + A^2 )}, \quad 0.5772 \leq A \leq 17.0,$$

where  $A$  is as given above. The accuracy of the Greenwood and Durand estimators will be greater than that of the Thom estimator, particularly for small values of the shape parameter. In either case, the scale parameter is subsequently calculated as

$$\hat{\beta} = \bar{X} / \hat{\alpha}.$$

Parameters can also be fit using the method of moments, although this is not recommended (Wilks 1990).

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## HOW TO USE THE TABLES

The following probability tables present percentage points of the standard gamma distribution, i.e., that having unit scale parameter  $\beta$ . Data values listed in the body of the table correspond to cumulative probabilities given in the first column. That is, for the standard gamma distribution having the shape parameter listed at the top of a given column, the probability of a random variable being less than or equal to a tabulated value is given in the corresponding row of the first column.

To extract cumulative probabilities corresponding to a data value  $x$  of interest in the general case of a distribution with  $\beta \neq 1$ , construct the standardized variable  $\xi = x/\beta$ , enter the tables at the appropriate column, locate the value of  $\xi$ , and interpolate between the rows of the first column to obtain the cumulative probability.

To use the tables in reverse, i.e., to find percentage points (data values,  $x$ ) corresponding to a particular cumulative probability in the first column, enter the table at the appropriate row, extract the tabulated value of  $\xi$  in the column for the shape parameter of interest, and then reconstitute the dimensional value  $x = \beta\xi$ .

For example, the distribution of total January precipitation at Ithaca, New York, is characterized by shape parameter  $\alpha = 4.4$  and scale parameter  $\beta = 1.16$  cm (Wilks and Eggleston 1992). To find the cumulative probability associated with the precipitation amount  $x = 10.0$  cm (i.e., the probability of no more than 10 cm of precipitation in an arbitrary January), first calculate the standardized variable  $\xi = x/\beta = (10.0 \text{ cm}) / (1.16 \text{ cm}) = 8.621$ . Enter the table on page 13 under the column headed by Shape Parameter = 4.40. It can be seen that the cumulative probability associated with  $\xi = 8.661$  is nearly 0.96 or, with interpolation, 0.959. Therefore, the gamma distribution probability model indicates a 4.1% chance of total January precipitation being greater than 10 cm at this location.

To find the median January precipitation for Ithaca, locate in the same column the value of the standardized variable associated with the cumulative probability 0.50:  $\xi = 4.072$ . The dimensional median precipitation value is thus  $x = \beta\xi = (1.16 \text{ cm})(4.072) = 4.72 \text{ cm}$ .

The tables contain values for distributions having shape parameters in the range 0.05 to 50.0. These will be adequate for most cases of climatological interest. For larger values of the shape parameter, the gamma distribution is well approximated by the normal distribution, so that readily available tables of that distribution can be used to evaluate probabilities of interest. In that case,

$$\Pr(x \leq r) \approx \Phi \left[ \frac{r - \alpha\beta}{\beta\sqrt{\alpha}} \right], \quad \alpha \geq 50,$$

where  $\Phi(\bullet)$  is the cumulative distribution function for the standard normal distribution.

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

Shape Parameter

| Cum.<br>Prob. | 0.05    | 0.10    | 0.15    | 0.20    | 0.25    | 0.30    | 0.35    | 0.40    | 0.45    | 0.50    |
|---------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| .001          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 |
| .005          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00002 |
| .010          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00003 | 0.00008 |
| .020          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00004 | 0.00013 | 0.00031 |
| .030          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00003 | 0.00012 | 0.00032 | 0.00071 |
| .040          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00002 | 0.00007 | 0.00024 | 0.00060 | 0.00126 |
| .050          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00003 | 0.00014 | 0.00041 | 0.00098 | 0.00197 |
| .060          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00006 | 0.00023 | 0.00065 | 0.00147 | 0.00283 |
| .080          | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00003 | 0.00015 | 0.00053 | 0.00134 | 0.00279 | 0.00504 |
| .100          | 0.00000 | 0.00000 | 0.00000 | 0.00001 | 0.00007 | 0.00032 | 0.00100 | 0.00235 | 0.00459 | 0.00790 |
| .120          | 0.00000 | 0.00000 | 0.00000 | 0.00002 | 0.00014 | 0.00059 | 0.00169 | 0.00371 | 0.00690 | 0.01140 |
| .140          | 0.00000 | 0.00000 | 0.00000 | 0.00004 | 0.00026 | 0.00099 | 0.00262 | 0.00546 | 0.00973 | 0.01555 |
| .160          | 0.00000 | 0.00000 | 0.00000 | 0.00007 | 0.00044 | 0.00155 | 0.00384 | 0.00763 | 0.01313 | 0.02038 |
| .180          | 0.00000 | 0.00000 | 0.00001 | 0.00012 | 0.00071 | 0.00230 | 0.00538 | 0.01027 | 0.01710 | 0.02589 |
| .200          | 0.00000 | 0.00000 | 0.00001 | 0.00021 | 0.00108 | 0.00327 | 0.00728 | 0.01339 | 0.02168 | 0.03209 |
| .220          | 0.00000 | 0.00000 | 0.00003 | 0.00034 | 0.00158 | 0.00450 | 0.00958 | 0.01704 | 0.02689 | 0.03901 |
| .240          | 0.00000 | 0.00000 | 0.00005 | 0.00052 | 0.00224 | 0.00602 | 0.01231 | 0.02124 | 0.03275 | 0.04666 |
| .260          | 0.00000 | 0.00000 | 0.00008 | 0.00078 | 0.00309 | 0.00787 | 0.01551 | 0.02604 | 0.03931 | 0.05506 |
| .280          | 0.00000 | 0.00000 | 0.00013 | 0.00112 | 0.00416 | 0.01009 | 0.01921 | 0.03146 | 0.04657 | 0.06425 |
| .300          | 0.00000 | 0.00000 | 0.00021 | 0.00159 | 0.00549 | 0.01273 | 0.02347 | 0.03754 | 0.05459 | 0.07424 |
| .320          | 0.00000 | 0.00001 | 0.00032 | 0.00219 | 0.00712 | 0.01582 | 0.02833 | 0.04433 | 0.06338 | 0.08506 |
| .340          | 0.00000 | 0.00001 | 0.00047 | 0.00297 | 0.00909 | 0.01941 | 0.03382 | 0.05186 | 0.07300 | 0.09676 |
| .360          | 0.00000 | 0.00002 | 0.00069 | 0.00396 | 0.01144 | 0.02356 | 0.04000 | 0.06017 | 0.08347 | 0.10937 |
| .380          | 0.00000 | 0.00004 | 0.00100 | 0.00519 | 0.01423 | 0.02832 | 0.04692 | 0.06932 | 0.09485 | 0.12293 |
| .400          | 0.00000 | 0.00006 | 0.00140 | 0.00672 | 0.01752 | 0.03374 | 0.05463 | 0.07936 | 0.10718 | 0.13750 |
| .420          | 0.00000 | 0.00010 | 0.00194 | 0.00859 | 0.02136 | 0.03988 | 0.06320 | 0.09035 | 0.12053 | 0.15312 |
| .440          | 0.00000 | 0.00017 | 0.00265 | 0.01086 | 0.02582 | 0.04682 | 0.07268 | 0.10234 | 0.13494 | 0.16985 |
| .460          | 0.00000 | 0.00026 | 0.00357 | 0.01359 | 0.03098 | 0.05462 | 0.08315 | 0.11540 | 0.15049 | 0.18777 |
| .480          | 0.00000 | 0.00039 | 0.00474 | 0.01686 | 0.03690 | 0.06336 | 0.09468 | 0.12962 | 0.16726 | 0.20695 |
| .500          | 0.00000 | 0.00059 | 0.00623 | 0.02075 | 0.04367 | 0.07313 | 0.10737 | 0.14508 | 0.18533 | 0.22747 |
| .520          | 0.00000 | 0.00088 | 0.00811 | 0.02534 | 0.05140 | 0.08403 | 0.12130 | 0.16187 | 0.20479 | 0.24943 |
| .540          | 0.00000 | 0.00128 | 0.01045 | 0.03074 | 0.06019 | 0.09616 | 0.13659 | 0.18010 | 0.22576 | 0.27295 |
| .560          | 0.00001 | 0.00185 | 0.01335 | 0.03706 | 0.07016 | 0.10965 | 0.15336 | 0.19989 | 0.24835 | 0.29814 |
| .580          | 0.00001 | 0.00262 | 0.01693 | 0.04443 | 0.08145 | 0.12463 | 0.17174 | 0.22139 | 0.27272 | 0.32516 |
| .600          | 0.00002 | 0.00368 | 0.02130 | 0.05301 | 0.09421 | 0.14125 | 0.19189 | 0.24475 | 0.29902 | 0.35416 |
| .620          | 0.00004 | 0.00512 | 0.02662 | 0.06296 | 0.10861 | 0.15971 | 0.21400 | 0.27016 | 0.32744 | 0.38535 |
| .640          | 0.00008 | 0.00705 | 0.03308 | 0.07449 | 0.12486 | 0.18020 | 0.23827 | 0.29784 | 0.35820 | 0.41895 |
| .660          | 0.00014 | 0.00961 | 0.04089 | 0.08782 | 0.14321 | 0.20297 | 0.26496 | 0.32804 | 0.39157 | 0.45522 |
| .680          | 0.00026 | 0.01299 | 0.05030 | 0.10323 | 0.16393 | 0.22831 | 0.29437 | 0.36106 | 0.42785 | 0.49447 |
| .700          | 0.00047 | 0.01743 | 0.06161 | 0.12104 | 0.18735 | 0.25656 | 0.32683 | 0.39726 | 0.46741 | 0.53710 |
| .720          | 0.00082 | 0.02322 | 0.07520 | 0.14164 | 0.21388 | 0.28814 | 0.36279 | 0.43708 | 0.51071 | 0.58355 |
| .740          | 0.00142 | 0.03075 | 0.09151 | 0.16552 | 0.24402 | 0.32356 | 0.40275 | 0.48106 | 0.55827 | 0.63438 |
| .760          | 0.00242 | 0.04049 | 0.11112 | 0.19325 | 0.27838 | 0.36345 | 0.44739 | 0.52986 | 0.61081 | 0.69030 |
| .780          | 0.00408 | 0.05310 | 0.13474 | 0.22561 | 0.31773 | 0.40861 | 0.49751 | 0.58433 | 0.66917 | 0.75219 |
| .800          | 0.00678 | 0.06939 | 0.16329 | 0.26354 | 0.36309 | 0.46007 | 0.55419 | 0.64557 | 0.73448 | 0.82119 |
| .820          | 0.01116 | 0.09049 | 0.19798 | 0.30834 | 0.41577 | 0.51922 | 0.61883 | 0.71502 | 0.80822 | 0.89881 |
| .840          | 0.01819 | 0.11792 | 0.24049 | 0.36174 | 0.47759 | 0.58792 | 0.69337 | 0.79465 | 0.89239 | 0.98711 |
| .860          | 0.02943 | 0.15388 | 0.29316 | 0.42620 | 0.55110 | 0.66879 | 0.78049 | 0.88723 | 0.98984 | 1.08898 |
| .880          | 0.04740 | 0.20159 | 0.35945 | 0.50536 | 0.64007 | 0.76574 | 0.88419 | 0.99684 | 1.10473 | 1.20866 |
| .900          | 0.07632 | 0.26615 | 0.44480 | 0.60490 | 0.75039 | 0.88481 | 1.01070 | 1.12984 | 1.24355 | 1.35277 |
| .920          | 0.12366 | 0.35624 | 0.55843 | 0.73446 | 0.89203 | 1.03627 | 1.17051 | 1.29698 | 1.41725 | 1.53245 |
| .940          | 0.20413 | 0.48840 | 0.71791 | 0.91232 | 1.08387 | 1.23951 | 1.38348 | 1.51851 | 1.64647 | 1.76869 |
| .950          | 0.26593 | 0.58044 | 0.82559 | 1.03053 | 1.21012 | 1.37235 | 1.52196 | 1.66196 | 1.79440 | 1.92073 |
| .960          | 0.35213 | 0.70077 | 0.96346 | 1.18025 | 1.36893 | 1.53864 | 1.69466 | 1.84034 | 1.97791 | 2.10894 |
| .970          | 0.47878 | 0.86693 | 1.14990 | 1.38049 | 1.57981 | 1.75831 | 1.92193 | 2.07434 | 2.21801 | 2.35465 |
| .980          | 0.68301 | 1.11903 | 1.42680 | 1.67444 | 1.88702 | 2.07657 | 2.24976 | 2.41072 | 2.56215 | 2.70595 |
| .990          | 1.08763 | 1.58848 | 1.93059 | 2.20231 | 2.43389 | 2.63941 | 2.82659 | 3.00010 | 3.16301 | 3.31745 |
| .995          | 1.54463 | 2.09456 | 2.46364 | 2.75470 | 3.00181 | 3.22057 | 3.41944 | 3.60355 | 3.77620 | 3.93972 |
| .999          | 2.73649 | 3.36367 | 3.77761 | 4.10198 | 4.37643 | 4.61895 | 4.83909 | 5.04260 | 5.23332 | 5.41382 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 0.50            | 0.55   | 0.60   | 0.65   | 0.70   | 0.75   | 0.80   | 0.85   | 0.90   | 0.95   | 1.00   |
| .001          | 0.0000          | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0001 | 0.0002 | 0.0003 | 0.0004 | 0.0007 | 0.0010 |
| .005          | 0.0000          | 0.0001 | 0.0001 | 0.0002 | 0.0005 | 0.0008 | 0.0012 | 0.0018 | 0.0027 | 0.0037 | 0.0050 |
| .010          | 0.0001          | 0.0002 | 0.0004 | 0.0007 | 0.0012 | 0.0019 | 0.0029 | 0.0042 | 0.0058 | 0.0077 | 0.0101 |
| .020          | 0.0003          | 0.0007 | 0.0012 | 0.0021 | 0.0033 | 0.0049 | 0.0069 | 0.0094 | 0.0125 | 0.0161 | 0.0202 |
| .030          | 0.0007          | 0.0014 | 0.0024 | 0.0039 | 0.0058 | 0.0084 | 0.0115 | 0.0153 | 0.0197 | 0.0247 | 0.0305 |
| .040          | 0.0013          | 0.0023 | 0.0039 | 0.0060 | 0.0088 | 0.0123 | 0.0165 | 0.0215 | 0.0272 | 0.0336 | 0.0408 |
| .050          | 0.0020          | 0.0035 | 0.0056 | 0.0085 | 0.0122 | 0.0166 | 0.0219 | 0.0280 | 0.0350 | 0.0427 | 0.0513 |
| .060          | 0.0028          | 0.0049 | 0.0077 | 0.0113 | 0.0158 | 0.0212 | 0.0276 | 0.0348 | 0.0430 | 0.0520 | 0.0619 |
| .080          | 0.0050          | 0.0082 | 0.0124 | 0.0177 | 0.0240 | 0.0314 | 0.0398 | 0.0493 | 0.0597 | 0.0711 | 0.0834 |
| .100          | 0.0079          | 0.0124 | 0.0181 | 0.0250 | 0.0331 | 0.0425 | 0.0530 | 0.0646 | 0.0772 | 0.0908 | 0.1054 |
| .120          | 0.0114          | 0.0173 | 0.0246 | 0.0332 | 0.0433 | 0.0546 | 0.0671 | 0.0807 | 0.0954 | 0.1112 | 0.1278 |
| .140          | 0.0156          | 0.0230 | 0.0319 | 0.0424 | 0.0543 | 0.0675 | 0.0820 | 0.0976 | 0.1144 | 0.1321 | 0.1508 |
| .160          | 0.0204          | 0.0294 | 0.0401 | 0.0524 | 0.0661 | 0.0813 | 0.0977 | 0.1153 | 0.1340 | 0.1537 | 0.1744 |
| .180          | 0.0259          | 0.0366 | 0.0490 | 0.0632 | 0.0788 | 0.0959 | 0.1142 | 0.1337 | 0.1543 | 0.1759 | 0.1985 |
| .200          | 0.0321          | 0.0445 | 0.0588 | 0.0748 | 0.0923 | 0.1113 | 0.1315 | 0.1529 | 0.1754 | 0.1988 | 0.2231 |
| .220          | 0.0390          | 0.0532 | 0.0694 | 0.0873 | 0.1067 | 0.1275 | 0.1496 | 0.1729 | 0.1972 | 0.2224 | 0.2485 |
| .240          | 0.0467          | 0.0627 | 0.0808 | 0.1005 | 0.1219 | 0.1446 | 0.1685 | 0.1936 | 0.2197 | 0.2466 | 0.2744 |
| .260          | 0.0551          | 0.0730 | 0.0930 | 0.1147 | 0.1379 | 0.1625 | 0.1882 | 0.2151 | 0.2429 | 0.2716 | 0.3011 |
| .280          | 0.0642          | 0.0842 | 0.1061 | 0.1297 | 0.1548 | 0.1812 | 0.2088 | 0.2374 | 0.2670 | 0.2974 | 0.3285 |
| .300          | 0.0742          | 0.0961 | 0.1200 | 0.1455 | 0.1725 | 0.2008 | 0.2302 | 0.2606 | 0.2919 | 0.3239 | 0.3567 |
| .320          | 0.0851          | 0.1090 | 0.1348 | 0.1623 | 0.1912 | 0.2213 | 0.2525 | 0.2846 | 0.3176 | 0.3513 | 0.3857 |
| .340          | 0.0968          | 0.1227 | 0.1506 | 0.1800 | 0.2108 | 0.2428 | 0.2757 | 0.3096 | 0.3442 | 0.3796 | 0.4155 |
| .360          | 0.1094          | 0.1374 | 0.1673 | 0.1987 | 0.2314 | 0.2652 | 0.2999 | 0.3355 | 0.3718 | 0.4088 | 0.4463 |
| .380          | 0.1229          | 0.1531 | 0.1850 | 0.2184 | 0.2530 | 0.2886 | 0.3251 | 0.3624 | 0.4004 | 0.4390 | 0.4780 |
| .400          | 0.1375          | 0.1698 | 0.2038 | 0.2392 | 0.2757 | 0.3131 | 0.3514 | 0.3904 | 0.4300 | 0.4702 | 0.5108 |
| .420          | 0.1531          | 0.1876 | 0.2237 | 0.2611 | 0.2995 | 0.3388 | 0.3789 | 0.4196 | 0.4608 | 0.5026 | 0.5447 |
| .440          | 0.1699          | 0.2066 | 0.2448 | 0.2841 | 0.3245 | 0.3656 | 0.4075 | 0.4499 | 0.4928 | 0.5361 | 0.5798 |
| .460          | 0.1878          | 0.2267 | 0.2671 | 0.3085 | 0.3508 | 0.3938 | 0.4374 | 0.4815 | 0.5260 | 0.5710 | 0.6162 |
| .480          | 0.2069          | 0.2482 | 0.2907 | 0.3341 | 0.3784 | 0.4232 | 0.4686 | 0.5145 | 0.5607 | 0.6072 | 0.6539 |
| .500          | 0.2275          | 0.2710 | 0.3149 | 0.3612 | 0.4074 | 0.4542 | 0.5014 | 0.5489 | 0.5967 | 0.6448 | 0.6931 |
| .520          | 0.2494          | 0.2953 | 0.3422 | 0.3898 | 0.4380 | 0.4867 | 0.5356 | 0.5849 | 0.6344 | 0.6841 | 0.7340 |
| .540          | 0.2729          | 0.3212 | 0.3704 | 0.4201 | 0.4703 | 0.5208 | 0.5716 | 0.6226 | 0.6738 | 0.7251 | 0.7765 |
| .560          | 0.2981          | 0.3489 | 0.4003 | 0.4521 | 0.5043 | 0.5568 | 0.6094 | 0.6622 | 0.7151 | 0.7680 | 0.8209 |
| .580          | 0.3252          | 0.3783 | 0.4320 | 0.4861 | 0.5403 | 0.5948 | 0.6493 | 0.7038 | 0.7584 | 0.8130 | 0.8675 |
| .600          | 0.3542          | 0.4099 | 0.4659 | 0.5222 | 0.5781 | 0.6349 | 0.6913 | 0.7476 | 0.8039 | 0.8601 | 0.9163 |
| .620          | 0.3854          | 0.4436 | 0.5020 | 0.5605 | 0.6190 | 0.6774 | 0.7357 | 0.7939 | 0.8519 | 0.9098 | 0.9676 |
| .640          | 0.4189          | 0.4798 | 0.5407 | 0.6015 | 0.6621 | 0.7225 | 0.7828 | 0.8428 | 0.9026 | 0.9622 | 1.0217 |
| .660          | 0.4552          | 0.5188 | 0.5821 | 0.6452 | 0.7081 | 0.7706 | 0.8328 | 0.8947 | 0.9564 | 1.0177 | 1.0788 |
| .680          | 0.4945          | 0.5608 | 0.6267 | 0.6922 | 0.7572 | 0.8219 | 0.8861 | 0.9500 | 1.0135 | 1.0766 | 1.1394 |
| .700          | 0.5371          | 0.6062 | 0.6747 | 0.7427 | 0.8101 | 0.8769 | 0.9432 | 1.0091 | 1.0744 | 1.1394 | 1.2040 |
| .720          | 0.5835          | 0.6556 | 0.7268 | 0.7973 | 0.8670 | 0.9361 | 1.0045 | 1.0724 | 1.1398 | 1.2066 | 1.2730 |
| .740          | 0.6344          | 0.7094 | 0.7834 | 0.8565 | 0.9287 | 1.0001 | 1.0707 | 1.1407 | 1.2101 | 1.2788 | 1.3471 |
| .760          | 0.6903          | 0.7684 | 0.8453 | 0.9211 | 0.9958 | 1.0696 | 1.1426 | 1.2147 | 1.2862 | 1.3569 | 1.4271 |
| .780          | 0.7522          | 0.8325 | 0.9135 | 0.9920 | 1.0694 | 1.1457 | 1.2210 | 1.2954 | 1.3691 | 1.4419 | 1.5141 |
| .800          | 0.8212          | 0.9060 | 0.9890 | 1.0705 | 1.1506 | 1.2296 | 1.3074 | 1.3842 | 1.4601 | 1.5351 | 1.6094 |
| .820          | 0.8988          | 0.9871 | 1.0735 | 1.1581 | 1.2412 | 1.3228 | 1.4033 | 1.4826 | 1.5609 | 1.6383 | 1.7148 |
| .840          | 0.9871          | 1.0792 | 1.1691 | 1.2570 | 1.3432 | 1.4278 | 1.5110 | 1.5930 | 1.6738 | 1.7537 | 1.8326 |
| .860          | 1.0890          | 1.1852 | 1.2788 | 1.3702 | 1.4597 | 1.5475 | 1.6337 | 1.7186 | 1.8022 | 1.8841 | 1.9661 |
| .880          | 1.2087          | 1.3093 | 1.4070 | 1.5023 | 1.5954 | 1.6866 | 1.7761 | 1.8640 | 1.9507 | 2.0360 | 2.1203 |
| .900          | 1.3528          | 1.4582 | 1.5605 | 1.6600 | 1.7571 | 1.8521 | 1.9453 | 2.0367 | 2.1267 | 2.2152 | 2.3026 |
| .920          | 1.5325          | 1.6434 | 1.7508 | 1.8552 | 1.9568 | 2.0562 | 2.1534 | 2.2488 | 2.3426 | 2.4348 | 2.5257 |
| .940          | 1.7687          | 1.8862 | 1.9996 | 2.1097 | 2.2167 | 2.3212 | 2.4233 | 2.5234 | 2.6217 | 2.7183 | 2.8134 |
| .950          | 1.9207          | 2.0420 | 2.1590 | 2.2724 | 2.3826 | 2.4901 | 2.5951 | 2.6980 | 2.7990 | 2.8981 | 2.9957 |
| .960          | 2.1089          | 2.2346 | 2.3557 | 2.4729 | 2.5868 | 2.6977 | 2.8061 | 2.9122 | 3.0162 | 3.1184 | 3.2189 |
| .970          | 2.3546          | 2.4855 | 2.6115 | 2.7333 | 2.8516 | 2.9667 | 3.0791 | 3.1891 | 3.2968 | 3.4026 | 3.5066 |
| .980          | 2.7059          | 2.8435 | 2.9757 | 3.1035 | 3.2275 | 3.3480 | 3.4656 | 3.5805 | 3.6931 | 3.8035 | 3.9120 |
| .990          | 3.3175          | 3.4649 | 3.6066 | 3.7433 | 3.8757 | 4.0044 | 4.1299 | 4.2524 | 4.3723 | 4.4898 | 4.6052 |
| .995          | 3.9397          | 4.0957 | 4.2455 | 4.3899 | 4.5297 | 4.6655 | 4.7978 | 4.9269 | 5.0532 | 5.1769 | 5.2983 |
| .999          | 5.4138          | 5.5859 | 5.7508 | 5.9099 | 6.0637 | 6.2130 | 6.3584 | 6.5002 | 6.6378 | 6.7747 | 6.9077 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 1.00            | 1.05   | 1.10   | 1.15   | 1.20   | 1.25   | 1.30   | 1.35   | 1.40   | 1.45   | 1.50   |
| .001          | 0.0010          | 0.0014 | 0.0020 | 0.0026 | 0.0034 | 0.0044 | 0.0056 | 0.0069 | 0.0084 | 0.0102 | 0.0121 |
| .005          | 0.0050          | 0.0066 | 0.0085 | 0.0107 | 0.0132 | 0.0161 | 0.0193 | 0.0229 | 0.0268 | 0.0312 | 0.0359 |
| .010          | 0.0101          | 0.0128 | 0.0160 | 0.0196 | 0.0236 | 0.0281 | 0.0331 | 0.0385 | 0.0443 | 0.0506 | 0.0574 |
| .020          | 0.0202          | 0.0249 | 0.0302 | 0.0360 | 0.0424 | 0.0494 | 0.0569 | 0.0650 | 0.0736 | 0.0828 | 0.0924 |
| .030          | 0.0305          | 0.0369 | 0.0439 | 0.0516 | 0.0600 | 0.0689 | 0.0785 | 0.0887 | 0.0994 | 0.1107 | 0.1225 |
| .040          | 0.0408          | 0.0488 | 0.0574 | 0.0667 | 0.0768 | 0.0875 | 0.0988 | 0.1107 | 0.1233 | 0.1364 | 0.1501 |
| .050          | 0.0513          | 0.0606 | 0.0708 | 0.0816 | 0.0931 | 0.1054 | 0.1183 | 0.1318 | 0.1459 | 0.1606 | 0.1759 |
| .060          | 0.0619          | 0.0726 | 0.0840 | 0.0963 | 0.1092 | 0.1229 | 0.1372 | 0.1521 | 0.1677 | 0.1839 | 0.2006 |
| .080          | 0.0834          | 0.0965 | 0.1105 | 0.1253 | 0.1408 | 0.1570 | 0.1739 | 0.1914 | 0.2095 | 0.2282 | 0.2475 |
| .100          | 0.1054          | 0.1208 | 0.1371 | 0.1541 | 0.1719 | 0.1904 | 0.2096 | 0.2293 | 0.2497 | 0.2707 | 0.2922 |
| .120          | 0.1278          | 0.1454 | 0.1638 | 0.1830 | 0.2029 | 0.2235 | 0.2447 | 0.2666 | 0.2890 | 0.3120 | 0.3355 |
| .140          | 0.1508          | 0.1704 | 0.1908 | 0.2120 | 0.2338 | 0.2564 | 0.2796 | 0.3034 | 0.3277 | 0.3526 | 0.3779 |
| .160          | 0.1744          | 0.1959 | 0.2182 | 0.2412 | 0.2650 | 0.2893 | 0.3144 | 0.3399 | 0.3660 | 0.3927 | 0.4197 |
| .180          | 0.1985          | 0.2218 | 0.2459 | 0.2708 | 0.2963 | 0.3225 | 0.3492 | 0.3765 | 0.4042 | 0.4325 | 0.4612 |
| .200          | 0.2231          | 0.2483 | 0.2742 | 0.3007 | 0.3280 | 0.3558 | 0.3842 | 0.4131 | 0.4425 | 0.4723 | 0.5026 |
| .220          | 0.2485          | 0.2753 | 0.3029 | 0.3312 | 0.3600 | 0.3895 | 0.4194 | 0.4499 | 0.4808 | 0.5122 | 0.5439 |
| .240          | 0.2744          | 0.3030 | 0.3322 | 0.3621 | 0.3926 | 0.4236 | 0.4551 | 0.4870 | 0.5194 | 0.5522 | 0.5854 |
| .260          | 0.3011          | 0.3313 | 0.3622 | 0.3936 | 0.4256 | 0.4581 | 0.4911 | 0.5246 | 0.5584 | 0.5926 | 0.6272 |
| .280          | 0.3285          | 0.3603 | 0.3928 | 0.4258 | 0.4593 | 0.4933 | 0.5277 | 0.5626 | 0.5978 | 0.6334 | 0.6693 |
| .300          | 0.3567          | 0.3901 | 0.4241 | 0.4586 | 0.4936 | 0.5290 | 0.5649 | 0.6011 | 0.6377 | 0.6746 | 0.7118 |
| .320          | 0.3857          | 0.4206 | 0.4561 | 0.4921 | 0.5286 | 0.5655 | 0.6027 | 0.6403 | 0.6782 | 0.7164 | 0.7549 |
| .340          | 0.4155          | 0.4520 | 0.4890 | 0.5265 | 0.5644 | 0.6026 | 0.6412 | 0.6802 | 0.7194 | 0.7589 | 0.7987 |
| .360          | 0.4463          | 0.4843 | 0.5228 | 0.5617 | 0.6010 | 0.6407 | 0.6806 | 0.7208 | 0.7614 | 0.8021 | 0.8431 |
| .380          | 0.4780          | 0.5176 | 0.5575 | 0.5979 | 0.6386 | 0.6796 | 0.7209 | 0.7624 | 0.8042 | 0.8462 | 0.8884 |
| .400          | 0.5108          | 0.5519 | 0.5933 | 0.6351 | 0.6771 | 0.7195 | 0.7621 | 0.8049 | 0.8479 | 0.8912 | 0.9346 |
| .420          | 0.5447          | 0.5873 | 0.6301 | 0.6733 | 0.7168 | 0.7604 | 0.8043 | 0.8484 | 0.8927 | 0.9372 | 0.9818 |
| .440          | 0.5798          | 0.6238 | 0.6682 | 0.7127 | 0.7575 | 0.8026 | 0.8478 | 0.8931 | 0.9387 | 0.9843 | 1.0301 |
| .460          | 0.6162          | 0.6617 | 0.7075 | 0.7534 | 0.7996 | 0.8459 | 0.8924 | 0.9391 | 0.9858 | 1.0327 | 1.0797 |
| .480          | 0.6539          | 0.7009 | 0.7481 | 0.7955 | 0.8430 | 0.8907 | 0.9385 | 0.9864 | 1.0344 | 1.0824 | 1.1306 |
| .500          | 0.6931          | 0.7416 | 0.7903 | 0.8390 | 0.8879 | 0.9369 | 0.9860 | 1.0352 | 1.0844 | 1.1337 | 1.1830 |
| .520          | 0.7340          | 0.7839 | 0.8340 | 0.8842 | 0.9345 | 0.9848 | 1.0352 | 1.0856 | 1.1360 | 1.1865 | 1.2370 |
| .540          | 0.7765          | 0.8280 | 0.8796 | 0.9311 | 0.9828 | 1.0344 | 1.0861 | 1.1378 | 1.1895 | 1.2412 | 1.2929 |
| .560          | 0.8209          | 0.8740 | 0.9270 | 0.9800 | 1.0330 | 1.0860 | 1.1390 | 1.1919 | 1.2449 | 1.2978 | 1.3507 |
| .580          | 0.8675          | 0.9220 | 0.9765 | 1.0310 | 1.0853 | 1.1397 | 1.1940 | 1.2482 | 1.3024 | 1.3566 | 1.4107 |
| .600          | 0.9163          | 0.9724 | 1.0283 | 1.0842 | 1.1400 | 1.1958 | 1.2514 | 1.3069 | 1.3624 | 1.4178 | 1.4731 |
| .620          | 0.9676          | 1.0252 | 1.0827 | 1.1401 | 1.1973 | 1.2544 | 1.3114 | 1.3683 | 1.4250 | 1.4816 | 1.5382 |
| .640          | 1.0217          | 1.0809 | 1.1399 | 1.1988 | 1.2574 | 1.3160 | 1.3743 | 1.4325 | 1.4906 | 1.5485 | 1.6063 |
| .660          | 1.0788          | 1.1397 | 1.2003 | 1.2606 | 1.3208 | 1.3807 | 1.4333 | 1.5001 | 1.5594 | 1.6187 | 1.6693 |
| .680          | 1.1394          | 1.2019 | 1.2641 | 1.3261 | 1.3877 | 1.4491 | 1.5103 | 1.5713 | 1.6320 | 1.6926 | 1.7529 |
| .700          | 1.2040          | 1.2682 | 1.3320 | 1.3955 | 1.4587 | 1.5197 | 1.5843 | 1.6467 | 1.7088 | 1.7707 | 1.8324 |
| .720          | 1.2730          | 1.3389 | 1.4044 | 1.4696 | 1.5344 | 1.5989 | 1.6630 | 1.7266 | 1.7904 | 1.8538 | 1.9168 |
| .740          | 1.3471          | 1.4148 | 1.4821 | 1.5489 | 1.6154 | 1.6814 | 1.7471 | 1.8125 | 1.8776 | 1.9423 | 2.0068 |
| .760          | 1.4271          | 1.4967 | 1.5658 | 1.6344 | 1.7025 | 1.7703 | 1.8376 | 1.9045 | 1.9711 | 2.0374 | 2.1033 |
| .780          | 1.5141          | 1.5857 | 1.6567 | 1.7271 | 1.7970 | 1.8664 | 1.9354 | 2.0040 | 2.0722 | 2.1400 | 2.2075 |
| .800          | 1.6094          | 1.6830 | 1.7560 | 1.8283 | 1.9001 | 1.9713 | 2.0421 | 2.1124 | 2.1823 | 2.2517 | 2.3208 |
| .820          | 1.7148          | 1.7905 | 1.8656 | 1.9399 | 2.0137 | 2.0868 | 2.1595 | 2.2316 | 2.3032 | 2.3744 | 2.4437 |
| .840          | 1.8326          | 1.9106 | 1.9879 | 2.0644 | 2.1375 | 2.2154 | 2.2900 | 2.3641 | 2.4376 | 2.5107 | 2.5833 |
| .860          | 1.9661          | 2.0466 | 2.1263 | 2.2051 | 2.2832 | 2.3606 | 2.4373 | 2.5135 | 2.5891 | 2.6641 | 2.7387 |
| .880          | 2.1203          | 2.2035 | 2.2857 | 2.3671 | 2.4477 | 2.5275 | 2.6066 | 2.6850 | 2.7628 | 2.8400 | 2.9167 |
| .900          | 2.3026          | 2.3888 | 2.4740 | 2.5582 | 2.6415 | 2.7239 | 2.8056 | 2.8866 | 2.9669 | 3.0466 | 3.1257 |
| .920          | 2.5257          | 2.6154 | 2.7039 | 2.7913 | 2.8777 | 2.9633 | 3.0480 | 3.1319 | 3.2151 | 3.2975 | 3.3793 |
| .940          | 2.8134          | 2.9071 | 2.9996 | 3.0909 | 3.1811 | 3.2703 | 3.3585 | 3.4459 | 3.5325 | 3.6183 | 3.7034 |
| .950          | 2.9957          | 3.0919 | 3.1867 | 3.2802 | 3.3727 | 3.4640 | 3.5544 | 3.6439 | 3.7325 | 3.8203 | 3.9074 |
| .960          | 3.2189          | 3.3178 | 3.4153 | 3.5115 | 3.6066 | 3.7005 | 3.7933 | 3.8852 | 3.9762 | 4.0663 | 4.1556 |
| .970          | 3.5066          | 3.6089 | 3.7097 | 3.8091 | 3.9073 | 4.0042 | 4.1000 | 4.1948 | 4.2887 | 4.3816 | 4.4736 |
| .980          | 3.9120          | 4.0187 | 4.1238 | 4.2274 | 4.3296 | 4.4306 | 4.5303 | 4.6289 | 4.7265 | 4.8230 | 4.9187 |
| .990          | 4.6052          | 4.7186 | 4.8302 | 4.9402 | 5.0486 | 5.1556 | 5.2613 | 5.3658 | 5.4691 | 5.5712 | 5.6724 |
| .995          | 5.2983          | 5.4176 | 5.5350 | 5.6506 | 5.7645 | 5.8769 | 5.9878 | 6.0975 | 6.2058 | 6.3130 | 6.4191 |
| .999          | 6.9077          | 7.0385 | 7.1670 | 7.2935 | 7.4182 | 7.5411 | 7.6623 | 7.7820 | 7.9004 | 8.0174 | 8.1331 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 1.50            | 1.55   | 1.60   | 1.65   | 1.70   | 1.75   | 1.80   | 1.85   | 1.90   | 1.95   | 2.00   |
| .001          | 0.0121          | 0.0143 | 0.0168 | 0.0195 | 0.0224 | 0.0256 | 0.0290 | 0.0327 | 0.0367 | 0.0409 | 0.0454 |
| .005          | 0.0359          | 0.0409 | 0.0464 | 0.0523 | 0.0585 | 0.0651 | 0.0720 | 0.0793 | 0.0870 | 0.0951 | 0.1035 |
| .010          | 0.0574          | 0.0646 | 0.0723 | 0.0804 | 0.0889 | 0.0978 | 0.1072 | 0.1169 | 0.1271 | 0.1376 | 0.1486 |
| .020          | 0.0924          | 0.1026 | 0.1132 | 0.1244 | 0.1360 | 0.1480 | 0.1605 | 0.1734 | 0.1868 | 0.2005 | 0.2147 |
| .030          | 0.1225          | 0.1349 | 0.1478 | 0.1612 | 0.1751 | 0.1894 | 0.2042 | 0.2194 | 0.2350 | 0.2511 | 0.2675 |
| .040          | 0.1501          | 0.1643 | 0.1790 | 0.1943 | 0.2100 | 0.2262 | 0.2428 | 0.2599 | 0.2774 | 0.2953 | 0.3136 |
| .050          | 0.1759          | 0.1917 | 0.2081 | 0.2249 | 0.2422 | 0.2600 | 0.2783 | 0.2969 | 0.3160 | 0.3355 | 0.3554 |
| .060          | 0.2006          | 0.2178 | 0.2356 | 0.2539 | 0.2726 | 0.2919 | 0.3115 | 0.3316 | 0.3521 | 0.3729 | 0.3942 |
| .080          | 0.2475          | 0.2673 | 0.2876 | 0.3083 | 0.3296 | 0.3513 | 0.3734 | 0.3959 | 0.4188 | 0.4421 | 0.4657 |
| .100          | 0.2922          | 0.3142 | 0.3367 | 0.3597 | 0.3831 | 0.4069 | 0.4311 | 0.4558 | 0.4808 | 0.5061 | 0.5318 |
| .120          | 0.3355          | 0.3595 | 0.3840 | 0.4089 | 0.4342 | 0.4600 | 0.4861 | 0.5126 | 0.5395 | 0.5667 | 0.5942 |
| .140          | 0.3779          | 0.4038 | 0.4300 | 0.4567 | 0.4839 | 0.5114 | 0.5392 | 0.5674 | 0.5960 | 0.6249 | 0.6540 |
| .160          | 0.4197          | 0.4473 | 0.4753 | 0.5036 | 0.5324 | 0.5615 | 0.5910 | 0.6208 | 0.6509 | 0.6813 | 0.7120 |
| .180          | 0.4612          | 0.4904 | 0.5199 | 0.5499 | 0.5802 | 0.6108 | 0.6418 | 0.6731 | 0.7047 | 0.7365 | 0.7687 |
| .200          | 0.5026          | 0.5333 | 0.5643 | 0.5957 | 0.6275 | 0.6596 | 0.6920 | 0.7247 | 0.7577 | 0.7909 | 0.8244 |
| .220          | 0.5439          | 0.5761 | 0.6086 | 0.6414 | 0.6746 | 0.7080 | 0.7418 | 0.7758 | 0.8101 | 0.8447 | 0.8794 |
| .240          | 0.5854          | 0.6190 | 0.6529 | 0.6871 | 0.7216 | 0.7563 | 0.7914 | 0.8267 | 0.8623 | 0.8980 | 0.9341 |
| .260          | 0.6272          | 0.6621 | 0.6973 | 0.7328 | 0.7686 | 0.8047 | 0.8410 | 0.8775 | 0.9143 | 0.9513 | 0.9885 |
| .280          | 0.6693          | 0.7055 | 0.7420 | 0.7788 | 0.8158 | 0.8531 | 0.8907 | 0.9284 | 0.9664 | 1.0045 | 1.0428 |
| .300          | 0.7118          | 0.7493 | 0.7871 | 0.8251 | 0.8634 | 0.9019 | 0.9406 | 0.9795 | 1.0186 | 1.0579 | 1.0973 |
| .320          | 0.7549          | 0.7937 | 0.8327 | 0.8719 | 0.9114 | 0.9511 | 0.9909 | 1.0310 | 1.0712 | 1.1116 | 1.1521 |
| .340          | 0.7987          | 0.8387 | 0.8789 | 0.9193 | 0.9599 | 1.0007 | 1.0417 | 1.0829 | 1.1242 | 1.1657 | 1.2073 |
| .360          | 0.8431          | 0.8843 | 0.9257 | 0.9673 | 1.0091 | 1.0510 | 1.0931 | 1.1354 | 1.1778 | 1.2203 | 1.2630 |
| .380          | 0.8884          | 0.9308 | 0.9734 | 1.0161 | 1.0590 | 1.1021 | 1.1453 | 1.1886 | 1.2321 | 1.2756 | 1.3193 |
| .400          | 0.9346          | 0.9782 | 1.0219 | 1.0658 | 1.1098 | 1.1540 | 1.1982 | 1.2426 | 1.2871 | 1.3317 | 1.3695 |
| .420          | 0.9818          | 1.0265 | 1.0714 | 1.1164 | 1.1615 | 1.2068 | 1.2522 | 1.2976 | 1.3431 | 1.3887 | 1.4344 |
| .440          | 1.0301          | 1.0760 | 1.1221 | 1.1682 | 1.2144 | 1.2607 | 1.3072 | 1.3536 | 1.4002 | 1.4468 | 1.4935 |
| .460          | 1.0797          | 1.1267 | 1.1739 | 1.2212 | 1.2685 | 1.3159 | 1.3633 | 1.4109 | 1.4584 | 1.5061 | 1.5537 |
| .480          | 1.1306          | 1.1788 | 1.2271 | 1.2755 | 1.3239 | 1.3723 | 1.4209 | 1.4694 | 1.5180 | 1.5666 | 1.6153 |
| .500          | 1.1830          | 1.2324 | 1.2818 | 1.3313 | 1.3808 | 1.4303 | 1.4799 | 1.5294 | 1.5791 | 1.6287 | 1.6783 |
| .520          | 1.2370          | 1.2876 | 1.3381 | 1.3887 | 1.4388 | 1.4899 | 1.5405 | 1.5911 | 1.6418 | 1.6924 | 1.7430 |
| .540          | 1.2929          | 1.3446 | 1.3962 | 1.4479 | 1.4959 | 1.5513 | 1.6030 | 1.6546 | 1.7063 | 1.7579 | 1.8096 |
| .560          | 1.3507          | 1.4035 | 1.4564 | 1.5092 | 1.5620 | 1.6147 | 1.6675 | 1.7116 | 1.7728 | 1.8255 | 1.8781 |
| .580          | 1.4107          | 1.4647 | 1.5187 | 1.5726 | 1.6265 | 1.6804 | 1.7342 | 1.7879 | 1.8417 | 1.8953 | 1.9489 |
| .600          | 1.4731          | 1.5283 | 1.5835 | 1.6386 | 1.6936 | 1.7485 | 1.8034 | 1.8582 | 1.9130 | 1.9674 | 2.0223 |
| .620          | 1.5382          | 1.5946 | 1.6510 | 1.7072 | 1.7633 | 1.8194 | 1.8754 | 1.9313 | 1.9871 | 2.0428 | 2.0985 |
| .640          | 1.6063          | 1.6639 | 1.7215 | 1.7789 | 1.8362 | 1.8934 | 1.9505 | 2.0075 | 2.0643 | 2.1211 | 2.1779 |
| .660          | 1.6693          | 1.7366 | 1.7954 | 1.8540 | 1.9125 | 1.9708 | 2.0290 | 2.0871 | 2.1451 | 2.2030 | 2.2608 |
| .680          | 1.7529          | 1.8131 | 1.8731 | 1.9329 | 1.9926 | 2.0521 | 2.1115 | 2.1708 | 2.2299 | 2.2889 | 2.3477 |
| .700          | 1.8324          | 1.8939 | 1.9552 | 2.0163 | 2.0765 | 2.1379 | 2.1985 | 2.2589 | 2.3191 | 2.3792 | 2.4392 |
| .720          | 1.9168          | 1.9796 | 2.0422 | 2.1046 | 2.1668 | 2.2287 | 2.2905 | 2.3521 | 2.4136 | 2.4748 | 2.5359 |
| .740          | 2.0068          | 2.0710 | 2.1350 | 2.1987 | 2.2621 | 2.3254 | 2.3884 | 2.4513 | 2.5139 | 2.5764 | 2.6387 |
| .760          | 2.1033          | 2.1690 | 2.2343 | 2.2994 | 2.3642 | 2.4288 | 2.4932 | 2.5573 | 2.6212 | 2.6849 | 2.7485 |
| .780          | 2.2075          | 2.2746 | 2.3415 | 2.4080 | 2.4742 | 2.5402 | 2.6059 | 2.6714 | 2.7358 | 2.8017 | 2.8665 |
| .800          | 2.3208          | 2.3895 | 2.4579 | 2.5133 | 2.5937 | 2.6611 | 2.7283 | 2.7881 | 2.8618 | 2.9282 | 2.9943 |
| .820          | 2.4437          | 2.5156 | 2.5856 | 2.6552 | 2.7245 | 2.7935 | 2.8622 | 2.9306 | 2.9987 | 3.0665 | 3.1341 |
| .840          | 2.5833          | 2.6554 | 2.7135 | 2.7985 | 2.8695 | 2.9401 | 3.0104 | 3.0804 | 3.1501 | 3.2194 | 3.2885 |
| .860          | 2.7387          | 2.8126 | 2.8864 | 2.9596 | 3.0324 | 3.1048 | 3.1768 | 3.2485 | 3.3199 | 3.3909 | 3.4616 |
| .880          | 2.9167          | 2.9929 | 3.0686 | 3.1438 | 3.2186 | 3.2929 | 3.3669 | 3.4405 | 3.5137 | 3.5865 | 3.6591 |
| .900          | 3.1257          | 3.2042 | 3.2822 | 3.3597 | 3.4366 | 3.5132 | 3.5893 | 3.6650 | 3.7403 | 3.8152 | 3.8897 |
| .920          | 3.3793          | 3.4605 | 3.5412 | 3.6212 | 3.7008 | 3.7798 | 3.8584 | 3.9365 | 4.0141 | 4.0914 | 4.1683 |
| .940          | 3.7034          | 3.7879 | 3.8716 | 3.9548 | 4.0374 | 4.1194 | 4.2009 | 4.2819 | 4.3625 | 4.4425 | 4.5222 |
| .950          | 3.9074          | 3.9937 | 4.0793 | 4.1643 | 4.2487 | 4.3326 | 4.4158 | 4.4986 | 4.5808 | 4.6626 | 4.7431 |
| .960          | 4.1556          | 4.2441 | 4.3320 | 4.4191 | 4.5056 | 4.5915 | 4.6768 | 4.7616 | 4.8458 | 4.9295 | 5.0128 |
| .970          | 4.4736          | 4.5649 | 4.6554 | 4.7451 | 4.8342 | 4.9226 | 5.0104 | 5.0976 | 5.1843 | 5.2704 | 5.3560 |
| .980          | 4.9187          | 5.0135 | 5.1074 | 5.2006 | 5.2931 | 5.3848 | 5.4758 | 5.5662 | 5.6560 | 5.7453 | 5.8339 |
| .990          | 5.6724          | 5.7726 | 5.8719 | 5.9704 | 6.0680 | 6.1648 | 6.2609 | 6.3562 | 6.4509 | 6.5449 | 6.6383 |
| .995          | 6.4191          | 6.5241 | 6.6281 | 6.7312 | 6.8334 | 6.9348 | 7.0354 | 7.1351 | 7.2341 | 7.3325 | 7.4301 |
| .999          | 8.1331          | 8.2476 | 8.3609 | 8.4732 | 8.5845 | 8.6949 | 8.8043 | 8.9129 | 9.0204 | 9.1273 | 9.2333 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |       |       |       |       |       |       |       |        |        |        |
|---------------|-----------------|-------|-------|-------|-------|-------|-------|-------|--------|--------|--------|
|               | 2.00            | 2.05  | 2.10  | 2.15  | 2.20  | 2.25  | 2.30  | 2.35  | 2.40   | 2.45   | 2.50   |
| .001          | 0.045           | 0.050 | 0.055 | 0.061 | 0.066 | 0.072 | 0.078 | 0.084 | 0.091  | 0.098  | 0.105  |
| .005          | 0.103           | 0.112 | 0.121 | 0.131 | 0.141 | 0.151 | 0.161 | 0.172 | 0.183  | 0.194  | 0.206  |
| .010          | 0.149           | 0.160 | 0.172 | 0.184 | 0.196 | 0.209 | 0.222 | 0.235 | 0.249  | 0.263  | 0.277  |
| .020          | 0.215           | 0.229 | 0.244 | 0.259 | 0.275 | 0.291 | 0.307 | 0.324 | 0.341  | 0.358  | 0.376  |
| .030          | 0.268           | 0.284 | 0.302 | 0.319 | 0.337 | 0.355 | 0.374 | 0.393 | 0.412  | 0.432  | 0.452  |
| .040          | 0.314           | 0.332 | 0.351 | 0.371 | 0.390 | 0.411 | 0.431 | 0.452 | 0.473  | 0.494  | 0.516  |
| .050          | 0.355           | 0.376 | 0.396 | 0.417 | 0.438 | 0.460 | 0.482 | 0.504 | 0.527  | 0.550  | 0.573  |
| .060          | 0.394           | 0.416 | 0.438 | 0.460 | 0.483 | 0.506 | 0.529 | 0.553 | 0.576  | 0.601  | 0.625  |
| .080          | 0.466           | 0.490 | 0.514 | 0.539 | 0.564 | 0.589 | 0.615 | 0.640 | 0.666  | 0.693  | 0.720  |
| .100          | 0.532           | 0.558 | 0.584 | 0.611 | 0.638 | 0.665 | 0.693 | 0.720 | 0.748  | 0.777  | 0.805  |
| .120          | 0.594           | 0.622 | 0.650 | 0.679 | 0.707 | 0.736 | 0.766 | 0.795 | 0.825  | 0.855  | 0.885  |
| .140          | 0.654           | 0.684 | 0.713 | 0.743 | 0.774 | 0.804 | 0.835 | 0.866 | 0.897  | 0.929  | 0.960  |
| .160          | 0.712           | 0.743 | 0.774 | 0.806 | 0.838 | 0.870 | 0.902 | 0.934 | 0.967  | 1.000  | 1.033  |
| .180          | 0.769           | 0.801 | 0.834 | 0.867 | 0.900 | 0.933 | 0.967 | 1.000 | 1.034  | 1.069  | 1.103  |
| .200          | 0.824           | 0.858 | 0.892 | 0.926 | 0.961 | 0.995 | 1.030 | 1.065 | 1.100  | 1.136  | 1.171  |
| .220          | 0.879           | 0.914 | 0.950 | 0.985 | 1.021 | 1.057 | 1.093 | 1.129 | 1.165  | 1.202  | 1.238  |
| .240          | 0.934           | 0.970 | 1.007 | 1.043 | 1.080 | 1.117 | 1.154 | 1.192 | 1.229  | 1.267  | 1.304  |
| .260          | 0.988           | 1.026 | 1.063 | 1.101 | 1.139 | 1.177 | 1.215 | 1.254 | 1.292  | 1.331  | 1.370  |
| .280          | 1.043           | 1.081 | 1.120 | 1.159 | 1.198 | 1.237 | 1.276 | 1.316 | 1.355  | 1.395  | 1.435  |
| .300          | 1.097           | 1.137 | 1.177 | 1.217 | 1.257 | 1.297 | 1.337 | 1.378 | 1.418  | 1.459  | 1.500  |
| .320          | 1.152           | 1.193 | 1.234 | 1.275 | 1.316 | 1.357 | 1.398 | 1.440 | 1.481  | 1.522  | 1.565  |
| .340          | 1.207           | 1.249 | 1.291 | 1.333 | 1.375 | 1.417 | 1.460 | 1.502 | 1.545  | 1.587  | 1.630  |
| .360          | 1.263           | 1.306 | 1.349 | 1.392 | 1.435 | 1.478 | 1.521 | 1.565 | 1.608  | 1.652  | 1.695  |
| .380          | 1.319           | 1.363 | 1.407 | 1.451 | 1.495 | 1.539 | 1.583 | 1.628 | 1.672  | 1.717  | 1.761  |
| .400          | 1.370           | 1.421 | 1.466 | 1.511 | 1.556 | 1.601 | 1.646 | 1.692 | 1.737  | 1.782  | 1.828  |
| .420          | 1.434           | 1.480 | 1.525 | 1.572 | 1.618 | 1.664 | 1.710 | 1.756 | 1.803  | 1.849  | 1.895  |
| .440          | 1.494           | 1.540 | 1.587 | 1.634 | 1.681 | 1.728 | 1.775 | 1.822 | 1.869  | 1.916  | 1.963  |
| .460          | 1.554           | 1.601 | 1.649 | 1.697 | 1.745 | 1.793 | 1.841 | 1.889 | 1.937  | 1.985  | 2.033  |
| .480          | 1.615           | 1.664 | 1.713 | 1.762 | 1.810 | 1.859 | 1.908 | 1.957 | 2.006  | 2.055  | 2.104  |
| .500          | 1.678           | 1.728 | 1.778 | 1.827 | 1.877 | 1.927 | 1.977 | 2.026 | 2.076  | 2.126  | 2.176  |
| .520          | 1.743           | 1.794 | 1.844 | 1.895 | 1.946 | 1.996 | 2.047 | 2.098 | 2.148  | 2.199  | 2.250  |
| .540          | 1.810           | 1.861 | 1.913 | 1.964 | 2.016 | 2.068 | 2.119 | 2.171 | 2.222  | 2.262  | 2.325  |
| .560          | 1.878           | 1.931 | 1.983 | 2.036 | 2.088 | 2.141 | 2.193 | 2.246 | 2.298  | 2.351  | 2.403  |
| .580          | 1.949           | 2.003 | 2.056 | 2.110 | 2.163 | 2.217 | 2.270 | 2.323 | 2.377  | 2.430  | 2.483  |
| .600          | 2.022           | 2.077 | 2.131 | 2.186 | 2.240 | 2.295 | 2.349 | 2.403 | 2.458  | 2.512  | 2.566  |
| .620          | 2.099           | 2.154 | 2.210 | 2.265 | 2.320 | 2.376 | 2.431 | 2.486 | 2.541  | 2.597  | 2.652  |
| .640          | 2.178           | 2.234 | 2.291 | 2.347 | 2.404 | 2.460 | 2.516 | 2.573 | 2.629  | 2.685  | 2.741  |
| .660          | 2.261           | 2.318 | 2.376 | 2.433 | 2.491 | 2.548 | 2.605 | 2.663 | 2.720  | 2.777  | 2.833  |
| .680          | 2.348           | 2.406 | 2.465 | 2.524 | 2.582 | 2.627 | 2.699 | 2.743 | 2.815  | 2.873  | 2.923  |
| .700          | 2.439           | 2.499 | 2.559 | 2.618 | 2.678 | 2.737 | 2.796 | 2.855 | 2.914  | 2.973  | 3.032  |
| .720          | 2.536           | 2.597 | 2.658 | 2.718 | 2.779 | 2.839 | 2.900 | 2.960 | 3.020  | 3.080  | 3.140  |
| .740          | 2.639           | 2.701 | 2.763 | 2.825 | 2.886 | 2.948 | 3.009 | 3.070 | 3.131  | 3.192  | 3.253  |
| .760          | 2.748           | 2.812 | 2.875 | 2.938 | 3.001 | 3.063 | 3.126 | 3.188 | 3.250  | 3.312  | 3.374  |
| .780          | 2.866           | 2.931 | 2.995 | 3.060 | 3.124 | 3.188 | 3.251 | 3.315 | 3.378  | 3.441  | 3.504  |
| .800          | 2.994           | 3.060 | 3.126 | 3.191 | 3.257 | 3.322 | 3.387 | 3.451 | 3.516  | 3.580  | 3.645  |
| .820          | 3.134           | 3.201 | 3.268 | 3.335 | 3.402 | 3.468 | 3.535 | 3.601 | 3.666  | 3.727  | 3.798  |
| .840          | 3.289           | 3.357 | 3.426 | 3.494 | 3.562 | 3.630 | 3.698 | 3.765 | 3.832  | 3.899  | 3.966  |
| .860          | 3.462           | 3.532 | 3.602 | 3.672 | 3.742 | 3.811 | 3.880 | 3.949 | 4.018  | 4.086  | 4.155  |
| .880          | 3.659           | 3.731 | 3.803 | 3.875 | 3.946 | 4.017 | 4.088 | 4.159 | 4.229  | 4.299  | 4.369  |
| .900          | 3.890           | 3.964 | 4.038 | 4.111 | 4.185 | 4.258 | 4.330 | 4.403 | 4.475  | 4.547  | 4.618  |
| .920          | 4.168           | 4.245 | 4.321 | 4.397 | 4.472 | 4.547 | 4.622 | 4.696 | 4.771  | 4.845  | 4.918  |
| .940          | 4.522           | 4.601 | 4.680 | 4.759 | 4.837 | 4.914 | 4.992 | 5.069 | 5.146  | 5.222  | 5.298  |
| .950          | 4.743           | 4.825 | 4.905 | 4.985 | 5.065 | 5.144 | 5.223 | 5.302 | 5.380  | 5.458  | 5.535  |
| .960          | 5.013           | 5.096 | 5.178 | 5.260 | 5.341 | 5.422 | 5.503 | 5.583 | 5.663  | 5.743  | 5.822  |
| .970          | 5.356           | 5.441 | 5.526 | 5.610 | 5.693 | 5.777 | 5.860 | 5.942 | 6.024  | 6.106  | 6.187  |
| .980          | 5.834           | 5.922 | 6.010 | 6.097 | 6.183 | 6.270 | 6.355 | 6.441 | 6.525  | 6.610  | 6.694  |
| .990          | 6.638           | 6.731 | 6.823 | 6.915 | 7.006 | 7.097 | 7.187 | 7.277 | 7.366  | 7.455  | 7.543  |
| .995          | 7.430           | 7.527 | 7.624 | 7.719 | 7.815 | 7.909 | 8.003 | 8.097 | 8.190  | 8.283  | 8.375  |
| .999          | 9.233           | 9.339 | 9.443 | 9.547 | 9.651 | 9.753 | 9.855 | 9.957 | 10.057 | 10.158 | 10.257 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 2.50            | 2.55   | 2.60   | 2.65   | 2.70   | 2.75   | 2.80   | 2.85   | 2.90   | 2.95   | 3.00   |
| .001          | 0.105           | 0.113  | 0.120  | 0.128  | 0.136  | 0.145  | 0.153  | 0.162  | 0.172  | 0.181  | 0.191  |
| .005          | 0.206           | 0.218  | 0.230  | 0.243  | 0.255  | 0.268  | 0.282  | 0.295  | 0.309  | 0.323  | 0.338  |
| .010          | 0.277           | 0.292  | 0.307  | 0.322  | 0.337  | 0.353  | 0.369  | 0.386  | 0.402  | 0.419  | 0.436  |
| .020          | 0.376           | 0.394  | 0.412  | 0.431  | 0.449  | 0.468  | 0.488  | 0.507  | 0.527  | 0.547  | 0.567  |
| .030          | 0.452           | 0.472  | 0.492  | 0.513  | 0.534  | 0.555  | 0.576  | 0.598  | 0.620  | 0.642  | 0.665  |
| .040          | 0.516           | 0.538  | 0.560  | 0.582  | 0.605  | 0.628  | 0.651  | 0.674  | 0.698  | 0.722  | 0.746  |
| .050          | 0.573           | 0.596  | 0.620  | 0.644  | 0.668  | 0.692  | 0.717  | 0.742  | 0.767  | 0.792  | 0.818  |
| .060          | 0.625           | 0.650  | 0.675  | 0.700  | 0.725  | 0.751  | 0.777  | 0.803  | 0.829  | 0.856  | 0.882  |
| .080          | 0.720           | 0.746  | 0.774  | 0.801  | 0.828  | 0.856  | 0.884  | 0.912  | 0.941  | 0.970  | 0.998  |
| .100          | 0.805           | 0.834  | 0.863  | 0.892  | 0.921  | 0.951  | 0.981  | 1.011  | 1.041  | 1.072  | 1.102  |
| .120          | 0.885           | 0.915  | 0.946  | 0.977  | 1.008  | 1.039  | 1.070  | 1.102  | 1.134  | 1.166  | 1.198  |
| .140          | 0.960           | 0.992  | 1.024  | 1.057  | 1.089  | 1.122  | 1.155  | 1.188  | 1.221  | 1.254  | 1.287  |
| .160          | 1.033           | 1.066  | 1.099  | 1.133  | 1.167  | 1.201  | 1.235  | 1.269  | 1.304  | 1.338  | 1.373  |
| .180          | 1.103           | 1.137  | 1.172  | 1.207  | 1.242  | 1.277  | 1.312  | 1.348  | 1.384  | 1.419  | 1.455  |
| .200          | 1.171           | 1.207  | 1.243  | 1.279  | 1.315  | 1.351  | 1.388  | 1.424  | 1.461  | 1.498  | 1.535  |
| .220          | 1.238           | 1.275  | 1.312  | 1.349  | 1.387  | 1.424  | 1.462  | 1.499  | 1.537  | 1.575  | 1.613  |
| .240          | 1.304           | 1.342  | 1.380  | 1.419  | 1.457  | 1.495  | 1.534  | 1.573  | 1.612  | 1.650  | 1.689  |
| .260          | 1.370           | 1.409  | 1.448  | 1.487  | 1.527  | 1.566  | 1.606  | 1.645  | 1.685  | 1.725  | 1.765  |
| .280          | 1.435           | 1.475  | 1.515  | 1.555  | 1.596  | 1.636  | 1.677  | 1.717  | 1.758  | 1.799  | 1.840  |
| .300          | 1.500           | 1.541  | 1.582  | 1.623  | 1.664  | 1.706  | 1.747  | 1.789  | 1.830  | 1.872  | 1.914  |
| .320          | 1.565           | 1.607  | 1.649  | 1.691  | 1.733  | 1.775  | 1.818  | 1.860  | 1.902  | 1.945  | 1.988  |
| .340          | 1.630           | 1.673  | 1.715  | 1.759  | 1.802  | 1.845  | 1.888  | 1.931  | 1.975  | 2.018  | 2.062  |
| .360          | 1.695           | 1.739  | 1.783  | 1.827  | 1.871  | 1.915  | 1.959  | 2.003  | 2.047  | 2.091  | 2.136  |
| .380          | 1.761           | 1.806  | 1.851  | 1.895  | 1.940  | 1.985  | 2.030  | 2.075  | 2.120  | 2.165  | 2.210  |
| .400          | 1.828           | 1.873  | 1.919  | 1.964  | 2.010  | 2.056  | 2.102  | 2.147  | 2.193  | 2.239  | 2.285  |
| .420          | 1.895           | 1.941  | 1.988  | 2.034  | 2.081  | 2.127  | 2.174  | 2.221  | 2.267  | 2.314  | 2.361  |
| .440          | 1.963           | 2.011  | 2.058  | 2.105  | 2.153  | 2.189  | 2.247  | 2.295  | 2.342  | 2.390  | 2.437  |
| .460          | 2.033           | 2.081  | 2.129  | 2.177  | 2.225  | 2.274  | 2.322  | 2.370  | 2.418  | 2.467  | 2.515  |
| .480          | 2.104           | 2.152  | 2.201  | 2.250  | 2.299  | 2.348  | 2.396  | 2.447  | 2.496  | 2.545  | 2.594  |
| .500          | 2.176           | 2.226  | 2.275  | 2.325  | 2.375  | 2.425  | 2.475  | 2.524  | 2.574  | 2.624  | 2.674  |
| .520          | 2.250           | 2.300  | 2.351  | 2.402  | 2.452  | 2.503  | 2.553  | 2.604  | 2.655  | 2.705  | 2.756  |
| .540          | 2.325           | 2.377  | 2.428  | 2.480  | 2.531  | 2.583  | 2.634  | 2.686  | 2.737  | 2.788  | 2.840  |
| .560          | 2.403           | 2.455  | 2.508  | 2.560  | 2.612  | 2.665  | 2.717  | 2.769  | 2.821  | 2.872  | 2.924  |
| .580          | 2.483           | 2.536  | 2.590  | 2.643  | 2.696  | 2.749  | 2.802  | 2.841  | 2.906  | 2.954  | 3.013  |
| .600          | 2.566           | 2.620  | 2.674  | 2.728  | 2.782  | 2.836  | 2.890  | 2.944  | 2.998  | 3.052  | 3.105  |
| .620          | 2.652           | 2.707  | 2.762  | 2.815  | 2.871  | 2.919  | 2.981  | 3.036  | 3.090  | 3.145  | 3.200  |
| .640          | 2.741           | 2.797  | 2.852  | 2.908  | 2.964  | 3.020  | 3.075  | 3.131  | 3.186  | 3.242  | 3.297  |
| .660          | 2.833           | 2.890  | 2.947  | 3.004  | 3.060  | 3.116  | 3.173  | 3.230  | 3.286  | 3.342  | 3.397  |
| .680          | 2.923           | 2.988  | 3.046  | 3.103  | 3.161  | 3.218  | 3.276  | 3.333  | 3.390  | 3.447  | 3.505  |
| .700          | 3.032           | 3.091  | 3.150  | 3.208  | 3.267  | 3.325  | 3.383  | 3.441  | 3.500  | 3.558  | 3.616  |
| .720          | 3.140           | 3.199  | 3.259  | 3.318  | 3.378  | 3.437  | 3.496  | 3.555  | 3.615  | 3.673  | 3.732  |
| .740          | 3.253           | 3.314  | 3.375  | 3.435  | 3.496  | 3.556  | 3.616  | 3.676  | 3.736  | 3.796  | 3.856  |
| .760          | 3.374           | 3.436  | 3.498  | 3.559  | 3.621  | 3.682  | 3.743  | 3.804  | 3.865  | 3.926  | 3.987  |
| .780          | 3.504           | 3.567  | 3.630  | 3.693  | 3.755  | 3.817  | 3.880  | 3.942  | 4.004  | 4.056  | 4.128  |
| .800          | 3.645           | 3.709  | 3.773  | 3.836  | 3.900  | 3.964  | 4.027  | 4.090  | 4.153  | 4.216  | 4.279  |
| .820          | 3.798           | 3.863  | 3.928  | 3.993  | 4.058  | 4.123  | 4.187  | 4.251  | 4.316  | 4.380  | 4.444  |
| .840          | 3.966           | 4.033  | 4.099  | 4.166  | 4.232  | 4.298  | 4.363  | 4.429  | 4.494  | 4.560  | 4.625  |
| .860          | 4.155           | 4.223  | 4.290  | 4.358  | 4.426  | 4.492  | 4.560  | 4.627  | 4.694  | 4.761  | 4.827  |
| .880          | 4.369           | 4.438  | 4.508  | 4.577  | 4.646  | 4.715  | 4.783  | 4.852  | 4.920  | 4.988  | 5.056  |
| .900          | 4.618           | 4.690  | 4.761  | 4.832  | 4.902  | 4.973  | 5.043  | 5.113  | 5.183  | 5.253  | 5.322  |
| .920          | 4.918           | 4.992  | 5.065  | 5.138  | 5.210  | 5.283  | 5.355  | 5.427  | 5.499  | 5.569  | 5.642  |
| .940          | 5.298           | 5.374  | 5.449  | 5.525  | 5.600  | 5.675  | 5.749  | 5.823  | 5.897  | 5.971  | 6.045  |
| .950          | 5.535           | 5.613  | 5.690  | 5.766  | 5.843  | 5.919  | 5.995  | 6.070  | 6.146  | 6.221  | 6.296  |
| .960          | 5.822           | 5.901  | 5.980  | 6.058  | 6.136  | 6.214  | 6.291  | 6.369  | 6.446  | 6.522  | 6.599  |
| .970          | 6.187           | 6.268  | 6.349  | 6.429  | 6.509  | 6.589  | 6.669  | 6.748  | 6.827  | 6.905  | 6.984  |
| .980          | 6.694           | 6.778  | 6.861  | 6.944  | 7.027  | 7.109  | 7.191  | 7.273  | 7.355  | 7.436  | 7.517  |
| .990          | 7.543           | 7.631  | 7.719  | 7.806  | 7.893  | 7.979  | 8.065  | 8.151  | 8.236  | 8.321  | 8.406  |
| .995          | 8.375           | 8.466  | 8.558  | 8.649  | 8.739  | 8.829  | 8.919  | 9.008  | 9.097  | 9.186  | 9.274  |
| .999          | 10.257          | 10.357 | 10.456 | 10.554 | 10.651 | 10.749 | 10.846 | 10.942 | 11.038 | 11.134 | 11.229 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 3.00            | 3.05   | 3.10   | 3.15   | 3.20   | 3.25   | 3.30   | 3.35   | 3.40   | 3.45   | 3.50   |
| .001          | 0.191           | 0.200  | 0.211  | 0.221  | 0.231  | 0.242  | 0.253  | 0.264  | 0.276  | 0.287  | 0.299  |
| .005          | 0.338           | 0.352  | 0.367  | 0.382  | 0.398  | 0.413  | 0.429  | 0.445  | 0.461  | 0.478  | 0.495  |
| .010          | 0.436           | 0.453  | 0.471  | 0.489  | 0.507  | 0.525  | 0.543  | 0.562  | 0.581  | 0.600  | 0.620  |
| .020          | 0.567           | 0.588  | 0.608  | 0.629  | 0.651  | 0.672  | 0.694  | 0.715  | 0.738  | 0.760  | 0.782  |
| .030          | 0.665           | 0.687  | 0.710  | 0.733  | 0.757  | 0.780  | 0.804  | 0.828  | 0.852  | 0.876  | 0.901  |
| .040          | 0.746           | 0.771  | 0.795  | 0.820  | 0.845  | 0.870  | 0.895  | 0.921  | 0.947  | 0.972  | 0.999  |
| .050          | 0.818           | 0.843  | 0.869  | 0.896  | 0.922  | 0.948  | 0.975  | 1.002  | 1.029  | 1.056  | 1.084  |
| .060          | 0.882           | 0.909  | 0.937  | 0.964  | 0.991  | 1.019  | 1.047  | 1.075  | 1.103  | 1.132  | 1.160  |
| .080          | 0.998           | 1.027  | 1.057  | 1.086  | 1.115  | 1.145  | 1.175  | 1.205  | 1.235  | 1.266  | 1.296  |
| .100          | 1.102           | 1.133  | 1.164  | 1.195  | 1.226  | 1.257  | 1.289  | 1.321  | 1.352  | 1.384  | 1.417  |
| .120          | 1.198           | 1.230  | 1.262  | 1.295  | 1.328  | 1.360  | 1.393  | 1.427  | 1.460  | 1.493  | 1.527  |
| .140          | 1.287           | 1.321  | 1.355  | 1.389  | 1.423  | 1.457  | 1.491  | 1.526  | 1.560  | 1.595  | 1.630  |
| .160          | 1.373           | 1.408  | 1.443  | 1.478  | 1.513  | 1.549  | 1.584  | 1.620  | 1.655  | 1.691  | 1.727  |
| .180          | 1.455           | 1.491  | 1.527  | 1.564  | 1.600  | 1.637  | 1.673  | 1.710  | 1.747  | 1.784  | 1.821  |
| .200          | 1.535           | 1.572  | 1.609  | 1.647  | 1.684  | 1.722  | 1.759  | 1.797  | 1.835  | 1.873  | 1.911  |
| .220          | 1.613           | 1.651  | 1.689  | 1.728  | 1.766  | 1.805  | 1.843  | 1.882  | 1.921  | 1.960  | 1.999  |
| .240          | 1.689           | 1.720  | 1.768  | 1.807  | 1.847  | 1.886  | 1.926  | 1.965  | 2.005  | 2.045  | 2.085  |
| .260          | 1.765           | 1.805  | 1.845  | 1.885  | 1.926  | 1.966  | 2.007  | 2.047  | 2.088  | 2.118  | 2.170  |
| .280          | 1.840           | 1.881  | 1.922  | 1.963  | 2.004  | 2.045  | 2.087  | 2.128  | 2.170  | 2.211  | 2.253  |
| .300          | 1.914           | 1.956  | 1.998  | 2.040  | 2.082  | 2.124  | 2.166  | 2.197  | 2.251  | 2.293  | 2.336  |
| .320          | 1.988           | 2.030  | 2.073  | 2.116  | 2.159  | 2.202  | 2.245  | 2.288  | 2.331  | 2.375  | 2.418  |
| .340          | 2.062           | 2.105  | 2.149  | 2.192  | 2.225  | 2.280  | 2.324  | 2.368  | 2.412  | 2.456  | 2.500  |
| .360          | 2.136           | 2.180  | 2.225  | 2.269  | 2.314  | 2.358  | 2.403  | 2.447  | 2.492  | 2.537  | 2.582  |
| .380          | 2.210           | 2.255  | 2.301  | 2.346  | 2.391  | 2.437  | 2.482  | 2.527  | 2.573  | 2.618  | 2.664  |
| .400          | 2.285           | 2.331  | 2.377  | 2.423  | 2.469  | 2.515  | 2.562  | 2.608  | 2.654  | 2.700  | 2.747  |
| .420          | 2.361           | 2.408  | 2.454  | 2.501  | 2.548  | 2.595  | 2.642  | 2.689  | 2.736  | 2.783  | 2.830  |
| .440          | 2.437           | 2.485  | 2.532  | 2.580  | 2.628  | 2.675  | 2.723  | 2.771  | 2.818  | 2.866  | 2.914  |
| .460          | 2.515           | 2.563  | 2.612  | 2.657  | 2.708  | 2.757  | 2.805  | 2.854  | 2.902  | 2.950  | 2.999  |
| .480          | 2.594           | 2.643  | 2.692  | 2.741  | 2.790  | 2.839  | 2.888  | 2.938  | 2.987  | 3.036  | 3.085  |
| .500          | 2.674           | 2.724  | 2.774  | 2.824  | 2.874  | 2.923  | 2.973  | 3.023  | 3.073  | 3.123  | 3.173  |
| .520          | 2.756           | 2.807  | 2.857  | 2.908  | 2.959  | 3.009  | 3.060  | 3.110  | 3.161  | 3.212  | 3.258  |
| .540          | 2.840           | 2.891  | 2.943  | 2.994  | 3.045  | 3.097  | 3.148  | 3.200  | 3.251  | 3.302  | 3.354  |
| .560          | 2.924           | 2.978  | 3.015  | 3.082  | 3.135  | 3.187  | 3.239  | 3.291  | 3.343  | 3.395  | 3.447  |
| .580          | 3.013           | 3.067  | 3.120  | 3.173  | 3.226  | 3.279  | 3.332  | 3.385  | 3.420  | 3.490  | 3.543  |
| .600          | 3.105           | 3.159  | 3.213  | 3.267  | 3.320  | 3.374  | 3.427  | 3.481  | 3.535  | 3.588  | 3.642  |
| .620          | 3.200           | 3.254  | 3.309  | 3.363  | 3.418  | 3.472  | 3.526  | 3.581  | 3.635  | 3.689  | 3.743  |
| .640          | 3.297           | 3.353  | 3.408  | 3.463  | 3.518  | 3.574  | 3.629  | 3.684  | 3.739  | 3.794  | 3.849  |
| .660          | 3.397           | 3.455  | 3.511  | 3.567  | 3.623  | 3.679  | 3.735  | 3.791  | 3.847  | 3.903  | 3.958  |
| .680          | 3.505           | 3.562  | 3.619  | 3.676  | 3.732  | 3.789  | 3.846  | 3.903  | 3.959  | 4.016  | 4.072  |
| .700          | 3.616           | 3.673  | 3.731  | 3.789  | 3.847  | 3.904  | 3.962  | 4.020  | 4.077  | 4.134  | 4.192  |
| .720          | 3.732           | 3.791  | 3.850  | 3.909  | 3.967  | 4.026  | 4.084  | 4.142  | 4.201  | 4.259  | 4.317  |
| .740          | 3.856           | 3.916  | 3.975  | 4.035  | 4.094  | 4.154  | 4.213  | 4.272  | 4.331  | 4.390  | 4.449  |
| .760          | 3.987           | 4.048  | 4.108  | 4.169  | 4.229  | 4.290  | 4.350  | 4.410  | 4.470  | 4.530  | 4.590  |
| .780          | 4.128           | 4.189  | 4.251  | 4.301  | 4.371  | 4.435  | 4.496  | 4.557  | 4.618  | 4.679  | 4.740  |
| .800          | 4.279           | 4.342  | 4.404  | 4.467  | 4.529  | 4.592  | 4.654  | 4.716  | 4.778  | 4.840  | 4.902  |
| .820          | 4.444           | 4.508  | 4.571  | 4.635  | 4.698  | 4.762  | 4.825  | 4.888  | 4.951  | 5.014  | 5.077  |
| .840          | 4.625           | 4.690  | 4.755  | 4.814  | 4.884  | 4.949  | 5.013  | 5.078  | 5.142  | 5.206  | 5.270  |
| .860          | 4.827           | 4.893  | 4.959  | 5.026  | 5.091  | 5.157  | 5.223  | 5.288  | 5.354  | 5.419  | 5.484  |
| .880          | 5.056           | 5.124  | 5.191  | 5.259  | 5.326  | 5.393  | 5.460  | 5.527  | 5.594  | 5.661  | 5.727  |
| .900          | 5.322           | 5.392  | 5.461  | 5.530  | 5.599  | 5.667  | 5.736  | 5.804  | 5.872  | 5.941  | 6.009  |
| .920          | 5.642           | 5.713  | 5.784  | 5.855  | 5.925  | 5.996  | 6.066  | 6.136  | 6.206  | 6.276  | 6.346  |
| .940          | 6.045           | 6.118  | 6.191  | 6.264  | 6.337  | 6.410  | 6.482  | 6.554  | 6.626  | 6.698  | 6.770  |
| .950          | 6.296           | 6.370  | 6.445  | 6.519  | 6.593  | 6.667  | 6.741  | 6.814  | 6.888  | 6.960  | 7.034  |
| .960          | 6.599           | 6.675  | 6.751  | 6.827  | 6.902  | 6.978  | 7.053  | 7.128  | 7.203  | 7.277  | 7.352  |
| .970          | 6.984           | 7.062  | 7.140  | 7.217  | 7.295  | 7.372  | 7.449  | 7.526  | 7.602  | 7.678  | 7.755  |
| .980          | 7.517           | 7.597  | 7.678  | 7.758  | 7.837  | 7.917  | 7.996  | 8.075  | 8.154  | 8.233  | 8.311  |
| .990          | 8.406           | 8.490  | 8.575  | 8.658  | 8.742  | 8.825  | 8.908  | 8.991  | 9.073  | 9.156  | 9.238  |
| .995          | 9.274           | 9.362  | 9.449  | 9.536  | 9.623  | 9.710  | 9.796  | 9.882  | 9.968  | 10.054 | 10.139 |
| .999          | 11.229          | 11.324 | 11.418 | 11.512 | 11.606 | 11.699 | 11.792 | 11.885 | 11.977 | 12.069 | 12.161 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 3.50            | 3.55   | 3.60   | 3.65   | 3.70   | 3.75   | 3.80   | 3.85   | 3.90   | 3.95   | 4.00   |
| .001          | 0.299           | 0.311  | 0.324  | 0.336  | 0.349  | 0.361  | 0.375  | 0.388  | 0.401  | 0.415  | 0.429  |
| .005          | 0.495           | 0.512  | 0.529  | 0.546  | 0.563  | 0.581  | 0.599  | 0.617  | 0.635  | 0.654  | 0.672  |
| .010          | 0.620           | 0.639  | 0.659  | 0.679  | 0.699  | 0.719  | 0.740  | 0.760  | 0.781  | 0.802  | 0.823  |
| .020          | 0.782           | 0.805  | 0.828  | 0.851  | 0.874  | 0.897  | 0.921  | 0.944  | 0.968  | 0.992  | 1.016  |
| .030          | 0.901           | 0.925  | 0.950  | 0.975  | 1.001  | 1.026  | 1.051  | 1.077  | 1.103  | 1.129  | 1.155  |
| .040          | 0.999           | 1.025  | 1.051  | 1.078  | 1.105  | 1.131  | 1.159  | 1.186  | 1.213  | 1.241  | 1.268  |
| .050          | 1.084           | 1.111  | 1.139  | 1.167  | 1.195  | 1.223  | 1.251  | 1.280  | 1.309  | 1.337  | 1.366  |
| .060          | 1.160           | 1.189  | 1.218  | 1.247  | 1.276  | 1.305  | 1.335  | 1.364  | 1.394  | 1.424  | 1.454  |
| .080          | 1.296           | 1.327  | 1.357  | 1.388  | 1.419  | 1.451  | 1.482  | 1.513  | 1.545  | 1.577  | 1.609  |
| .100          | 1.417           | 1.449  | 1.481  | 1.514  | 1.546  | 1.579  | 1.612  | 1.645  | 1.678  | 1.711  | 1.745  |
| .120          | 1.527           | 1.560  | 1.594  | 1.628  | 1.662  | 1.696  | 1.731  | 1.765  | 1.799  | 1.834  | 1.869  |
| .140          | 1.630           | 1.665  | 1.700  | 1.735  | 1.770  | 1.806  | 1.841  | 1.877  | 1.912  | 1.948  | 1.984  |
| .160          | 1.727           | 1.763  | 1.800  | 1.836  | 1.872  | 1.909  | 1.945  | 1.982  | 2.019  | 2.056  | 2.093  |
| .180          | 1.821           | 1.858  | 1.895  | 1.933  | 1.970  | 2.008  | 2.045  | 2.083  | 2.121  | 2.159  | 2.197  |
| .200          | 1.911           | 1.949  | 1.988  | 2.026  | 2.064  | 2.103  | 2.142  | 2.180  | 2.219  | 2.258  | 2.297  |
| .220          | 1.999           | 2.038  | 2.077  | 2.117  | 2.156  | 2.195  | 2.235  | 2.275  | 2.314  | 2.354  | 2.394  |
| .240          | 2.085           | 2.125  | 2.165  | 2.205  | 2.246  | 2.286  | 2.326  | 2.367  | 2.407  | 2.448  | 2.489  |
| .260          | 2.170           | 2.210  | 2.251  | 2.292  | 2.334  | 2.375  | 2.416  | 2.457  | 2.499  | 2.540  | 2.582  |
| .280          | 2.253           | 2.295  | 2.337  | 2.378  | 2.420  | 2.462  | 2.504  | 2.546  | 2.589  | 2.631  | 2.673  |
| .300          | 2.336           | 2.378  | 2.421  | 2.464  | 2.506  | 2.549  | 2.592  | 2.635  | 2.678  | 2.721  | 2.764  |
| .320          | 2.418           | 2.461  | 2.505  | 2.548  | 2.592  | 2.635  | 2.679  | 2.722  | 2.766  | 2.810  | 2.854  |
| .340          | 2.500           | 2.544  | 2.588  | 2.632  | 2.677  | 2.721  | 2.765  | 2.810  | 2.854  | 2.898  | 2.943  |
| .360          | 2.582           | 2.627  | 2.672  | 2.717  | 2.762  | 2.807  | 2.852  | 2.897  | 2.942  | 2.987  | 3.032  |
| .380          | 2.664           | 2.710  | 2.755  | 2.801  | 2.847  | 2.892  | 2.938  | 2.984  | 3.030  | 3.076  | 3.122  |
| .400          | 2.747           | 2.793  | 2.839  | 2.886  | 2.932  | 2.979  | 3.025  | 3.072  | 3.118  | 3.165  | 3.211  |
| .420          | 2.830           | 2.877  | 2.924  | 2.971  | 3.018  | 3.065  | 3.113  | 3.160  | 3.207  | 3.254  | 3.302  |
| .440          | 2.914           | 2.962  | 3.009  | 3.057  | 3.105  | 3.153  | 3.201  | 3.249  | 3.297  | 3.345  | 3.392  |
| .460          | 2.999           | 3.047  | 3.096  | 3.144  | 3.193  | 3.242  | 3.290  | 3.339  | 3.387  | 3.436  | 3.484  |
| .480          | 3.085           | 3.134  | 3.184  | 3.233  | 3.282  | 3.331  | 3.381  | 3.430  | 3.479  | 3.528  | 3.578  |
| .500          | 3.173           | 3.223  | 3.273  | 3.323  | 3.373  | 3.422  | 3.472  | 3.522  | 3.572  | 3.622  | 3.672  |
| .520          | 3.258           | 3.313  | 3.363  | 3.414  | 3.465  | 3.515  | 3.566  | 3.616  | 3.667  | 3.715  | 3.768  |
| .540          | 3.354           | 3.405  | 3.456  | 3.507  | 3.559  | 3.610  | 3.661  | 3.713  | 3.764  | 3.815  | 3.866  |
| .560          | 3.447           | 3.499  | 3.551  | 3.603  | 3.655  | 3.698  | 3.759  | 3.811  | 3.863  | 3.915  | 3.967  |
| .580          | 3.543           | 3.596  | 3.644  | 3.701  | 3.754  | 3.806  | 3.859  | 3.912  | 3.964  | 4.017  | 4.070  |
| .600          | 3.642           | 3.695  | 3.749  | 3.802  | 3.855  | 3.904  | 3.962  | 4.015  | 4.069  | 4.122  | 4.175  |
| .620          | 3.743           | 3.798  | 3.849  | 3.906  | 3.960  | 4.014  | 4.068  | 4.122  | 4.176  | 4.230  | 4.284  |
| .640          | 3.849           | 3.904  | 3.959  | 4.014  | 4.068  | 4.123  | 4.178  | 4.233  | 4.288  | 4.342  | 4.397  |
| .660          | 3.958           | 4.014  | 4.070  | 4.125  | 4.181  | 4.236  | 4.292  | 4.342  | 4.403  | 4.458  | 4.514  |
| .680          | 4.072           | 4.129  | 4.185  | 4.242  | 4.298  | 4.354  | 4.411  | 4.467  | 4.523  | 4.579  | 4.635  |
| .700          | 4.192           | 4.244  | 4.306  | 4.363  | 4.421  | 4.478  | 4.535  | 4.592  | 4.649  | 4.705  | 4.762  |
| .720          | 4.317           | 4.375  | 4.433  | 4.491  | 4.549  | 4.607  | 4.665  | 4.723  | 4.780  | 4.832  | 4.896  |
| .740          | 4.449           | 4.508  | 4.567  | 4.626  | 4.685  | 4.741  | 4.802  | 4.861  | 4.919  | 4.978  | 5.036  |
| .760          | 4.590           | 4.650  | 4.710  | 4.769  | 4.829  | 4.888  | 4.948  | 5.007  | 5.067  | 5.126  | 5.185  |
| .780          | 4.740           | 4.801  | 4.861  | 4.922  | 4.983  | 5.043  | 5.103  | 5.164  | 5.224  | 5.284  | 5.344  |
| .800          | 4.902           | 4.963  | 5.025  | 5.087  | 5.148  | 5.209  | 5.271  | 5.332  | 5.393  | 5.454  | 5.515  |
| .820          | 5.077           | 5.140  | 5.203  | 5.265  | 5.328  | 5.390  | 5.452  | 5.514  | 5.576  | 5.639  | 5.672  |
| .840          | 5.270           | 5.334  | 5.397  | 5.461  | 5.525  | 5.588  | 5.651  | 5.715  | 5.778  | 5.841  | 5.904  |
| .860          | 5.484           | 5.549  | 5.614  | 5.679  | 5.744  | 5.808  | 5.873  | 5.937  | 6.001  | 6.066  | 6.130  |
| .880          | 5.727           | 5.793  | 5.860  | 5.926  | 5.992  | 6.058  | 6.123  | 6.189  | 6.252  | 6.320  | 6.385  |
| .900          | 6.009           | 6.076  | 6.144  | 6.212  | 6.279  | 6.346  | 6.413  | 6.480  | 6.547  | 6.614  | 6.681  |
| .920          | 6.346           | 6.415  | 6.484  | 6.554  | 6.623  | 6.692  | 6.760  | 6.829  | 6.898  | 6.966  | 7.034  |
| .940          | 6.770           | 6.841  | 6.913  | 6.984  | 7.055  | 7.126  | 7.197  | 7.267  | 7.338  | 7.408  | 7.478  |
| .950          | 7.034           | 7.106  | 7.179  | 7.251  | 7.324  | 7.396  | 7.467  | 7.539  | 7.611  | 7.682  | 7.754  |
| .960          | 7.352           | 7.426  | 7.500  | 7.573  | 7.647  | 7.721  | 7.794  | 7.867  | 7.940  | 8.013  | 8.085  |
| .970          | 7.755           | 7.830  | 7.906  | 7.982  | 8.057  | 8.132  | 8.207  | 8.282  | 8.357  | 8.431  | 8.505  |
| .980          | 8.311           | 8.389  | 8.467  | 8.545  | 8.623  | 8.700  | 8.777  | 8.854  | 8.931  | 9.008  | 9.084  |
| .990          | 9.238           | 9.319  | 9.401  | 9.482  | 9.563  | 9.644  | 9.725  | 9.805  | 9.885  | 9.965  | 10.045 |
| .995          | 10.139          | 10.224 | 10.309 | 10.393 | 10.477 | 10.561 | 10.645 | 10.728 | 10.812 | 10.895 | 10.977 |
| .999          | 12.161          | 12.252 | 12.344 | 12.434 | 12.525 | 12.615 | 12.705 | 12.795 | 12.884 | 12.973 | 13.062 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 4.00            | 4.05   | 4.10   | 4.15   | 4.20   | 4.25   | 4.30   | 4.35   | 4.40   | 4.45   | 4.50   |
| .001          | 0.429           | 0.443  | 0.457  | 0.471  | 0.485  | 0.500  | 0.515  | 0.530  | 0.545  | 0.560  | 0.576  |
| .005          | 0.672           | 0.691  | 0.710  | 0.729  | 0.748  | 0.768  | 0.787  | 0.807  | 0.827  | 0.847  | 0.867  |
| .010          | 0.823           | 0.845  | 0.866  | 0.888  | 0.910  | 0.932  | 0.954  | 0.976  | 0.999  | 1.021  | 1.044  |
| .020          | 1.016           | 1.041  | 1.065  | 1.090  | 1.114  | 1.139  | 1.164  | 1.190  | 1.215  | 1.241  | 1.266  |
| .030          | 1.155           | 1.181  | 1.208  | 1.234  | 1.261  | 1.288  | 1.315  | 1.342  | 1.369  | 1.397  | 1.424  |
| .040          | 1.268           | 1.296  | 1.324  | 1.352  | 1.380  | 1.409  | 1.437  | 1.466  | 1.495  | 1.523  | 1.552  |
| .050          | 1.366           | 1.395  | 1.425  | 1.454  | 1.483  | 1.513  | 1.543  | 1.572  | 1.602  | 1.632  | 1.663  |
| .060          | 1.454           | 1.484  | 1.514  | 1.545  | 1.575  | 1.606  | 1.637  | 1.667  | 1.698  | 1.730  | 1.761  |
| .080          | 1.609           | 1.641  | 1.673  | 1.705  | 1.737  | 1.769  | 1.802  | 1.835  | 1.867  | 1.900  | 1.933  |
| .100          | 1.745           | 1.778  | 1.812  | 1.845  | 1.879  | 1.913  | 1.947  | 1.981  | 2.015  | 2.050  | 2.084  |
| .120          | 1.869           | 1.904  | 1.938  | 1.973  | 2.008  | 2.044  | 2.079  | 2.114  | 2.150  | 2.185  | 2.221  |
| .140          | 1.984           | 2.020  | 2.056  | 2.092  | 2.128  | 2.165  | 2.201  | 2.238  | 2.274  | 2.311  | 2.348  |
| .160          | 2.093           | 2.130  | 2.167  | 2.204  | 2.242  | 2.279  | 2.316  | 2.354  | 2.392  | 2.429  | 2.467  |
| .180          | 2.197           | 2.235  | 2.273  | 2.311  | 2.349  | 2.388  | 2.426  | 2.465  | 2.503  | 2.542  | 2.581  |
| .200          | 2.297           | 2.336  | 2.375  | 2.408  | 2.453  | 2.493  | 2.532  | 2.571  | 2.611  | 2.650  | 2.690  |
| .220          | 2.394           | 2.434  | 2.474  | 2.514  | 2.554  | 2.594  | 2.634  | 2.675  | 2.715  | 2.742  | 2.796  |
| .240          | 2.489           | 2.529  | 2.570  | 2.611  | 2.652  | 2.693  | 2.734  | 2.775  | 2.816  | 2.857  | 2.899  |
| .260          | 2.582           | 2.623  | 2.665  | 2.706  | 2.748  | 2.790  | 2.832  | 2.874  | 2.916  | 2.958  | 3.000  |
| .280          | 2.673           | 2.715  | 2.758  | 2.800  | 2.843  | 2.885  | 2.928  | 2.971  | 3.013  | 3.056  | 3.099  |
| .300          | 2.764           | 2.807  | 2.850  | 2.893  | 2.936  | 2.980  | 3.023  | 3.066  | 3.110  | 3.153  | 3.197  |
| .320          | 2.854           | 2.897  | 2.941  | 2.985  | 3.029  | 3.073  | 3.117  | 3.161  | 3.205  | 3.249  | 3.294  |
| .340          | 2.943           | 2.988  | 3.032  | 3.077  | 3.121  | 3.166  | 3.211  | 3.256  | 3.300  | 3.345  | 3.390  |
| .360          | 3.032           | 3.078  | 3.123  | 3.168  | 3.213  | 3.259  | 3.304  | 3.350  | 3.395  | 3.441  | 3.486  |
| .380          | 3.122           | 3.168  | 3.214  | 3.260  | 3.306  | 3.352  | 3.398  | 3.444  | 3.490  | 3.536  | 3.582  |
| .400          | 3.211           | 3.258  | 3.305  | 3.351  | 3.398  | 3.445  | 3.491  | 3.538  | 3.585  | 3.632  | 3.679  |
| .420          | 3.302           | 3.349  | 3.396  | 3.443  | 3.491  | 3.538  | 3.586  | 3.633  | 3.680  | 3.728  | 3.775  |
| .440          | 3.392           | 3.440  | 3.488  | 3.536  | 3.584  | 3.632  | 3.680  | 3.728  | 3.777  | 3.825  | 3.873  |
| .460          | 3.484           | 3.533  | 3.582  | 3.630  | 3.679  | 3.728  | 3.776  | 3.825  | 3.874  | 3.922  | 3.971  |
| .480          | 3.578           | 3.627  | 3.676  | 3.725  | 3.775  | 3.824  | 3.873  | 3.913  | 3.972  | 4.021  | 4.071  |
| .500          | 3.672           | 3.722  | 3.772  | 3.822  | 3.872  | 3.922  | 3.972  | 4.022  | 4.072  | 4.111  | 4.171  |
| .520          | 3.768           | 3.819  | 3.869  | 3.920  | 3.971  | 4.021  | 4.072  | 4.117  | 4.173  | 4.223  | 4.274  |
| .540          | 3.866           | 3.918  | 3.969  | 4.020  | 4.071  | 4.123  | 4.174  | 4.225  | 4.275  | 4.327  | 4.379  |
| .560          | 3.967           | 4.019  | 4.071  | 4.122  | 4.174  | 4.226  | 4.278  | 4.330  | 4.382  | 4.428  | 4.485  |
| .580          | 4.070           | 4.122  | 4.175  | 4.227  | 4.280  | 4.332  | 4.385  | 4.437  | 4.487  | 4.542  | 4.595  |
| .600          | 4.175           | 4.229  | 4.282  | 4.335  | 4.388  | 4.441  | 4.493  | 4.548  | 4.601  | 4.653  | 4.707  |
| .620          | 4.284           | 4.338  | 4.392  | 4.444  | 4.500  | 4.554  | 4.607  | 4.638  | 4.715  | 4.763  | 4.810  |
| .640          | 4.397           | 4.451  | 4.506  | 4.561  | 4.615  | 4.670  | 4.724  | 4.779  | 4.833  | 4.887  | 4.942  |
| .660          | 4.514           | 4.569  | 4.624  | 4.680  | 4.735  | 4.790  | 4.845  | 4.900  | 4.955  | 5.010  | 5.040  |
| .680          | 4.635           | 4.691  | 4.747  | 4.803  | 4.859  | 4.915  | 4.971  | 5.025  | 5.083  | 5.113  | 5.194  |
| .700          | 4.762           | 4.819  | 4.876  | 4.932  | 4.989  | 5.046  | 5.102  | 5.159  | 5.215  | 5.272  | 5.328  |
| .720          | 4.896           | 4.953  | 5.011  | 5.068  | 5.125  | 5.183  | 5.240  | 5.297  | 5.328  | 5.412  | 5.469  |
| .740          | 5.036           | 5.094  | 5.153  | 5.211  | 5.269  | 5.301  | 5.385  | 5.443  | 5.500  | 5.559  | 5.617  |
| .760          | 5.185           | 5.244  | 5.303  | 5.362  | 5.421  | 5.480  | 5.539  | 5.598  | 5.657  | 5.715  | 5.774  |
| .780          | 5.344           | 5.404  | 5.464  | 5.524  | 5.584  | 5.644  | 5.703  | 5.763  | 5.822  | 5.882  | 5.941  |
| .800          | 5.515           | 5.576  | 5.637  | 5.698  | 5.758  | 5.804  | 5.876  | 5.940  | 6.000  | 6.061  | 6.106  |
| .820          | 5.672           | 5.762  | 5.824  | 5.886  | 5.947  | 6.009  | 6.071  | 6.132  | 6.193  | 6.255  | 6.316  |
| .840          | 5.904           | 5.967  | 6.029  | 6.092  | 6.155  | 6.217  | 6.280  | 6.311  | 6.405  | 6.467  | 6.529  |
| .860          | 6.130           | 6.194  | 6.258  | 6.321  | 6.385  | 6.449  | 6.512  | 6.576  | 6.639  | 6.669  | 6.766  |
| .880          | 6.385           | 6.450  | 6.515  | 6.572  | 6.645  | 6.710  | 6.775  | 6.840  | 6.904  | 6.969  | 7.033  |
| .900          | 6.681           | 6.747  | 6.814  | 6.880  | 6.946  | 7.013  | 7.079  | 7.145  | 7.210  | 7.276  | 7.342  |
| .920          | 7.034           | 7.102  | 7.170  | 7.238  | 7.306  | 7.374  | 7.441  | 7.509  | 7.576  | 7.643  | 7.711  |
| .940          | 7.478           | 7.548  | 7.618  | 7.688  | 7.758  | 7.826  | 7.896  | 7.966  | 8.035  | 8.104  | 8.173  |
| .950          | 7.754           | 7.825  | 7.896  | 7.967  | 8.038  | 8.108  | 8.179  | 8.249  | 8.319  | 8.389  | 8.459  |
| .960          | 8.085           | 8.158  | 8.230  | 8.302  | 8.364  | 8.446  | 8.518  | 8.590  | 8.661  | 8.733  | 8.804  |
| .970          | 8.505           | 8.579  | 8.653  | 8.727  | 8.801  | 8.874  | 8.948  | 9.021  | 9.094  | 9.167  | 9.240  |
| .980          | 9.084           | 9.160  | 9.236  | 9.312  | 9.388  | 9.464  | 9.539  | 9.615  | 9.690  | 9.765  | 9.840  |
| .990          | 10.045          | 10.125 | 10.204 | 10.283 | 10.362 | 10.441 | 10.520 | 10.598 | 10.677 | 10.755 | 10.833 |
| .995          | 10.977          | 11.060 | 11.142 | 11.225 | 11.307 | 11.388 | 11.470 | 11.552 | 11.633 | 11.714 | 11.795 |
| .999          | 13.062          | 13.151 | 13.239 | 13.327 | 13.416 | 13.503 | 13.591 | 13.678 | 13.765 | 13.852 | 13.939 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 4.50            | 4.55   | 4.60   | 4.65   | 4.70   | 4.75   | 4.80   | 4.85   | 4.90   | 4.95   | 5.00   |
| .001          | 0.576           | 0.592  | 0.607  | 0.623  | 0.640  | 0.656  | 0.672  | 0.689  | 0.706  | 0.722  | 0.739  |
| .005          | 0.867           | 0.888  | 0.908  | 0.929  | 0.950  | 0.971  | 0.992  | 1.013  | 1.035  | 1.056  | 1.078  |
| .010          | 1.044           | 1.067  | 1.090  | 1.113  | 1.136  | 1.160  | 1.183  | 1.207  | 1.231  | 1.255  | 1.279  |
| .020          | 1.266           | 1.292  | 1.318  | 1.344  | 1.370  | 1.396  | 1.423  | 1.449  | 1.476  | 1.503  | 1.530  |
| .030          | 1.424           | 1.452  | 1.480  | 1.508  | 1.536  | 1.564  | 1.592  | 1.620  | 1.649  | 1.677  | 1.706  |
| .040          | 1.552           | 1.581  | 1.611  | 1.640  | 1.669  | 1.699  | 1.729  | 1.758  | 1.788  | 1.818  | 1.848  |
| .050          | 1.663           | 1.693  | 1.723  | 1.754  | 1.784  | 1.815  | 1.846  | 1.877  | 1.908  | 1.939  | 1.970  |
| .060          | 1.761           | 1.792  | 1.823  | 1.855  | 1.887  | 1.918  | 1.950  | 1.982  | 2.014  | 2.046  | 2.078  |
| .080          | 1.933           | 1.966  | 1.999  | 2.032  | 2.066  | 2.099  | 2.133  | 2.166  | 2.200  | 2.234  | 2.268  |
| .100          | 2.084           | 2.119  | 2.153  | 2.188  | 2.222  | 2.257  | 2.292  | 2.327  | 2.362  | 2.397  | 2.433  |
| .120          | 2.221           | 2.257  | 2.292  | 2.328  | 2.364  | 2.400  | 2.436  | 2.473  | 2.509  | 2.545  | 2.582  |
| .140          | 2.348           | 2.385  | 2.422  | 2.459  | 2.496  | 2.533  | 2.570  | 2.607  | 2.645  | 2.682  | 2.719  |
| .160          | 2.467           | 2.505  | 2.543  | 2.581  | 2.619  | 2.657  | 2.695  | 2.734  | 2.772  | 2.810  | 2.849  |
| .180          | 2.581           | 2.620  | 2.658  | 2.697  | 2.736  | 2.775  | 2.815  | 2.854  | 2.893  | 2.932  | 2.972  |
| .200          | 2.690           | 2.730  | 2.769  | 2.809  | 2.849  | 2.889  | 2.929  | 2.969  | 3.009  | 3.049  | 3.090  |
| .220          | 2.796           | 2.836  | 2.877  | 2.918  | 2.958  | 2.999  | 3.040  | 3.081  | 3.121  | 3.162  | 3.203  |
| .240          | 2.899           | 2.940  | 2.981  | 3.023  | 3.064  | 3.106  | 3.147  | 3.189  | 3.231  | 3.272  | 3.314  |
| .260          | 3.000           | 3.042  | 3.084  | 3.126  | 3.168  | 3.210  | 3.253  | 3.295  | 3.338  | 3.380  | 3.422  |
| .280          | 3.099           | 3.142  | 3.184  | 3.227  | 3.270  | 3.313  | 3.356  | 3.399  | 3.442  | 3.486  | 3.529  |
| .300          | 3.197           | 3.240  | 3.284  | 3.327  | 3.371  | 3.415  | 3.458  | 3.502  | 3.546  | 3.590  | 3.634  |
| .320          | 3.294           | 3.338  | 3.382  | 3.426  | 3.471  | 3.515  | 3.559  | 3.604  | 3.648  | 3.693  | 3.737  |
| .340          | 3.390           | 3.435  | 3.480  | 3.525  | 3.570  | 3.615  | 3.660  | 3.705  | 3.750  | 3.795  | 3.840  |
| .360          | 3.486           | 3.532  | 3.577  | 3.623  | 3.669  | 3.714  | 3.760  | 3.806  | 3.851  | 3.897  | 3.943  |
| .380          | 3.582           | 3.628  | 3.670  | 3.721  | 3.767  | 3.813  | 3.860  | 3.906  | 3.952  | 3.999  | 4.045  |
| .400          | 3.679           | 3.725  | 3.767  | 3.819  | 3.866  | 3.913  | 3.959  | 4.007  | 4.054  | 4.101  | 4.148  |
| .420          | 3.775           | 3.823  | 3.870  | 3.918  | 3.965  | 4.013  | 4.060  | 4.108  | 4.155  | 4.203  | 4.248  |
| .440          | 3.873           | 3.921  | 3.949  | 4.017  | 4.065  | 4.113  | 4.161  | 4.204  | 4.258  | 4.306  | 4.354  |
| .460          | 3.971           | 4.000  | 4.068  | 4.117  | 4.166  | 4.215  | 4.263  | 4.312  | 4.361  | 4.410  | 4.458  |
| .480          | 4.071           | 4.120  | 4.164  | 4.219  | 4.257  | 4.317  | 4.367  | 4.416  | 4.465  | 4.515  | 4.564  |
| .500          | 4.171           | 4.221  | 4.271  | 4.321  | 4.371  | 4.421  | 4.471  | 4.510  | 4.571  | 4.621  | 4.671  |
| .520          | 4.274           | 4.325  | 4.375  | 4.426  | 4.476  | 4.527  | 4.577  | 4.628  | 4.678  | 4.729  | 4.779  |
| .540          | 4.379           | 4.430  | 4.481  | 4.532  | 4.583  | 4.634  | 4.685  | 4.737  | 4.788  | 4.839  | 4.890  |
| .560          | 4.485           | 4.537  | 4.589  | 4.641  | 4.692  | 4.738  | 4.796  | 4.823  | 4.899  | 4.951  | 5.003  |
| .580          | 4.595           | 4.647  | 4.699  | 4.752  | 4.804  | 4.857  | 4.909  | 4.961  | 5.014  | 5.066  | 5.118  |
| .600          | 4.707           | 4.748  | 4.813  | 4.866  | 4.919  | 4.972  | 5.025  | 5.078  | 5.131  | 5.184  | 5.237  |
| .620          | 4.810           | 4.876  | 4.930  | 4.977  | 5.037  | 5.091  | 5.144  | 5.198  | 5.251  | 5.305  | 5.358  |
| .640          | 4.942           | 4.971  | 5.050  | 5.105  | 5.159  | 5.213  | 5.267  | 5.322  | 5.376  | 5.430  | 5.484  |
| .660          | 5.040           | 5.120  | 5.175  | 5.230  | 5.285  | 5.340  | 5.395  | 5.450  | 5.504  | 5.559  | 5.614  |
| .680          | 5.194           | 5.250  | 5.305  | 5.361  | 5.417  | 5.472  | 5.528  | 5.583  | 5.639  | 5.694  | 5.749  |
| .700          | 5.328           | 5.385  | 5.441  | 5.497  | 5.553  | 5.610  | 5.666  | 5.721  | 5.778  | 5.834  | 5.890  |
| .720          | 5.469           | 5.526  | 5.583  | 5.640  | 5.697  | 5.754  | 5.811  | 5.868  | 5.924  | 5.981  | 6.038  |
| .740          | 5.617           | 5.675  | 5.733  | 5.790  | 5.848  | 5.906  | 5.963  | 6.021  | 6.078  | 6.136  | 6.193  |
| .760          | 5.774           | 5.833  | 5.891  | 5.950  | 6.008  | 6.067  | 6.125  | 6.183  | 6.241  | 6.300  | 6.358  |
| .780          | 5.941           | 6.001  | 6.060  | 6.119  | 6.179  | 6.238  | 6.297  | 6.356  | 6.383  | 6.474  | 6.533  |
| .800          | 6.106           | 6.181  | 6.242  | 6.302  | 6.362  | 6.422  | 6.482  | 6.542  | 6.601  | 6.661  | 6.721  |
| .820          | 6.316           | 6.377  | 6.438  | 6.499  | 6.560  | 6.621  | 6.682  | 6.742  | 6.803  | 6.864  | 6.924  |
| .840          | 6.529           | 6.591  | 6.653  | 6.715  | 6.777  | 6.839  | 6.901  | 6.962  | 7.024  | 7.067  | 7.147  |
| .860          | 6.766           | 6.829  | 6.892  | 6.955  | 7.018  | 7.081  | 7.143  | 7.206  | 7.269  | 7.331  | 7.394  |
| .880          | 7.033           | 7.097  | 7.161  | 7.226  | 7.290  | 7.354  | 7.417  | 7.481  | 7.545  | 7.609  | 7.672  |
| .900          | 7.342           | 7.407  | 7.473  | 7.538  | 7.604  | 7.669  | 7.734  | 7.799  | 7.861  | 7.929  | 7.994  |
| .920          | 7.711           | 7.778  | 7.845  | 7.911  | 7.978  | 8.045  | 8.111  | 8.178  | 8.244  | 8.311  | 8.377  |
| .940          | 8.173           | 8.242  | 8.311  | 8.379  | 8.448  | 8.516  | 8.584  | 8.653  | 8.721  | 8.789  | 8.857  |
| .950          | 8.459           | 8.529  | 8.599  | 8.669  | 8.738  | 8.808  | 8.877  | 8.946  | 9.016  | 9.085  | 9.154  |
| .960          | 8.804           | 8.875  | 8.946  | 9.017  | 9.088  | 9.159  | 9.229  | 9.300  | 9.368  | 9.440  | 9.510  |
| .970          | 9.240           | 9.312  | 9.385  | 9.457  | 9.530  | 9.602  | 9.674  | 9.746  | 9.818  | 9.889  | 9.961  |
| .980          | 9.840           | 9.914  | 9.989  | 10.063 | 10.137 | 10.212 | 10.286 | 10.359 | 10.433 | 10.507 | 10.580 |
| .990          | 10.833          | 10.911 | 10.989 | 11.066 | 11.143 | 11.221 | 11.298 | 11.375 | 11.451 | 11.528 | 11.605 |
| .995          | 11.795          | 11.875 | 11.956 | 12.036 | 12.116 | 12.196 | 12.276 | 12.356 | 12.436 | 12.515 | 12.594 |
| .999          | 13.939          | 14.025 | 14.111 | 14.197 | 14.283 | 14.369 | 14.454 | 14.539 | 14.625 | 14.709 | 14.794 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 5.00            | 5.10   | 5.20   | 5.30   | 5.40   | 5.50   | 5.60   | 5.70   | 5.80   | 5.90   | 6.00   |
| .001          | 0.739           | 0.774  | 0.809  | 0.844  | 0.880  | 0.917  | 0.954  | 0.992  | 1.030  | 1.068  | 1.107  |
| .005          | 1.078           | 1.122  | 1.166  | 1.211  | 1.256  | 1.302  | 1.348  | 1.394  | 1.441  | 1.489  | 1.537  |
| .010          | 1.279           | 1.328  | 1.377  | 1.426  | 1.476  | 1.527  | 1.578  | 1.629  | 1.681  | 1.733  | 1.785  |
| .020          | 1.530           | 1.584  | 1.638  | 1.693  | 1.749  | 1.804  | 1.861  | 1.917  | 1.974  | 2.031  | 2.089  |
| .030          | 1.706           | 1.764  | 1.822  | 1.880  | 1.939  | 1.999  | 2.058  | 2.118  | 2.179  | 2.239  | 2.300  |
| .040          | 1.848           | 1.909  | 1.970  | 2.031  | 2.092  | 2.154  | 2.217  | 2.279  | 2.342  | 2.406  | 2.469  |
| .050          | 1.970           | 2.033  | 2.096  | 2.159  | 2.223  | 2.287  | 2.352  | 2.417  | 2.482  | 2.547  | 2.613  |
| .060          | 2.078           | 2.143  | 2.208  | 2.273  | 2.339  | 2.405  | 2.472  | 2.538  | 2.605  | 2.672  | 2.740  |
| .080          | 2.268           | 2.335  | 2.404  | 2.472  | 2.541  | 2.610  | 2.680  | 2.750  | 2.820  | 2.890  | 2.961  |
| .100          | 2.433           | 2.503  | 2.574  | 2.646  | 2.717  | 2.789  | 2.861  | 2.933  | 3.006  | 3.079  | 3.152  |
| .120          | 2.582           | 2.655  | 2.728  | 2.802  | 2.876  | 2.950  | 3.024  | 3.099  | 3.173  | 3.248  | 3.324  |
| .140          | 2.719           | 2.795  | 2.870  | 2.946  | 3.022  | 3.098  | 3.174  | 3.251  | 3.328  | 3.405  | 3.482  |
| .160          | 2.849           | 2.926  | 3.003  | 3.081  | 3.159  | 3.237  | 3.315  | 3.393  | 3.472  | 3.551  | 3.630  |
| .180          | 2.972           | 3.051  | 3.130  | 3.209  | 3.289  | 3.368  | 3.448  | 3.528  | 3.609  | 3.689  | 3.770  |
| .200          | 3.090           | 3.170  | 3.251  | 3.332  | 3.413  | 3.494  | 3.576  | 3.658  | 3.739  | 3.821  | 3.904  |
| .220          | 3.203           | 3.286  | 3.368  | 3.450  | 3.533  | 3.616  | 3.699  | 3.782  | 3.866  | 3.949  | 4.033  |
| .240          | 3.314           | 3.398  | 3.482  | 3.566  | 3.650  | 3.734  | 3.819  | 3.903  | 3.988  | 4.073  | 4.158  |
| .260          | 3.422           | 3.508  | 3.593  | 3.678  | 3.764  | 3.849  | 3.935  | 4.021  | 4.107  | 4.194  | 4.280  |
| .280          | 3.529           | 3.615  | 3.702  | 3.789  | 3.876  | 3.963  | 4.050  | 4.137  | 4.224  | 4.312  | 4.399  |
| .300          | 3.634           | 3.721  | 3.809  | 3.897  | 3.986  | 4.074  | 4.162  | 4.251  | 4.340  | 4.428  | 4.517  |
| .320          | 3.737           | 3.817  | 3.916  | 4.005  | 4.094  | 4.184  | 4.263  | 4.363  | 4.453  | 4.543  | 4.633  |
| .340          | 3.840           | 3.931  | 4.021  | 4.112  | 4.202  | 4.293  | 4.384  | 4.475  | 4.566  | 4.657  | 4.748  |
| .360          | 3.943           | 4.034  | 4.126  | 4.207  | 4.310  | 4.402  | 4.494  | 4.586  | 4.678  | 4.771  | 4.863  |
| .380          | 4.045           | 4.138  | 4.231  | 4.324  | 4.417  | 4.510  | 4.603  | 4.697  | 4.784  | 4.884  | 4.977  |
| .400          | 4.148           | 4.242  | 4.336  | 4.430  | 4.524  | 4.619  | 4.713  | 4.807  | 4.902  | 4.996  | 5.091  |
| .420          | 4.248           | 4.346  | 4.441  | 4.536  | 4.632  | 4.727  | 4.823  | 4.918  | 5.014  | 5.110  | 5.205  |
| .440          | 4.354           | 4.451  | 4.547  | 4.643  | 4.740  | 4.837  | 4.933  | 5.030  | 5.127  | 5.223  | 5.320  |
| .460          | 4.458           | 4.556  | 4.654  | 4.739  | 4.849  | 4.947  | 5.044  | 5.142  | 5.240  | 5.338  | 5.436  |
| .480          | 4.564           | 4.663  | 4.762  | 4.860  | 4.959  | 5.058  | 5.157  | 5.256  | 5.354  | 5.452  | 5.552  |
| .500          | 4.671           | 4.771  | 4.871  | 4.971  | 5.071  | 5.170  | 5.270  | 5.357  | 5.470  | 5.570  | 5.670  |
| .520          | 4.779           | 4.881  | 4.982  | 5.083  | 5.184  | 5.271  | 5.359  | 5.473  | 5.581  | 5.689  | 5.790  |
| .540          | 4.890           | 4.992  | 5.093  | 5.195  | 5.292  | 5.401  | 5.503  | 5.605  | 5.707  | 5.809  | 5.911  |
| .560          | 5.003           | 5.106  | 5.210  | 5.313  | 5.416  | 5.520  | 5.623  | 5.726  | 5.829  | 5.932  | 6.035  |
| .580          | 5.118           | 5.223  | 5.327  | 5.432  | 5.536  | 5.641  | 5.745  | 5.849  | 5.954  | 6.058  | 6.162  |
| .600          | 5.237           | 5.342  | 5.448  | 5.554  | 5.659  | 5.765  | 5.870  | 5.976  | 6.074  | 6.187  | 6.292  |
| .620          | 5.358           | 5.465  | 5.572  | 5.678  | 5.786  | 5.893  | 5.999  | 6.106  | 6.212  | 6.315  | 6.393  |
| .640          | 5.484           | 5.592  | 5.700  | 5.808  | 5.916  | 6.024  | 6.132  | 6.240  | 6.347  | 6.455  | 6.563  |
| .660          | 5.614           | 5.716  | 5.833  | 5.942  | 6.051  | 6.160  | 6.270  | 6.378  | 6.455  | 6.596  | 6.705  |
| .680          | 5.749           | 5.860  | 5.971  | 6.081  | 6.192  | 6.302  | 6.412  | 6.522  | 6.632  | 6.742  | 6.835  |
| .700          | 5.890           | 6.002  | 6.114  | 6.226  | 6.334  | 6.448  | 6.561  | 6.672  | 6.783  | 6.895  | 7.006  |
| .720          | 6.038           | 6.151  | 6.265  | 6.378  | 6.491  | 6.604  | 6.716  | 6.829  | 6.941  | 7.054  | 7.166  |
| .740          | 6.193           | 6.308  | 6.423  | 6.537  | 6.652  | 6.766  | 6.880  | 6.994  | 7.108  | 7.221  | 7.335  |
| .760          | 6.358           | 6.474  | 6.590  | 6.706  | 6.822  | 6.937  | 7.053  | 7.168  | 7.283  | 7.398  | 7.513  |
| .780          | 6.533           | 6.651  | 6.768  | 6.886  | 7.003  | 7.120  | 7.237  | 7.354  | 7.470  | 7.587  | 7.703  |
| .800          | 6.721           | 6.840  | 6.959  | 7.078  | 7.197  | 7.316  | 7.434  | 7.533  | 7.670  | 7.788  | 7.906  |
| .820          | 6.924           | 7.045  | 7.166  | 7.287  | 7.407  | 7.527  | 7.647  | 7.767  | 7.887  | 8.006  | 8.126  |
| .840          | 7.147           | 7.270  | 7.392  | 7.515  | 7.637  | 7.759  | 7.881  | 8.002  | 8.123  | 8.245  | 8.365  |
| .860          | 7.394           | 7.519  | 7.643  | 7.767  | 7.891  | 8.015  | 8.139  | 8.262  | 8.385  | 8.508  | 8.631  |
| .880          | 7.672           | 7.799  | 7.926  | 8.052  | 8.178  | 8.304  | 8.430  | 8.555  | 8.680  | 8.805  | 8.930  |
| .900          | 7.994           | 8.123  | 8.252  | 8.381  | 8.509  | 8.638  | 8.765  | 8.893  | 9.021  | 9.148  | 9.275  |
| .920          | 8.377           | 8.509  | 8.641  | 8.772  | 8.903  | 9.034  | 9.165  | 9.295  | 9.425  | 9.555  | 9.685  |
| .940          | 8.857           | 8.992  | 9.127  | 9.262  | 9.397  | 9.531  | 9.665  | 9.798  | 9.931  | 10.061 | 10.197 |
| .950          | 9.154           | 9.291  | 9.428  | 9.565  | 9.701  | 9.838  | 9.973  | 10.109 | 10.244 | 10.372 | 10.513 |
| .960          | 9.510           | 9.650  | 9.790  | 9.929  | 10.068 | 10.206 | 10.344 | 10.478 | 10.619 | 10.756 | 10.893 |
| .970          | 9.961           | 10.104 | 10.246 | 10.388 | 10.530 | 10.671 | 10.812 | 10.952 | 11.092 | 11.232 | 11.371 |
| .980          | 10.580          | 10.727 | 10.873 | 11.019 | 11.164 | 11.309 | 11.453 | 11.597 | 11.741 | 11.884 | 12.027 |
| .990          | 11.605          | 11.757 | 11.909 | 12.061 | 12.212 | 12.362 | 12.513 | 12.662 | 12.811 | 12.960 | 13.108 |
| .995          | 12.594          | 12.752 | 12.910 | 13.066 | 13.223 | 13.378 | 13.534 | 13.688 | 13.843 | 13.996 | 14.150 |
| .999          | 14.794          | 14.963 | 15.131 | 15.299 | 15.466 | 15.632 | 15.798 | 15.963 | 16.127 | 16.291 | 16.455 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 6.00            | 6.10   | 6.20   | 6.30   | 6.40   | 6.50   | 6.60   | 6.70   | 6.80   | 6.90   | 7.00   |
| .001          | 1.107           | 1.147  | 1.186  | 1.227  | 1.267  | 1.309  | 1.350  | 1.392  | 1.434  | 1.477  | 1.520  |
| .005          | 1.537           | 1.585  | 1.634  | 1.683  | 1.733  | 1.783  | 1.833  | 1.883  | 1.934  | 1.986  | 2.037  |
| .010          | 1.785           | 1.838  | 1.891  | 1.945  | 1.999  | 2.053  | 2.108  | 2.163  | 2.219  | 2.274  | 2.330  |
| .020          | 2.089           | 2.147  | 2.206  | 2.264  | 2.323  | 2.383  | 2.442  | 2.502  | 2.563  | 2.623  | 2.684  |
| .030          | 2.300           | 2.362  | 2.424  | 2.486  | 2.548  | 2.611  | 2.673  | 2.737  | 2.800  | 2.864  | 2.928  |
| .040          | 2.469           | 2.533  | 2.597  | 2.662  | 2.727  | 2.792  | 2.857  | 2.923  | 2.989  | 3.055  | 3.121  |
| .050          | 2.613           | 2.679  | 2.745  | 2.812  | 2.879  | 2.946  | 3.013  | 3.081  | 3.149  | 3.217  | 3.285  |
| .060          | 2.740           | 2.808  | 2.876  | 2.944  | 3.013  | 3.082  | 3.151  | 3.220  | 3.290  | 3.360  | 3.430  |
| .080          | 2.961           | 3.031  | 3.103  | 3.174  | 3.245  | 3.317  | 3.389  | 3.461  | 3.534  | 3.606  | 3.679  |
| .100          | 3.152           | 3.225  | 3.299  | 3.373  | 3.447  | 3.521  | 3.595  | 3.670  | 3.745  | 3.820  | 3.895  |
| .120          | 3.324           | 3.399  | 3.475  | 3.551  | 3.627  | 3.703  | 3.780  | 3.856  | 3.933  | 4.010  | 4.088  |
| .140          | 3.482           | 3.559  | 3.637  | 3.715  | 3.793  | 3.871  | 3.949  | 4.028  | 4.107  | 4.185  | 4.264  |
| .160          | 3.630           | 3.709  | 3.788  | 3.868  | 3.948  | 4.027  | 4.108  | 4.188  | 4.268  | 4.349  | 4.407  |
| .180          | 3.770           | 3.851  | 3.932  | 4.013  | 4.094  | 4.176  | 4.257  | 4.339  | 4.421  | 4.503  | 4.585  |
| .200          | 3.904           | 3.986  | 4.069  | 4.151  | 4.234  | 4.317  | 4.400  | 4.483  | 4.567  | 4.650  | 4.734  |
| .220          | 4.033           | 4.116  | 4.200  | 4.284  | 4.369  | 4.453  | 4.537  | 4.622  | 4.707  | 4.792  | 4.877  |
| .240          | 4.158           | 4.243  | 4.328  | 4.414  | 4.499  | 4.585  | 4.671  | 4.757  | 4.843  | 4.929  | 5.015  |
| .260          | 4.280           | 4.366  | 4.453  | 4.540  | 4.626  | 4.713  | 4.800  | 4.888  | 4.975  | 5.062  | 5.146  |
| .280          | 4.399           | 4.487  | 4.575  | 4.663  | 4.751  | 4.839  | 4.927  | 5.016  | 5.104  | 5.193  | 5.281  |
| .300          | 4.517           | 4.606  | 4.695  | 4.784  | 4.874  | 4.963  | 5.052  | 5.142  | 5.231  | 5.321  | 5.411  |
| .320          | 4.633           | 4.723  | 4.814  | 4.904  | 4.994  | 5.085  | 5.175  | 5.266  | 5.357  | 5.448  | 5.538  |
| .340          | 4.748           | 4.840  | 4.931  | 5.023  | 5.114  | 5.206  | 5.297  | 5.389  | 5.481  | 5.573  | 5.665  |
| .360          | 4.863           | 4.955  | 5.048  | 5.140  | 5.233  | 5.326  | 5.418  | 5.511  | 5.604  | 5.697  | 5.790  |
| .380          | 4.977           | 5.071  | 5.164  | 5.258  | 5.351  | 5.445  | 5.539  | 5.633  | 5.727  | 5.821  | 5.915  |
| .400          | 5.091           | 5.186  | 5.280  | 5.375  | 5.470  | 5.565  | 5.659  | 5.754  | 5.849  | 5.944  | 6.039  |
| .420          | 5.205           | 5.301  | 5.397  | 5.492  | 5.588  | 5.684  | 5.780  | 5.876  | 5.972  | 6.068  | 6.164  |
| .440          | 5.320           | 5.417  | 5.514  | 5.610  | 5.707  | 5.804  | 5.901  | 5.998  | 6.095  | 6.190  | 6.289  |
| .460          | 5.436           | 5.533  | 5.631  | 5.729  | 5.827  | 5.925  | 6.023  | 6.121  | 6.219  | 6.317  | 6.413  |
| .480          | 5.552           | 5.651  | 5.750  | 5.849  | 5.948  | 6.039  | 6.146  | 6.245  | 6.344  | 6.443  | 6.541  |
| .500          | 5.670           | 5.770  | 5.870  | 5.970  | 6.070  | 6.170  | 6.270  | 6.370  | 6.462  | 6.570  | 6.670  |
| .520          | 5.790           | 5.891  | 5.984  | 6.093  | 6.194  | 6.295  | 6.396  | 6.497  | 6.598  | 6.699  | 6.791  |
| .540          | 5.911           | 6.014  | 6.108  | 6.218  | 6.320  | 6.422  | 6.524  | 6.624  | 6.727  | 6.829  | 6.931  |
| .560          | 6.035           | 6.139  | 6.242  | 6.345  | 6.444  | 6.551  | 6.654  | 6.757  | 6.860  | 6.963  | 7.065  |
| .580          | 6.162           | 6.266  | 6.370  | 6.475  | 6.579  | 6.683  | 6.787  | 6.891  | 6.995  | 7.099  | 7.193  |
| .600          | 6.292           | 6.397  | 6.502  | 6.608  | 6.713  | 6.818  | 6.923  | 7.028  | 7.133  | 7.238  | 7.343  |
| .620          | 6.393           | 6.532  | 6.630  | 6.744  | 6.850  | 6.956  | 7.063  | 7.169  | 7.275  | 7.381  | 7.487  |
| .640          | 6.563           | 6.637  | 6.778  | 6.876  | 6.992  | 7.099  | 7.207  | 7.314  | 7.421  | 7.528  | 7.635  |
| .660          | 6.705           | 6.813  | 6.922  | 7.030  | 7.139  | 7.247  | 7.355  | 7.463  | 7.572  | 7.680  | 7.788  |
| .680          | 6.835           | 6.962  | 7.071  | 7.181  | 7.291  | 7.400  | 7.507  | 7.619  | 7.708  | 7.837  | 7.946  |
| .700          | 7.006           | 7.116  | 7.227  | 7.338  | 7.449  | 7.559  | 7.670  | 7.780  | 7.891  | 8.001  | 8.111  |
| .720          | 7.166           | 7.278  | 7.390  | 7.502  | 7.614  | 7.687  | 7.838  | 7.949  | 8.061  | 8.172  | 8.283  |
| .740          | 7.335           | 7.448  | 7.562  | 7.675  | 7.788  | 7.901  | 8.014  | 8.127  | 8.239  | 8.352  | 8.464  |
| .760          | 7.513           | 7.628  | 7.743  | 7.857  | 7.971  | 8.086  | 8.200  | 8.314  | 8.428  | 8.542  | 8.655  |
| .780          | 7.703           | 7.819  | 7.935  | 8.051  | 8.167  | 8.282  | 8.398  | 8.513  | 8.628  | 8.743  | 8.858  |
| .800          | 7.906           | 8.024  | 8.141  | 8.258  | 8.375  | 8.492  | 8.609  | 8.723  | 8.843  | 8.959  | 9.075  |
| .820          | 8.126           | 8.245  | 8.364  | 8.482  | 8.601  | 8.720  | 8.838  | 8.956  | 9.074  | 9.192  | 9.310  |
| .840          | 8.365           | 8.486  | 8.596  | 8.684  | 8.847  | 8.968  | 9.087  | 9.207  | 9.327  | 9.446  | 9.566  |
| .860          | 8.631           | 8.754  | 8.876  | 8.998  | 9.120  | 9.242  | 9.363  | 9.485  | 9.606  | 9.727  | 9.848  |
| .880          | 8.930           | 9.055  | 9.179  | 9.303  | 9.427  | 9.551  | 9.674  | 9.797  | 9.921  | 10.044 | 10.166 |
| .900          | 9.275           | 9.401  | 9.528  | 9.654  | 9.780  | 9.906  | 10.031 | 10.157 | 10.282 | 10.407 | 10.532 |
| .920          | 9.685           | 9.814  | 9.943  | 10.072 | 10.200 | 10.328 | 10.456 | 10.584 | 10.712 | 10.839 | 10.966 |
| .940          | 10.197          | 10.322 | 10.461 | 10.593 | 10.724 | 10.856 | 10.987 | 11.117 | 11.248 | 11.378 | 11.508 |
| .950          | 10.513          | 10.647 | 10.781 | 10.915 | 11.048 | 11.181 | 11.314 | 11.446 | 11.579 | 11.711 | 11.842 |
| .960          | 10.893          | 11.029 | 11.165 | 11.301 | 11.436 | 11.571 | 11.706 | 11.841 | 11.975 | 12.109 | 12.243 |
| .970          | 11.371          | 11.510 | 11.648 | 11.787 | 11.925 | 12.062 | 12.200 | 12.337 | 12.474 | 12.610 | 12.747 |
| .980          | 12.027          | 12.169 | 12.312 | 12.453 | 12.595 | 12.736 | 12.877 | 13.017 | 13.157 | 13.297 | 13.436 |
| .990          | 13.108          | 13.256 | 13.404 | 13.551 | 13.698 | 13.844 | 13.990 | 14.136 | 14.281 | 14.426 | 14.571 |
| .995          | 14.150          | 14.303 | 14.455 | 14.607 | 14.759 | 14.910 | 15.060 | 15.211 | 15.361 | 15.510 | 15.660 |
| .999          | 16.455          | 16.618 | 16.780 | 16.942 | 17.103 | 17.264 | 17.425 | 17.585 | 17.744 | 17.903 | 18.062 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 7.00            | 7.10   | 7.20   | 7.30   | 7.40   | 7.50   | 7.60   | 7.70   | 7.80   | 7.90   | 8.00   |
| .001          | 1.520           | 1.564  | 1.608  | 1.652  | 1.696  | 1.741  | 1.787  | 1.832  | 1.878  | 1.924  | 1.971  |
| .005          | 2.037           | 2.089  | 2.142  | 2.194  | 2.247  | 2.300  | 2.354  | 2.408  | 2.462  | 2.516  | 2.571  |
| .010          | 2.330           | 2.387  | 2.443  | 2.500  | 2.557  | 2.615  | 2.672  | 2.730  | 2.789  | 2.847  | 2.906  |
| .020          | 2.684           | 2.745  | 2.807  | 2.868  | 2.930  | 2.992  | 3.055  | 3.118  | 3.181  | 3.244  | 3.307  |
| .030          | 2.928           | 2.992  | 3.057  | 3.121  | 3.186  | 3.252  | 3.317  | 3.383  | 3.449  | 3.515  | 3.581  |
| .040          | 3.121           | 3.188  | 3.255  | 3.322  | 3.389  | 3.457  | 3.525  | 3.593  | 3.661  | 3.729  | 3.798  |
| .050          | 3.285           | 3.354  | 3.423  | 3.492  | 3.561  | 3.630  | 3.700  | 3.770  | 3.840  | 3.910  | 3.981  |
| .060          | 3.430           | 3.500  | 3.570  | 3.641  | 3.712  | 3.783  | 3.854  | 3.926  | 3.997  | 4.069  | 4.141  |
| .080          | 3.679           | 3.752  | 3.826  | 3.899  | 3.973  | 4.046  | 4.120  | 4.195  | 4.269  | 4.343  | 4.418  |
| .100          | 3.895           | 3.970  | 4.046  | 4.121  | 4.197  | 4.273  | 4.350  | 4.426  | 4.503  | 4.579  | 4.656  |
| .120          | 4.088           | 4.165  | 4.243  | 4.320  | 4.398  | 4.476  | 4.554  | 4.633  | 4.711  | 4.790  | 4.868  |
| .140          | 4.264           | 4.344  | 4.423  | 4.502  | 4.582  | 4.662  | 4.742  | 4.822  | 4.902  | 4.982  | 5.063  |
| .160          | 4.407           | 4.510  | 4.591  | 4.672  | 4.753  | 4.835  | 4.916  | 4.998  | 5.080  | 5.161  | 5.243  |
| .180          | 4.585           | 4.667  | 4.750  | 4.832  | 4.915  | 4.998  | 5.081  | 5.164  | 5.247  | 5.330  | 5.414  |
| .200          | 4.734           | 4.817  | 4.901  | 4.985  | 5.069  | 5.153  | 5.238  | 5.322  | 5.407  | 5.491  | 5.569  |
| .220          | 4.877           | 4.962  | 5.047  | 5.132  | 5.217  | 5.303  | 5.389  | 5.474  | 5.560  | 5.646  | 5.732  |
| .240          | 5.015           | 5.101  | 5.188  | 5.274  | 5.361  | 5.448  | 5.534  | 5.621  | 5.708  | 5.795  | 5.882  |
| .260          | 5.146           | 5.237  | 5.325  | 5.412  | 5.500  | 5.588  | 5.676  | 5.764  | 5.852  | 5.941  | 6.029  |
| .280          | 5.281           | 5.370  | 5.459  | 5.548  | 5.637  | 5.726  | 5.815  | 5.904  | 5.993  | 6.082  | 6.172  |
| .300          | 5.411           | 5.501  | 5.590  | 5.680  | 5.770  | 5.861  | 5.951  | 6.041  | 6.131  | 6.222  | 6.312  |
| .320          | 5.538           | 5.629  | 5.720  | 5.811  | 5.902  | 5.994  | 6.085  | 6.176  | 6.264  | 6.359  | 6.450  |
| .340          | 5.665           | 5.757  | 5.849  | 5.941  | 6.033  | 6.125  | 6.217  | 6.310  | 6.402  | 6.494  | 6.554  |
| .360          | 5.790           | 5.883  | 5.976  | 6.069  | 6.162  | 6.256  | 6.349  | 6.442  | 6.536  | 6.629  | 6.722  |
| .380          | 5.915           | 6.009  | 6.103  | 6.197  | 6.291  | 6.385  | 6.480  | 6.574  | 6.635  | 6.763  | 6.857  |
| .400          | 6.039           | 6.134  | 6.229  | 6.325  | 6.420  | 6.515  | 6.608  | 6.705  | 6.801  | 6.896  | 6.983  |
| .420          | 6.164           | 6.252  | 6.356  | 6.452  | 6.548  | 6.644  | 6.741  | 6.837  | 6.931  | 7.029  | 7.126  |
| .440          | 6.289           | 6.382  | 6.483  | 6.580  | 6.677  | 6.774  | 6.871  | 6.969  | 7.066  | 7.163  | 7.260  |
| .460          | 6.413           | 6.513  | 6.611  | 6.709  | 6.807  | 6.905  | 7.003  | 7.101  | 7.163  | 7.297  | 7.395  |
| .480          | 6.541           | 6.640  | 6.739  | 6.838  | 6.937  | 7.001  | 7.136  | 7.235  | 7.334  | 7.433  | 7.532  |
| .500          | 6.670           | 6.770  | 6.870  | 6.970  | 7.065  | 7.134  | 7.269  | 7.369  | 7.469  | 7.569  | 7.660  |
| .520          | 6.791           | 6.900  | 7.001  | 7.102  | 7.203  | 7.304  | 7.405  | 7.506  | 7.607  | 7.708  | 7.808  |
| .540          | 6.931           | 7.033  | 7.135  | 7.236  | 7.339  | 7.441  | 7.542  | 7.644  | 7.707  | 7.848  | 7.950  |
| .560          | 7.065           | 7.168  | 7.271  | 7.374  | 7.477  | 7.580  | 7.682  | 7.785  | 7.888  | 7.971  | 8.093  |
| .580          | 7.193           | 7.306  | 7.410  | 7.514  | 7.618  | 7.722  | 7.825  | 7.929  | 8.033  | 8.136  | 8.235  |
| .600          | 7.343           | 7.448  | 7.552  | 7.657  | 7.762  | 7.867  | 7.971  | 8.071  | 8.181  | 8.285  | 8.390  |
| .620          | 7.487           | 7.592  | 7.698  | 7.804  | 7.910  | 8.015  | 8.121  | 8.227  | 8.332  | 8.438  | 8.543  |
| .640          | 7.635           | 7.742  | 7.848  | 7.955  | 8.062  | 8.166  | 8.275  | 8.382  | 8.486  | 8.595  | 8.701  |
| .660          | 7.788           | 7.896  | 8.003  | 8.111  | 8.178  | 8.327  | 8.434  | 8.542  | 8.639  | 8.757  | 8.865  |
| .680          | 7.946           | 8.055  | 8.164  | 8.232  | 8.382  | 8.490  | 8.599  | 8.708  | 8.816  | 8.925  | 9.033  |
| .700          | 8.111           | 8.221  | 8.331  | 8.436  | 8.551  | 8.661  | 8.771  | 8.880  | 8.990  | 9.099  | 9.209  |
| .720          | 8.283           | 8.395  | 8.506  | 8.617  | 8.728  | 8.795  | 8.950  | 9.060  | 9.171  | 9.235  | 9.392  |
| .740          | 8.464           | 8.577  | 8.688  | 8.801  | 8.913  | 9.025  | 9.137  | 9.249  | 9.361  | 9.473  | 9.584  |
| .760          | 8.655           | 8.769  | 8.882  | 8.996  | 9.064  | 9.222  | 9.334  | 9.449  | 9.562  | 9.674  | 9.787  |
| .780          | 8.858           | 8.973  | 9.088  | 9.203  | 9.317  | 9.432  | 9.546  | 9.654  | 9.774  | 9.888  | 10.002 |
| .800          | 9.075           | 9.192  | 9.307  | 9.424  | 9.540  | 9.655  | 9.771  | 9.887  | 10.002 | 10.117 | 10.181 |
| .820          | 9.310           | 9.427  | 9.545  | 9.614  | 9.780  | 9.897  | 10.014 | 10.131 | 10.247 | 10.364 | 10.481 |
| .840          | 9.566           | 9.685  | 9.804  | 9.923  | 10.041 | 10.160 | 10.278 | 10.397 | 10.462 | 10.633 | 10.751 |
| .860          | 9.848           | 9.969  | 10.090 | 10.210 | 10.331 | 10.451 | 10.571 | 10.691 | 10.811 | 10.930 | 11.050 |
| .880          | 10.166          | 10.289 | 10.411 | 10.534 | 10.656 | 10.778 | 10.900 | 11.021 | 11.143 | 11.264 | 11.384 |
| .900          | 10.532          | 10.657 | 10.778 | 10.905 | 11.030 | 11.154 | 11.277 | 11.401 | 11.524 | 11.648 | 11.771 |
| .920          | 10.966          | 11.094 | 11.220 | 11.347 | 11.473 | 11.600 | 11.726 | 11.851 | 11.977 | 12.103 | 12.228 |
| .940          | 11.508          | 11.638 | 11.768 | 11.897 | 12.026 | 12.155 | 12.284 | 12.413 | 12.541 | 12.669 | 12.797 |
| .950          | 11.842          | 11.974 | 12.105 | 12.236 | 12.367 | 12.498 | 12.628 | 12.759 | 12.889 | 13.018 | 13.148 |
| .960          | 12.243          | 12.376 | 12.510 | 12.643 | 12.775 | 12.908 | 13.040 | 13.173 | 13.305 | 13.436 | 13.568 |
| .970          | 12.747          | 12.883 | 13.018 | 13.154 | 13.289 | 13.424 | 13.559 | 13.693 | 13.827 | 13.962 | 14.095 |
| .980          | 13.436          | 13.576 | 13.715 | 13.853 | 13.992 | 14.130 | 14.268 | 14.405 | 14.543 | 14.680 | 14.817 |
| .990          | 14.571          | 14.715 | 14.859 | 15.003 | 15.146 | 15.289 | 15.432 | 15.574 | 15.716 | 15.858 | 16.000 |
| .995          | 15.660          | 15.809 | 15.957 | 16.105 | 16.253 | 16.401 | 16.548 | 16.695 | 16.841 | 16.988 | 17.134 |
| .999          | 18.062          | 18.220 | 18.378 | 18.535 | 18.692 | 18.849 | 19.005 | 19.161 | 19.316 | 19.471 | 19.626 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 8.00            | 8.10   | 8.20   | 8.30   | 8.40   | 8.50   | 8.60   | 8.70   | 8.80   | 8.90   | 9.00   |
| .001          | 1.971           | 2.018  | 2.065  | 2.112  | 2.160  | 2.208  | 2.256  | 2.305  | 2.354  | 2.403  | 2.452  |
| .005          | 2.571           | 2.626  | 2.681  | 2.737  | 2.793  | 2.849  | 2.905  | 2.961  | 3.018  | 3.075  | 3.132  |
| .010          | 2.906           | 2.965  | 3.024  | 3.084  | 3.144  | 3.204  | 3.264  | 3.325  | 3.385  | 3.446  | 3.507  |
| .020          | 3.307           | 3.371  | 3.435  | 3.499  | 3.563  | 3.627  | 3.692  | 3.757  | 3.822  | 3.888  | 3.953  |
| .030          | 3.581           | 3.648  | 3.715  | 3.782  | 3.849  | 3.916  | 3.984  | 4.052  | 4.120  | 4.188  | 4.256  |
| .040          | 3.798           | 3.867  | 3.936  | 4.005  | 4.074  | 4.144  | 4.214  | 4.284  | 4.354  | 4.424  | 4.494  |
| .050          | 3.981           | 4.051  | 4.122  | 4.193  | 4.265  | 4.336  | 4.407  | 4.479  | 4.551  | 4.623  | 4.695  |
| .060          | 4.141           | 4.214  | 4.286  | 4.359  | 4.431  | 4.504  | 4.577  | 4.650  | 4.724  | 4.797  | 4.871  |
| .080          | 4.418           | 4.493  | 4.568  | 4.643  | 4.718  | 4.794  | 4.870  | 4.945  | 5.021  | 5.097  | 5.173  |
| .100          | 4.656           | 4.733  | 4.810  | 4.888  | 4.965  | 5.043  | 5.120  | 5.198  | 5.276  | 5.354  | 5.432  |
| .120          | 4.868           | 4.947  | 5.026  | 5.106  | 5.185  | 5.264  | 5.344  | 5.423  | 5.503  | 5.583  | 5.663  |
| .140          | 5.063           | 5.143  | 5.224  | 5.305  | 5.379  | 5.467  | 5.548  | 5.629  | 5.711  | 5.792  | 5.874  |
| .160          | 5.243           | 5.326  | 5.408  | 5.490  | 5.572  | 5.655  | 5.738  | 5.820  | 5.903  | 5.986  | 6.069  |
| .180          | 5.414           | 5.497  | 5.581  | 5.665  | 5.748  | 5.832  | 5.916  | 5.997  | 6.085  | 6.169  | 6.253  |
| .200          | 5.569           | 5.661  | 5.746  | 5.831  | 5.916  | 6.001  | 6.086  | 6.172  | 6.257  | 6.343  | 6.428  |
| .220          | 5.732           | 5.818  | 5.904  | 5.990  | 6.077  | 6.163  | 6.250  | 6.336  | 6.407  | 6.510  | 6.596  |
| .240          | 5.882           | 5.970  | 6.053  | 6.141  | 6.232  | 6.319  | 6.407  | 6.495  | 6.583  | 6.670  | 6.758  |
| .260          | 6.029           | 6.117  | 6.206  | 6.294  | 6.383  | 6.471  | 6.560  | 6.649  | 6.730  | 6.827  | 6.916  |
| .280          | 6.172           | 6.261  | 6.351  | 6.440  | 6.530  | 6.616  | 6.710  | 6.783  | 6.889  | 6.979  | 7.069  |
| .300          | 6.312           | 6.403  | 6.493  | 6.584  | 6.675  | 6.757  | 6.856  | 6.947  | 7.038  | 7.129  | 7.220  |
| .320          | 6.450           | 6.542  | 6.633  | 6.725  | 6.817  | 6.909  | 7.000  | 7.092  | 7.184  | 7.276  | 7.368  |
| .340          | 6.554           | 6.679  | 6.772  | 6.865  | 6.957  | 7.050  | 7.143  | 7.235  | 7.328  | 7.421  | 7.514  |
| .360          | 6.722           | 6.816  | 6.909  | 7.003  | 7.097  | 7.190  | 7.284  | 7.378  | 7.472  | 7.565  | 7.659  |
| .380          | 6.857           | 6.952  | 7.046  | 7.141  | 7.199  | 7.330  | 7.424  | 7.519  | 7.614  | 7.708  | 7.803  |
| .400          | 6.983           | 7.087  | 7.182  | 7.278  | 7.373  | 7.469  | 7.564  | 7.660  | 7.755  | 7.851  | 7.947  |
| .420          | 7.126           | 7.222  | 7.318  | 7.415  | 7.511  | 7.607  | 7.704  | 7.800  | 7.897  | 7.993  | 8.089  |
| .440          | 7.260           | 7.357  | 7.455  | 7.552  | 7.649  | 7.747  | 7.844  | 7.941  | 8.039  | 8.136  | 8.233  |
| .460          | 7.395           | 7.494  | 7.592  | 7.690  | 7.788  | 7.886  | 7.985  | 8.083  | 8.181  | 8.279  | 8.378  |
| .480          | 7.532           | 7.631  | 7.730  | 7.828  | 7.928  | 8.027  | 8.126  | 8.225  | 8.324  | 8.423  | 8.523  |
| .500          | 7.660           | 7.769  | 7.869  | 7.969  | 8.059  | 8.169  | 8.269  | 8.327  | 8.469  | 8.566  | 8.666  |
| .520          | 7.808           | 7.909  | 8.010  | 8.111  | 8.212  | 8.313  | 8.414  | 8.514  | 8.615  | 8.716  | 8.795  |
| .540          | 7.950           | 8.052  | 8.153  | 8.245  | 8.357  | 8.459  | 8.539  | 8.662  | 8.763  | 8.865  | 8.967  |
| .560          | 8.093           | 8.196  | 8.299  | 8.401  | 8.483  | 8.607  | 8.709  | 8.812  | 8.914  | 9.017  | 9.120  |
| .580          | 8.235           | 8.344  | 8.447  | 8.551  | 8.654  | 8.758  | 8.856  | 8.965  | 9.068  | 9.169  | 9.275  |
| .600          | 8.390           | 8.489  | 8.597  | 8.703  | 8.808  | 8.901  | 9.014  | 9.121  | 9.225  | 9.283  | 9.434  |
| .620          | 8.543           | 8.649  | 8.711  | 8.860  | 8.920  | 9.070  | 9.176  | 9.280  | 9.386  | 9.492  | 9.597  |
| .640          | 8.701           | 8.805  | 8.914  | 8.976  | 9.127  | 9.210  | 9.293  | 9.446  | 9.504  | 9.658  | 9.764  |
| .660          | 8.865           | 8.972  | 9.079  | 9.186  | 9.294  | 9.401  | 9.508  | 9.615  | 9.723  | 9.830  | 9.887  |
| .680          | 9.033           | 9.096  | 9.250  | 9.358  | 9.467  | 9.569  | 9.683  | 9.791  | 9.899  | 9.995  | 10.115 |
| .700          | 9.209           | 9.318  | 9.428  | 9.537  | 9.643  | 9.756  | 9.865  | 9.974  | 10.081 | 10.192 | 10.301 |
| .720          | 9.392           | 9.503  | 9.613  | 9.723  | 9.834  | 9.944  | 10.054 | 10.164 | 10.274 | 10.378 | 10.494 |
| .740          | 9.584           | 9.696  | 9.808  | 9.919  | 10.030 | 10.142 | 10.253 | 10.351 | 10.475 | 10.559 | 10.697 |
| .760          | 9.787           | 9.900  | 9.987  | 10.125 | 10.238 | 10.350 | 10.462 | 10.575 | 10.687 | 10.799 | 10.911 |
| .780          | 10.002          | 10.116 | 10.230 | 10.344 | 10.405 | 10.571 | 10.684 | 10.798 | 10.908 | 11.024 | 11.109 |
| .800          | 10.181          | 10.348 | 10.463 | 10.578 | 10.693 | 10.807 | 10.922 | 11.036 | 11.151 | 11.265 | 11.380 |
| .820          | 10.481          | 10.597 | 10.714 | 10.830 | 10.946 | 11.062 | 11.178 | 11.294 | 11.410 | 11.525 | 11.641 |
| .840          | 10.751          | 10.869 | 10.987 | 11.104 | 11.222 | 11.332 | 11.457 | 11.574 | 11.691 | 11.808 | 11.925 |
| .860          | 11.050          | 11.169 | 11.289 | 11.408 | 11.527 | 11.646 | 11.765 | 11.883 | 12.002 | 12.120 | 12.239 |
| .880          | 11.384          | 11.507 | 11.627 | 11.748 | 11.869 | 11.990 | 12.079 | 12.230 | 12.351 | 12.471 | 12.528 |
| .900          | 11.771          | 11.894 | 12.017 | 12.140 | 12.262 | 12.385 | 12.507 | 12.629 | 12.751 | 12.873 | 12.995 |
| .920          | 12.228          | 12.353 | 12.478 | 12.603 | 12.728 | 12.853 | 12.977 | 13.101 | 13.226 | 13.345 | 13.473 |
| .940          | 12.797          | 12.925 | 13.053 | 13.181 | 13.308 | 13.435 | 13.562 | 13.689 | 13.816 | 13.942 | 14.069 |
| .950          | 13.148          | 13.278 | 13.407 | 13.536 | 13.665 | 13.794 | 13.922 | 14.050 | 14.179 | 14.307 | 14.435 |
| .960          | 13.568          | 13.699 | 13.830 | 13.961 | 14.092 | 14.222 | 14.353 | 14.483 | 14.613 | 14.743 | 14.873 |
| .970          | 14.095          | 14.229 | 14.362 | 14.496 | 14.629 | 14.761 | 14.894 | 15.026 | 15.159 | 15.291 | 15.422 |
| .980          | 14.817          | 14.953 | 15.090 | 15.226 | 15.362 | 15.498 | 15.633 | 15.768 | 15.903 | 16.038 | 16.173 |
| .990          | 16.000          | 16.141 | 16.282 | 16.423 | 16.564 | 16.704 | 16.844 | 16.984 | 17.124 | 17.263 | 17.403 |
| .995          | 17.134          | 17.279 | 17.425 | 17.570 | 17.715 | 17.859 | 18.004 | 18.148 | 18.291 | 18.435 | 18.578 |
| .999          | 19.626          | 19.781 | 19.935 | 20.088 | 20.242 | 20.395 | 20.548 | 20.700 | 20.853 | 21.004 | 21.156 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 9.00            | 9.10   | 9.20   | 9.30   | 9.40   | 9.50   | 9.60   | 9.70   | 9.80   | 9.90   | 10.00  |
| .001          | 2.452           | 2.502  | 2.552  | 2.602  | 2.653  | 2.703  | 2.754  | 2.806  | 2.857  | 2.909  | 2.961  |
| .005          | 3.132           | 3.190  | 3.248  | 3.305  | 3.364  | 3.422  | 3.481  | 3.539  | 3.598  | 3.658  | 3.717  |
| .010          | 3.507           | 3.569  | 3.630  | 3.692  | 3.754  | 3.816  | 3.879  | 3.941  | 4.004  | 4.067  | 4.130  |
| .020          | 3.953           | 4.019  | 4.085  | 4.151  | 4.217  | 4.284  | 4.350  | 4.417  | 4.484  | 4.551  | 4.618  |
| .030          | 4.256           | 4.324  | 4.393  | 4.462  | 4.531  | 4.600  | 4.670  | 4.739  | 4.809  | 4.879  | 4.949  |
| .040          | 4.494           | 4.565  | 4.636  | 4.707  | 4.778  | 4.849  | 4.921  | 4.992  | 5.064  | 5.136  | 5.208  |
| .050          | 4.695           | 4.768  | 4.840  | 4.913  | 4.986  | 5.059  | 5.132  | 5.205  | 5.278  | 5.352  | 5.425  |
| .060          | 4.871           | 4.945  | 5.019  | 5.093  | 5.167  | 5.242  | 5.316  | 5.391  | 5.466  | 5.541  | 5.616  |
| .080          | 5.173           | 5.250  | 5.326  | 5.403  | 5.479  | 5.556  | 5.633  | 5.710  | 5.787  | 5.865  | 5.942  |
| .100          | 5.432           | 5.511  | 5.589  | 5.668  | 5.747  | 5.825  | 5.904  | 5.983  | 6.063  | 6.142  | 6.221  |
| .120          | 5.663           | 5.743  | 5.824  | 5.904  | 5.984  | 6.065  | 6.146  | 6.226  | 6.307  | 6.388  | 6.469  |
| .140          | 5.874           | 5.955  | 6.037  | 6.119  | 6.201  | 6.283  | 6.362  | 6.448  | 6.530  | 6.613  | 6.695  |
| .160          | 6.069           | 6.152  | 6.236  | 6.319  | 6.402  | 6.486  | 6.569  | 6.653  | 6.737  | 6.821  | 6.905  |
| .180          | 6.253           | 6.338  | 6.422  | 6.507  | 6.592  | 6.677  | 6.762  | 6.847  | 6.932  | 7.017  | 7.102  |
| .200          | 6.428           | 6.514  | 6.600  | 6.686  | 6.772  | 6.858  | 6.944  | 7.030  | 7.116  | 7.203  | 7.289  |
| .220          | 6.596           | 6.683  | 6.770  | 6.857  | 6.944  | 7.032  | 7.119  | 7.206  | 7.294  | 7.381  | 7.469  |
| .240          | 6.758           | 6.846  | 6.935  | 7.023  | 7.111  | 7.199  | 7.287  | 7.376  | 7.464  | 7.553  | 7.641  |
| .260          | 6.916           | 7.005  | 7.094  | 7.183  | 7.272  | 7.357  | 7.451  | 7.541  | 7.629  | 7.720  | 7.809  |
| .280          | 7.069           | 7.157  | 7.250  | 7.340  | 7.430  | 7.520  | 7.610  | 7.701  | 7.792  | 7.882  | 7.973  |
| .300          | 7.220           | 7.311  | 7.402  | 7.493  | 7.585  | 7.676  | 7.767  | 7.859  | 7.950  | 8.041  | 8.133  |
| .320          | 7.368           | 7.460  | 7.552  | 7.644  | 7.736  | 7.829  | 7.920  | 8.013  | 8.106  | 8.198  | 8.290  |
| .340          | 7.514           | 7.607  | 7.700  | 7.793  | 7.886  | 7.980  | 8.073  | 8.166  | 8.249  | 8.352  | 8.446  |
| .360          | 7.659           | 7.753  | 7.847  | 7.941  | 8.035  | 8.129  | 8.223  | 8.317  | 8.411  | 8.505  | 8.600  |
| .380          | 7.803           | 7.898  | 7.993  | 8.088  | 8.182  | 8.277  | 8.372  | 8.467  | 8.562  | 8.657  | 8.752  |
| .400          | 7.947           | 8.042  | 8.138  | 8.234  | 8.329  | 8.383  | 8.478  | 8.595  | 8.713  | 8.809  | 8.904  |
| .420          | 8.089           | 8.186  | 8.283  | 8.338  | 8.471  | 8.573  | 8.669  | 8.766  | 8.863  | 8.959  | 9.056  |
| .440          | 8.233           | 8.331  | 8.386  | 8.515  | 8.623  | 8.721  | 8.818  | 8.916  | 9.013  | 9.111  | 9.208  |
| .460          | 8.378           | 8.476  | 8.574  | 8.672  | 8.771  | 8.869  | 8.967  | 9.043  | 9.164  | 9.262  | 9.361  |
| .480          | 8.523           | 8.619  | 8.699  | 8.809  | 8.919  | 9.018  | 9.117  | 9.214  | 9.316  | 9.415  | 9.514  |
| .500          | 8.666           | 8.769  | 8.869  | 8.969  | 9.069  | 9.169  | 9.269  | 9.369  | 9.468  | 9.569  | 9.669  |
| .520          | 8.795           | 8.917  | 9.019  | 9.119  | 9.219  | 9.321  | 9.422  | 9.520  | 9.623  | 9.724  | 9.825  |
| .540          | 8.967           | 9.069  | 9.170  | 9.249  | 9.374  | 9.475  | 9.553  | 9.679  | 9.780  | 9.882  | 9.934  |
| .560          | 9.120           | 9.222  | 9.325  | 9.403  | 9.530  | 9.632  | 9.735  | 9.837  | 9.940  | 10.042 | 10.144 |
| .580          | 9.275           | 9.378  | 9.482  | 9.561  | 9.689  | 9.792  | 9.895  | 9.999  | 10.102 | 10.205 | 10.302 |
| .600          | 9.434           | 9.538  | 9.642  | 9.747  | 9.851  | 9.955  | 10.059 | 10.163 | 10.268 | 10.372 | 10.476 |
| .620          | 9.597           | 9.702  | 9.801  | 9.863  | 10.017 | 10.122 | 10.227 | 10.332 | 10.437 | 10.542 | 10.647 |
| .640          | 9.764           | 9.870  | 9.976  | 10.082 | 10.188 | 10.294 | 10.400 | 10.506 | 10.611 | 10.717 | 10.823 |
| .660          | 9.887           | 10.044 | 10.147 | 10.244 | 10.364 | 10.471 | 10.578 | 10.685 | 10.791 | 10.898 | 11.005 |
| .680          | 10.115          | 10.223 | 10.331 | 10.439 | 10.540 | 10.653 | 10.762 | 10.870 | 10.977 | 11.085 | 11.192 |
| .700          | 10.301          | 10.410 | 10.518 | 10.627 | 10.736 | 10.845 | 10.953 | 11.034 | 11.163 | 11.279 | 11.387 |
| .720          | 10.494          | 10.602 | 10.714 | 10.824 | 10.926 | 11.043 | 11.138 | 11.262 | 11.372 | 11.481 | 11.590 |
| .740          | 10.697          | 10.808 | 10.919 | 11.029 | 11.140 | 11.251 | 11.361 | 11.472 | 11.582 | 11.693 | 11.803 |
| .760          | 10.911          | 11.023 | 11.135 | 11.246 | 11.358 | 11.470 | 11.582 | 11.693 | 11.805 | 11.916 | 12.027 |
| .780          | 11.109          | 11.251 | 11.364 | 11.477 | 11.589 | 11.702 | 11.815 | 11.912 | 12.040 | 12.153 | 12.265 |
| .800          | 11.380          | 11.494 | 11.608 | 11.722 | 11.836 | 11.943 | 12.064 | 12.178 | 12.292 | 12.405 | 12.519 |
| .820          | 11.641          | 11.756 | 11.872 | 11.987 | 12.102 | 12.217 | 12.332 | 12.447 | 12.562 | 12.677 | 12.792 |
| .840          | 11.925          | 12.042 | 12.159 | 12.275 | 12.392 | 12.508 | 12.625 | 12.741 | 12.857 | 12.973 | 13.089 |
| .860          | 12.239          | 12.357 | 12.475 | 12.593 | 12.711 | 12.765 | 12.947 | 13.065 | 13.182 | 13.300 | 13.417 |
| .880          | 12.528          | 12.711 | 12.830 | 12.950 | 13.070 | 13.189 | 13.308 | 13.427 | 13.547 | 13.666 | 13.785 |
| .900          | 12.995          | 13.116 | 13.204 | 13.359 | 13.481 | 13.602 | 13.723 | 13.844 | 13.965 | 14.085 | 14.206 |
| .920          | 13.473          | 13.597 | 13.721 | 13.844 | 13.967 | 14.091 | 14.214 | 14.337 | 14.460 | 14.582 | 14.705 |
| .940          | 14.069          | 14.195 | 14.321 | 14.447 | 14.573 | 14.698 | 14.824 | 14.949 | 15.074 | 15.199 | 15.324 |
| .950          | 14.435          | 14.562 | 14.690 | 14.817 | 14.945 | 15.072 | 15.179 | 15.326 | 15.452 | 15.579 | 15.705 |
| .960          | 14.873          | 15.002 | 15.131 | 15.260 | 15.390 | 15.518 | 15.647 | 15.776 | 15.904 | 16.032 | 16.160 |
| .970          | 15.422          | 15.554 | 15.685 | 15.817 | 15.948 | 16.079 | 16.210 | 16.340 | 16.471 | 16.601 | 16.731 |
| .980          | 16.173          | 16.308 | 16.442 | 16.576 | 16.710 | 16.844 | 16.977 | 17.111 | 17.244 | 17.377 | 17.510 |
| .990          | 17.403          | 17.542 | 17.680 | 17.819 | 17.957 | 18.095 | 18.233 | 18.371 | 18.509 | 18.646 | 18.783 |
| .995          | 18.578          | 18.721 | 18.864 | 19.007 | 19.149 | 19.291 | 19.433 | 19.575 | 19.716 | 19.857 | 19.998 |
| .999          | 21.156          | 21.308 | 21.458 | 21.609 | 21.760 | 21.910 | 22.060 | 22.210 | 22.359 | 22.508 | 22.657 |

### Percentage Points of the Gamma Distribution with Unit Scale Parameter

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 10.00           | 10.50  | 11.00  | 11.50  | 12.00  | 12.50  | 13.00  | 13.50  | 14.00  | 14.50  | 15.00  |
| .001          | 2.961           | 3.223  | 3.492  | 3.765  | 4.042  | 4.325  | 4.611  | 4.901  | 5.195  | 5.493  | 5.794  |
| .005          | 3.717           | 4.017  | 4.321  | 4.630  | 4.943  | 5.260  | 5.580  | 5.904  | 6.231  | 6.561  | 6.893  |
| .010          | 4.130           | 4.449  | 4.771  | 5.098  | 5.428  | 5.762  | 6.099  | 6.439  | 6.782  | 7.128  | 7.477  |
| .020          | 4.618           | 4.957  | 5.300  | 5.646  | 5.996  | 6.349  | 6.704  | 7.063  | 7.424  | 7.787  | 8.153  |
| .030          | 4.949           | 5.301  | 5.656  | 6.015  | 6.377  | 6.742  | 7.110  | 7.480  | 7.852  | 8.227  | 8.604  |
| .040          | 5.208           | 5.570  | 5.935  | 6.304  | 6.675  | 7.049  | 7.425  | 7.804  | 8.186  | 8.569  | 8.954  |
| .050          | 5.425           | 5.796  | 6.169  | 6.545  | 6.924  | 7.306  | 7.690  | 8.076  | 8.464  | 8.854  | 9.246  |
| .060          | 5.616           | 5.993  | 6.373  | 6.756  | 7.141  | 7.529  | 7.919  | 8.312  | 8.706  | 9.102  | 9.500  |
| .080          | 5.942           | 6.331  | 6.723  | 7.117  | 7.513  | 7.911  | 8.312  | 8.715  | 9.119  | 9.525  | 9.933  |
| .100          | 6.221           | 6.620  | 7.021  | 7.424  | 7.829  | 8.237  | 8.646  | 9.057  | 9.470  | 9.884  | 10.300 |
| .120          | 6.469           | 6.876  | 7.285  | 7.696  | 8.110  | 8.525  | 8.941  | 9.360  | 9.780  | 10.201 | 10.624 |
| .140          | 6.695           | 7.110  | 7.526  | 7.944  | 8.364  | 8.786  | 9.210  | 9.634  | 10.061 | 10.488 | 10.917 |
| .160          | 6.905           | 7.326  | 7.710  | 8.174  | 8.599  | 9.028  | 9.457  | 9.888  | 10.320 | 10.754 | 11.188 |
| .180          | 7.102           | 7.529  | 7.958  | 8.389  | 8.821  | 9.252  | 9.690  | 10.126 | 10.564 | 11.002 | 11.442 |
| .200          | 7.289           | 7.722  | 8.157  | 8.593  | 9.031  | 9.470  | 9.910  | 10.351 | 10.794 | 11.238 | 11.682 |
| .220          | 7.469           | 7.907  | 8.347  | 8.789  | 9.231  | 9.651  | 10.121 | 10.567 | 10.987 | 11.462 | 11.911 |
| .240          | 7.641           | 8.084  | 8.530  | 8.977  | 9.424  | 9.873  | 10.322 | 10.774 | 11.225 | 11.678 | 12.131 |
| .260          | 7.809           | 8.258  | 8.708  | 9.159  | 9.611  | 10.065 | 10.519 | 10.974 | 11.430 | 11.887 | 12.343 |
| .280          | 7.973           | 8.426  | 8.881  | 9.337  | 9.787  | 10.200 | 10.710 | 11.169 | 11.626 | 12.090 | 12.552 |
| .300          | 8.133           | 8.591  | 9.028  | 9.511  | 9.959  | 10.434 | 10.896 | 11.360 | 11.824 | 12.288 | 12.754 |
| .320          | 8.290           | 8.731  | 9.217  | 9.680  | 10.146 | 10.612 | 11.079 | 11.547 | 12.015 | 12.483 | 12.948 |
| .340          | 8.446           | 8.910  | 9.381  | 9.849  | 10.293 | 10.789 | 11.259 | 11.731 | 12.202 | 12.675 | 13.147 |
| .360          | 8.600           | 9.071  | 9.543  | 10.016 | 10.489 | 10.963 | 11.438 | 11.913 | 12.387 | 12.864 | 13.332 |
| .380          | 8.752           | 9.227  | 9.703  | 10.181 | 10.655 | 11.136 | 11.611 | 12.093 | 12.572 | 13.019 | 13.531 |
| .400          | 8.904           | 9.384  | 9.864  | 10.345 | 10.826 | 11.308 | 11.790 | 12.272 | 12.755 | 13.238 | 13.721 |
| .420          | 9.056           | 9.540  | 10.024 | 10.509 | 10.994 | 11.479 | 11.965 | 12.451 | 12.937 | 13.423 | 13.910 |
| .440          | 9.208           | 9.696  | 10.184 | 10.673 | 11.134 | 11.621 | 12.139 | 12.629 | 13.119 | 13.608 | 14.098 |
| .460          | 9.361           | 9.853  | 10.345 | 10.837 | 11.329 | 11.822 | 12.311 | 12.808 | 13.234 | 13.794 | 14.252 |
| .480          | 9.514           | 10.010 | 10.506 | 11.002 | 11.498 | 11.995 | 12.491 | 12.987 | 13.475 | 13.911 | 14.477 |
| .500          | 9.669           | 10.143 | 10.669 | 11.168 | 11.668 | 12.107 | 12.668 | 13.164 | 13.668 | 14.168 | 14.667 |
| .520          | 9.825           | 10.327 | 10.833 | 11.333 | 11.840 | 12.344 | 12.839 | 13.342 | 13.854 | 14.357 | 14.861 |
| .540          | 9.934           | 10.491 | 10.999 | 11.507 | 12.014 | 12.505 | 13.028 | 13.531 | 14.042 | 14.549 | 15.054 |
| .560          | 10.144          | 10.656 | 11.168 | 11.650 | 12.190 | 12.701 | 13.212 | 13.721 | 14.233 | 14.743 | 15.252 |
| .580          | 10.302          | 10.823 | 11.311 | 11.855 | 12.370 | 12.885 | 13.399 | 13.912 | 14.427 | 14.940 | 15.453 |
| .600          | 10.476          | 10.996 | 11.515 | 12.054 | 12.553 | 13.071 | 13.589 | 14.105 | 14.624 | 15.139 | 15.658 |
| .620          | 10.647          | 11.164 | 11.694 | 12.217 | 12.741 | 13.263 | 13.784 | 14.287 | 14.752 | 15.347 | 15.862 |
| .640          | 10.823          | 11.352 | 11.879 | 12.406 | 12.929 | 13.459 | 13.967 | 14.509 | 15.034 | 15.558 | 16.081 |
| .660          | 11.005          | 11.537 | 12.069 | 12.538 | 13.129 | 13.661 | 14.190 | 14.719 | 15.245 | 15.775 | 16.302 |
| .680          | 11.192          | 11.730 | 12.266 | 12.797 | 13.336 | 13.870 | 14.403 | 14.935 | 15.466 | 15.999 | 16.529 |
| .700          | 11.387          | 11.929 | 12.470 | 13.005 | 13.547 | 14.086 | 14.623 | 15.160 | 15.695 | 16.231 | 16.765 |
| .720          | 11.590          | 12.135 | 12.682 | 13.226 | 13.769 | 14.311 | 14.853 | 15.393 | 15.933 | 16.472 | 17.000 |
| .740          | 11.803          | 12.354 | 12.904 | 13.453 | 14.000 | 14.547 | 15.093 | 15.637 | 16.181 | 16.725 | 17.267 |
| .760          | 12.027          | 12.575 | 13.138 | 13.674 | 14.244 | 14.795 | 15.345 | 15.893 | 16.443 | 16.990 | 17.536 |
| .780          | 12.265          | 12.826 | 13.386 | 13.945 | 14.502 | 15.058 | 15.612 | 16.165 | 16.719 | 17.270 | 17.821 |
| .800          | 12.519          | 13.086 | 13.651 | 14.214 | 14.777 | 15.337 | 15.897 | 16.456 | 17.013 | 17.570 | 18.125 |
| .820          | 12.792          | 13.365 | 13.935 | 14.505 | 15.072 | 15.637 | 16.204 | 16.767 | 17.285 | 17.891 | 18.451 |
| .840          | 13.089          | 13.668 | 14.245 | 14.820 | 15.394 | 15.886 | 16.536 | 17.105 | 17.673 | 18.240 | 18.805 |
| .860          | 13.417          | 14.003 | 14.586 | 15.168 | 15.748 | 16.326 | 16.903 | 17.478 | 18.051 | 18.624 | 19.195 |
| .880          | 13.785          | 14.378 | 14.969 | 15.557 | 16.144 | 16.729 | 17.312 | 17.894 | 18.473 | 19.053 | 19.630 |
| .900          | 14.206          | 14.808 | 15.407 | 16.003 | 16.555 | 17.191 | 17.782 | 18.371 | 18.958 | 19.518 | 20.128 |
| .920          | 14.705          | 15.316 | 15.925 | 16.531 | 17.135 | 17.730 | 18.336 | 18.933 | 19.529 | 20.123 | 20.715 |
| .940          | 15.324          | 15.947 | 16.567 | 17.185 | 17.799 | 18.412 | 19.022 | 19.628 | 20.235 | 20.839 | 21.442 |
| .950          | 15.705          | 16.335 | 16.962 | 17.586 | 18.208 | 18.826 | 19.442 | 20.057 | 20.669 | 21.278 | 21.886 |
| .960          | 16.160          | 16.799 | 17.434 | 18.066 | 18.695 | 19.321 | 19.945 | 20.566 | 21.185 | 21.802 | 22.417 |
| .970          | 16.731          | 17.380 | 18.025 | 18.666 | 19.305 | 19.940 | 20.573 | 21.203 | 21.831 | 22.457 | 23.080 |
| .980          | 17.510          | 18.172 | 18.830 | 19.484 | 20.135 | 20.783 | 21.428 | 22.070 | 22.709 | 23.346 | 23.981 |
| .990          | 18.783          | 19.466 | 20.145 | 20.819 | 21.490 | 22.157 | 22.821 | 23.481 | 24.139 | 24.794 | 25.446 |
| .995          | 19.998          | 20.701 | 21.398 | 22.091 | 22.779 | 23.464 | 24.145 | 24.822 | 25.497 | 26.168 | 26.836 |
| .999          | 22.657          | 23.398 | 24.134 | 24.864 | 25.589 | 26.310 | 27.026 | 27.738 | 28.446 | 29.150 | 29.851 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 15.00           | 15.50  | 16.00  | 16.50  | 17.00  | 17.50  | 18.00  | 18.50  | 19.00  | 19.50  | 20.00  |
| .001          | 5.794           | 6.098  | 6.405  | 6.715  | 7.028  | 7.344  | 7.662  | 7.983  | 8.306  | 8.631  | 8.958  |
| .005          | 6.893           | 7.229  | 7.567  | 7.908  | 8.251  | 8.596  | 8.943  | 9.293  | 9.644  | 9.998  | 10.353 |
| .010          | 7.477           | 7.828  | 8.181  | 8.537  | 8.895  | 9.254  | 9.616  | 9.980  | 10.346 | 10.713 | 11.082 |
| .020          | 8.153           | 8.521  | 8.891  | 9.264  | 9.638  | 10.014 | 10.391 | 10.771 | 11.152 | 11.535 | 11.919 |
| .030          | 8.604           | 8.983  | 9.364  | 9.747  | 10.131 | 10.517 | 10.905 | 11.295 | 11.686 | 12.078 | 12.472 |
| .040          | 8.954           | 9.341  | 9.730  | 10.121 | 10.514 | 10.908 | 11.303 | 11.700 | 12.099 | 12.498 | 12.899 |
| .050          | 9.246           | 9.640  | 10.036 | 10.433 | 10.832 | 11.233 | 11.634 | 12.037 | 12.442 | 12.848 | 13.255 |
| .060          | 9.500           | 9.900  | 10.301 | 10.704 | 11.108 | 11.514 | 11.921 | 12.330 | 12.739 | 13.150 | 13.562 |
| .080          | 9.933           | 10.342 | 10.753 | 11.165 | 11.578 | 11.993 | 12.409 | 12.826 | 13.244 | 13.662 | 14.084 |
| .100          | 10.300          | 10.717 | 11.135 | 11.555 | 11.976 | 12.398 | 12.822 | 13.214 | 13.663 | 14.098 | 14.525 |
| .120          | 10.624          | 11.048 | 11.473 | 11.899 | 12.326 | 12.755 | 13.185 | 13.616 | 14.047 | 14.480 | 14.913 |
| .140          | 10.917          | 11.347 | 11.778 | 12.211 | 12.644 | 13.079 | 13.513 | 13.950 | 14.387 | 14.825 | 15.264 |
| .160          | 11.188          | 11.624 | 12.060 | 12.498 | 12.937 | 13.376 | 13.816 | 14.258 | 14.700 | 15.143 | 15.587 |
| .180          | 11.442          | 11.883 | 12.323 | 12.767 | 13.210 | 13.621 | 14.100 | 14.546 | 14.992 | 15.440 | 15.888 |
| .200          | 11.682          | 12.128 | 12.574 | 13.021 | 13.436 | 13.918 | 14.367 | 14.818 | 15.259 | 15.682 | 16.172 |
| .220          | 11.911          | 12.361 | 12.812 | 13.263 | 13.716 | 14.169 | 14.614 | 15.077 | 15.529 | 15.987 | 16.443 |
| .240          | 12.131          | 12.586 | 13.025 | 13.496 | 13.944 | 14.410 | 14.867 | 15.325 | 15.784 | 16.244 | 16.693 |
| .260          | 12.343          | 12.803 | 13.262 | 13.687 | 14.177 | 14.642 | 15.104 | 15.556 | 16.028 | 16.491 | 16.955 |
| .280          | 12.552          | 13.013 | 13.409 | 13.940 | 14.404 | 14.869 | 15.334 | 15.799 | 16.265 | 16.731 | 17.193 |
| .300          | 12.754          | 13.216 | 13.686 | 14.153 | 14.621 | 15.080 | 15.558 | 16.022 | 16.495 | 16.961 | 17.436 |
| .320          | 12.948          | 13.418 | 13.892 | 14.363 | 14.834 | 15.305 | 15.767 | 16.244 | 16.717 | 17.195 | 17.669 |
| .340          | 13.147          | 13.621 | 14.094 | 14.568 | 15.043 | 15.518 | 15.993 | 16.469 | 16.944 | 17.418 | 17.897 |
| .360          | 13.332          | 13.816 | 14.294 | 14.771 | 15.249 | 15.727 | 16.206 | 16.685 | 17.163 | 17.643 | 18.123 |
| .380          | 13.531          | 14.011 | 14.490 | 14.973 | 15.454 | 15.934 | 16.417 | 16.899 | 17.380 | 17.841 | 18.346 |
| .400          | 13.721          | 14.204 | 14.687 | 15.134 | 15.657 | 16.141 | 16.626 | 17.100 | 17.595 | 18.079 | 18.567 |
| .420          | 13.910          | 14.397 | 14.884 | 15.371 | 15.858 | 16.341 | 16.831 | 17.322 | 17.810 | 18.299 | 18.787 |
| .440          | 14.098          | 14.589 | 15.079 | 15.569 | 16.059 | 16.551 | 17.040 | 17.533 | 18.018 | 18.515 | 19.007 |
| .460          | 14.252          | 14.781 | 15.274 | 15.768 | 16.262 | 16.756 | 17.250 | 17.744 | 18.238 | 18.731 | 19.226 |
| .480          | 14.477          | 14.899 | 15.471 | 15.967 | 16.464 | 16.961 | 17.457 | 17.955 | 18.452 | 18.949 | 19.443 |
| .500          | 14.667          | 15.158 | 15.668 | 16.168 | 16.668 | 17.168 | 17.623 | 18.166 | 18.668 | 19.168 | 19.667 |
| .520          | 14.861          | 15.325 | 15.827 | 16.370 | 16.873 | 17.376 | 17.878 | 18.376 | 18.885 | 19.386 | 19.891 |
| .540          | 15.054          | 15.562 | 16.058 | 16.574 | 17.080 | 17.581 | 18.093 | 18.599 | 19.104 | 19.604 | 20.116 |
| .560          | 15.252          | 15.761 | 16.271 | 16.781 | 17.291 | 17.794 | 18.306 | 18.812 | 19.325 | 19.785 | 20.344 |
| .580          | 15.453          | 15.966 | 16.479 | 16.949 | 17.499 | 18.017 | 18.523 | 19.041 | 19.552 | 20.064 | 20.575 |
| .600          | 15.658          | 16.169 | 16.690 | 17.206 | 17.722 | 18.191 | 18.752 | 19.267 | 19.782 | 20.195 | 20.798 |
| .620          | 15.862          | 16.387 | 16.906 | 17.425 | 17.944 | 18.463 | 18.981 | 19.499 | 20.017 | 20.534 | 21.048 |
| .640          | 16.081          | 16.604 | 17.106 | 17.627 | 18.081 | 18.694 | 19.215 | 19.736 | 20.257 | 20.777 | 21.244 |
| .660          | 16.302          | 16.807 | 17.353 | 17.881 | 18.406 | 18.931 | 19.456 | 19.977 | 20.504 | 21.028 | 21.551 |
| .680          | 16.529          | 17.057 | 17.567 | 18.119 | 18.648 | 19.176 | 19.704 | 20.228 | 20.759 | 21.286 | 21.811 |
| .700          | 16.765          | 17.299 | 17.832 | 18.319 | 18.898 | 19.423 | 19.861 | 20.492 | 21.009 | 21.553 | 22.082 |
| .720          | 17.000          | 17.548 | 18.085 | 18.622 | 19.158 | 19.693 | 20.228 | 20.763 | 21.297 | 21.830 | 22.363 |
| .740          | 17.267          | 17.809 | 18.350 | 18.890 | 19.423 | 19.965 | 20.507 | 21.044 | 21.583 | 22.118 | 22.656 |
| .760          | 17.536          | 18.082 | 18.627 | 19.171 | 19.715 | 20.206 | 20.800 | 21.342 | 21.883 | 22.416 | 22.960 |
| .780          | 17.821          | 18.371 | 18.920 | 19.444 | 20.013 | 20.537 | 21.110 | 21.655 | 22.172 | 22.716 | 23.289 |
| .800          | 18.125          | 18.679 | 19.233 | 19.783 | 20.338 | 20.889 | 21.439 | 21.933 | 22.538 | 23.086 | 23.634 |
| .820          | 18.451          | 18.962 | 19.569 | 20.126 | 20.683 | 21.238 | 21.793 | 22.347 | 22.893 | 23.453 | 24.005 |
| .840          | 18.805          | 19.368 | 19.933 | 20.489 | 21.057 | 21.614 | 22.177 | 22.728 | 23.293 | 23.850 | 24.407 |
| .860          | 19.195          | 19.764 | 20.333 | 20.901 | 21.468 | 22.033 | 22.591 | 23.161 | 23.606 | 24.287 | 24.840 |
| .880          | 19.630          | 20.206 | 20.781 | 21.327 | 21.927 | 22.497 | 23.069 | 23.634 | 24.206 | 24.774 | 25.341 |
| .900          | 20.128          | 20.711 | 21.292 | 21.873 | 22.452 | 23.029 | 23.606 | 24.182 | 24.756 | 25.330 | 25.903 |
| .920          | 20.715          | 21.306 | 21.895 | 22.479 | 23.070 | 23.655 | 24.118 | 24.822 | 25.399 | 25.984 | 26.564 |
| .940          | 21.442          | 22.042 | 22.641 | 23.238 | 23.834 | 24.428 | 25.021 | 25.613 | 26.203 | 26.792 | 27.380 |
| .950          | 21.886          | 22.493 | 23.097 | 23.700 | 24.301 | 24.901 | 25.497 | 26.096 | 26.692 | 27.286 | 27.879 |
| .960          | 22.417          | 23.030 | 23.641 | 24.250 | 24.858 | 25.464 | 26.069 | 26.672 | 27.273 | 27.874 | 28.473 |
| .970          | 23.080          | 23.701 | 24.320 | 24.938 | 25.554 | 26.168 | 26.780 | 27.391 | 28.000 | 28.608 | 29.214 |
| .980          | 23.981          | 24.613 | 25.243 | 25.871 | 26.498 | 27.122 | 27.744 | 28.365 | 28.984 | 29.592 | 30.218 |
| .990          | 25.446          | 26.096 | 26.743 | 27.388 | 28.030 | 28.671 | 29.310 | 29.946 | 30.581 | 31.214 | 31.845 |
| .995          | 26.836          | 27.501 | 28.164 | 28.824 | 29.482 | 30.137 | 30.791 | 31.442 | 32.091 | 32.738 | 33.383 |
| .999          | 29.851          | 30.549 | 31.243 | 31.935 | 32.623 | 33.309 | 33.992 | 34.673 | 35.351 | 36.027 | 36.701 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 20.00           | 20.50  | 21.00  | 21.50  | 22.00  | 22.50  | 23.00  | 23.50  | 24.00  | 24.50  | 25.00  |
| .001          | 8.958           | 9.288  | 9.619  | 9.953  | 10.288 | 10.625 | 10.964 | 11.305 | 11.647 | 11.991 | 12.337 |
| .005          | 10.353          | 10.710 | 11.069 | 11.430 | 11.792 | 12.156 | 12.521 | 12.887 | 13.255 | 13.625 | 13.995 |
| .010          | 11.082          | 11.453 | 11.825 | 12.199 | 12.574 | 12.951 | 13.329 | 13.708 | 14.089 | 14.470 | 14.853 |
| .020          | 11.919          | 12.304 | 12.691 | 13.080 | 13.469 | 13.860 | 14.252 | 14.646 | 15.040 | 15.435 | 15.832 |
| .030          | 12.472          | 12.867 | 13.263 | 13.661 | 14.060 | 14.460 | 14.861 | 15.263 | 15.666 | 16.070 | 16.475 |
| .040          | 12.899          | 13.302 | 13.705 | 14.110 | 14.516 | 14.922 | 15.330 | 15.739 | 16.149 | 16.560 | 16.971 |
| .050          | 13.255          | 13.663 | 14.072 | 14.482 | 14.894 | 15.306 | 15.719 | 16.134 | 16.549 | 16.965 | 17.382 |
| .060          | 13.562          | 13.975 | 14.390 | 14.805 | 15.221 | 15.638 | 16.056 | 16.475 | 16.895 | 17.316 | 17.737 |
| .080          | 14.084          | 14.506 | 14.928 | 15.351 | 15.776 | 16.201 | 16.627 | 17.053 | 17.480 | 17.904 | 18.338 |
| .100          | 14.525          | 14.954 | 15.383 | 15.794 | 16.244 | 16.674 | 17.108 | 17.541 | 17.975 | 18.409 | 18.844 |
| .120          | 14.913          | 15.347 | 15.782 | 16.218 | 16.655 | 17.092 | 17.529 | 17.969 | 18.408 | 18.848 | 19.289 |
| .140          | 15.264          | 15.703 | 16.143 | 16.584 | 17.005 | 17.468 | 17.911 | 18.310 | 18.799 | 19.244 | 19.689 |
| .160          | 15.587          | 16.031 | 16.476 | 16.921 | 17.365 | 17.815 | 18.262 | 18.617 | 19.159 | 19.605 | 20.058 |
| .180          | 15.888          | 16.337 | 16.786 | 17.236 | 17.686 | 18.138 | 18.496 | 19.041 | 19.494 | 19.947 | 20.401 |
| .200          | 16.172          | 16.625 | 17.074 | 17.532 | 17.987 | 18.442 | 18.898 | 19.354 | 19.810 | 20.267 | 20.725 |
| .220          | 16.443          | 16.900 | 17.347 | 17.815 | 18.273 | 18.732 | 19.191 | 19.651 | 20.111 | 20.572 | 21.032 |
| .240          | 16.693          | 17.164 | 17.625 | 18.086 | 18.548 | 19.010 | 19.473 | 19.936 | 20.399 | 20.860 | 21.328 |
| .260          | 16.955          | 17.419 | 17.883 | 18.348 | 18.813 | 19.273 | 19.744 | 20.208 | 20.678 | 21.143 | 21.612 |
| .280          | 17.193          | 17.666 | 18.133 | 18.601 | 19.070 | 19.538 | 19.983 | 20.477 | 20.843 | 21.418 | 21.881 |
| .300          | 17.436          | 17.906 | 18.377 | 18.849 | 19.317 | 19.791 | 20.265 | 20.737 | 21.210 | 21.682 | 22.157 |
| .320          | 17.669          | 18.142 | 18.616 | 19.091 | 19.565 | 20.040 | 20.490 | 20.978 | 21.454 | 21.889 | 22.419 |
| .340          | 17.897          | 18.368 | 18.851 | 19.329 | 19.806 | 20.183 | 20.711 | 21.135 | 21.719 | 22.198 | 22.676 |
| .360          | 18.123          | 18.602 | 19.080 | 19.563 | 20.044 | 20.524 | 21.005 | 21.487 | 21.858 | 22.450 | 22.928 |
| .380          | 18.346          | 18.829 | 19.312 | 19.770 | 20.277 | 20.710 | 21.246 | 21.723 | 22.214 | 22.695 | 23.179 |
| .400          | 18.567          | 19.050 | 19.539 | 20.012 | 20.511 | 20.997 | 21.484 | 21.971 | 22.458 | 22.945 | 23.432 |
| .420          | 18.787          | 19.276 | 19.765 | 20.247 | 20.736 | 21.232 | 21.719 | 22.209 | 22.700 | 23.161 | 23.679 |
| .440          | 19.007          | 19.497 | 19.990 | 20.475 | 20.973 | 21.462 | 21.957 | 22.421 | 22.941 | 23.432 | 23.926 |
| .460          | 19.226          | 19.721 | 20.215 | 20.703 | 21.204 | 21.699 | 22.193 | 22.684 | 23.183 | 23.678 | 24.173 |
| .480          | 19.443          | 19.942 | 20.439 | 20.938 | 21.435 | 21.933 | 22.423 | 22.913 | 23.424 | 23.922 | 24.389 |
| .500          | 19.667          | 20.167 | 20.616 | 21.168 | 21.668 | 22.154 | 22.554 | 23.167 | 23.660 | 24.047 | 24.664 |
| .520          | 19.891          | 20.342 | 20.896 | 21.399 | 21.902 | 22.397 | 22.905 | 23.409 | 23.912 | 24.413 | 24.901 |
| .540          | 20.116          | 20.621 | 21.114 | 21.632 | 22.138 | 22.643 | 23.148 | 23.654 | 24.155 | 24.662 | 25.169 |
| .560          | 20.344          | 20.839 | 21.361 | 21.814 | 22.377 | 22.885 | 23.393 | 23.893 | 24.408 | 24.916 | 25.424 |
| .580          | 20.575          | 21.086 | 21.598 | 22.107 | 22.620 | 23.130 | 23.641 | 24.136 | 24.662 | 25.172 | 25.618 |
| .600          | 20.798          | 21.325 | 21.839 | 22.353 | 22.838 | 23.373 | 23.894 | 24.407 | 24.920 | 25.433 | 25.946 |
| .620          | 21.048          | 21.569 | 22.086 | 22.602 | 23.119 | 23.635 | 24.151 | 24.663 | 25.183 | 25.699 | 26.214 |
| .640          | 21.244          | 21.818 | 22.335 | 22.854 | 23.375 | 23.896 | 24.415 | 24.933 | 25.444 | 25.971 | 26.489 |
| .660          | 21.551          | 22.071 | 22.597 | 23.119 | 23.642 | 24.156 | 24.686 | 25.207 | 25.725 | 26.250 | 26.770 |
| .680          | 21.811          | 22.339 | 22.864 | 23.360 | 23.915 | 24.409 | 24.965 | 25.362 | 26.014 | 26.537 | 27.027 |
| .700          | 22.082          | 22.612 | 23.141 | 23.669 | 24.198 | 24.710 | 25.252 | 25.773 | 26.274 | 26.835 | 27.361 |
| .720          | 22.363          | 22.896 | 23.428 | 23.944 | 24.487 | 25.021 | 25.553 | 26.084 | 26.614 | 27.008 | 27.638 |
| .740          | 22.656          | 23.192 | 23.724 | 24.263 | 24.798 | 25.332 | 25.865 | 26.400 | 26.933 | 27.466 | 27.998 |
| .760          | 22.960          | 23.488 | 24.042 | 24.581 | 25.119 | 25.655 | 26.194 | 26.727 | 27.268 | 27.803 | 28.340 |
| .780          | 23.289          | 23.832 | 24.374 | 24.917 | 25.459 | 26.000 | 26.541 | 27.063 | 27.621 | 28.088 | 28.699 |
| .800          | 23.634          | 24.181 | 24.728 | 25.241 | 25.753 | 26.364 | 26.909 | 27.453 | 27.996 | 28.530 | 29.082 |
| .820          | 24.005          | 24.554 | 25.107 | 25.657 | 26.206 | 26.754 | 27.303 | 27.851 | 28.399 | 28.908 | 29.492 |
| .840          | 24.407          | 24.962 | 25.518 | 26.072 | 26.625 | 27.170 | 27.731 | 28.283 | 28.834 | 29.385 | 29.933 |
| .860          | 24.840          | 25.408 | 25.838 | 26.527 | 27.086 | 27.643 | 28.200 | 28.757 | 29.313 | 29.868 | 30.422 |
| .880          | 25.341          | 25.906 | 26.471 | 27.036 | 27.581 | 28.162 | 28.723 | 29.285 | 29.846 | 30.254 | 30.965 |
| .900          | 25.903          | 26.474 | 27.045 | 27.615 | 28.184 | 28.678 | 29.320 | 29.887 | 30.301 | 31.019 | 31.584 |
| .920          | 26.564          | 27.143 | 27.720 | 28.297 | 28.873 | 29.448 | 30.022 | 30.595 | 31.165 | 31.739 | 32.310 |
| .940          | 27.380          | 27.967 | 28.553 | 29.138 | 29.722 | 30.305 | 30.884 | 31.468 | 32.048 | 32.627 | 33.206 |
| .950          | 27.879          | 28.471 | 29.062 | 29.652 | 30.240 | 30.748 | 31.415 | 32.001 | 32.585 | 33.169 | 33.752 |
| .960          | 28.473          | 29.071 | 29.667 | 30.263 | 30.857 | 31.450 | 32.043 | 32.634 | 33.224 | 33.814 | 34.402 |
| .970          | 29.214          | 29.816 | 30.423 | 31.025 | 31.627 | 32.227 | 32.826 | 33.422 | 34.021 | 34.617 | 35.211 |
| .980          | 30.218          | 30.833 | 31.446 | 32.058 | 32.668 | 33.278 | 33.716 | 34.493 | 35.098 | 35.703 | 36.307 |
| .990          | 31.845          | 32.475 | 33.103 | 33.730 | 34.355 | 34.978 | 35.601 | 36.222 | 36.841 | 37.460 | 38.077 |
| .995          | 33.383          | 34.026 | 34.668 | 35.308 | 35.946 | 36.583 | 37.218 | 37.852 | 38.484 | 39.115 | 39.745 |
| .999          | 36.701          | 37.372 | 38.042 | 38.709 | 39.375 | 40.038 | 40.700 | 41.360 | 42.018 | 42.675 | 43.330 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 25.00           | 25.50  | 26.00  | 26.50  | 27.00  | 27.50  | 28.00  | 28.50  | 29.00  | 29.50  | 30.00  |
| .001          | 12.337          | 12.684 | 13.033 | 13.383 | 13.734 | 14.087 | 14.441 | 14.796 | 15.152 | 15.510 | 15.869 |
| .005          | 13.995          | 14.367 | 14.741 | 15.115 | 15.491 | 15.867 | 16.245 | 16.624 | 17.004 | 17.385 | 17.767 |
| .010          | 14.853          | 15.238 | 15.623 | 16.009 | 16.397 | 16.785 | 17.175 | 17.565 | 17.957 | 18.349 | 18.742 |
| .020          | 15.832          | 16.230 | 16.628 | 17.028 | 17.428 | 17.830 | 18.232 | 18.635 | 19.039 | 19.444 | 19.850 |
| .030          | 16.475          | 16.882 | 17.289 | 17.697 | 18.105 | 18.515 | 18.925 | 19.337 | 19.749 | 20.162 | 20.575 |
| .040          | 16.971          | 17.384 | 17.796 | 18.212 | 18.627 | 19.042 | 19.459 | 19.876 | 20.295 | 20.713 | 21.133 |
| .050          | 17.382          | 17.800 | 18.219 | 18.638 | 18.963 | 19.479 | 19.901 | 20.323 | 20.746 | 21.170 | 21.594 |
| .060          | 17.737          | 18.159 | 18.582 | 19.006 | 19.334 | 19.856 | 20.258 | 20.708 | 21.136 | 21.562 | 21.992 |
| .080          | 18.338          | 18.768 | 19.198 | 19.629 | 20.061 | 20.493 | 20.926 | 21.360 | 21.794 | 22.229 | 22.664 |
| .100          | 18.844          | 19.257 | 19.717 | 20.053 | 20.592 | 21.030 | 21.469 | 21.895 | 22.348 | 22.788 | 23.229 |
| .120          | 19.289          | 19.730 | 20.172 | 20.614 | 21.057 | 21.500 | 21.944 | 22.277 | 22.806 | 23.279 | 23.725 |
| .140          | 19.689          | 20.135 | 20.582 | 21.028 | 21.476 | 21.924 | 22.372 | 22.821 | 23.267 | 23.720 | 24.171 |
| .160          | 20.058          | 20.508 | 20.958 | 21.410 | 21.861 | 22.313 | 22.766 | 23.219 | 23.672 | 24.122 | 24.580 |
| .180          | 20.401          | 20.855 | 21.309 | 21.765 | 22.220 | 22.676 | 23.125 | 23.589 | 24.044 | 24.503 | 24.961 |
| .200          | 20.725          | 21.176 | 21.641 | 22.099 | 22.446 | 23.018 | 23.478 | 23.938 | 24.398 | 24.859 | 25.320 |
| .220          | 21.032          | 21.494 | 21.929 | 22.418 | 22.880 | 23.343 | 23.806 | 24.269 | 24.733 | 25.197 | 25.662 |
| .240          | 21.328          | 21.766 | 22.257 | 22.722 | 23.188 | 23.654 | 24.120 | 24.587 | 25.046 | 25.513 | 25.988 |
| .260          | 21.612          | 22.025 | 22.548 | 22.988 | 23.485 | 23.954 | 24.423 | 24.893 | 25.363 | 25.832 | 26.295 |
| .280          | 21.888          | 22.359 | 22.826 | 23.301 | 23.773 | 24.245 | 24.717 | 25.063 | 25.533 | 26.135 | 26.608 |
| .300          | 22.157          | 22.517 | 23.103 | 23.579 | 24.053 | 24.528 | 25.003 | 25.478 | 25.953 | 26.429 | 26.905 |
| .320          | 22.419          | 22.882 | 23.372 | 23.850 | 24.327 | 24.804 | 25.282 | 25.759 | 26.238 | 26.716 | 27.190 |
| .340          | 22.677          | 23.157 | 23.622 | 24.116 | 24.596 | 25.076 | 25.541 | 26.029 | 26.516 | 26.998 | 27.479 |
| .360          | 22.917          | 23.414 | 23.896 | 24.377 | 24.861 | 25.343 | 25.826 | 26.309 | 26.726 | 27.267 | 27.757 |
| .380          | 23.176          | 23.667 | 24.152 | 24.637 | 24.997 | 25.607 | 26.093 | 26.579 | 27.064 | 27.550 | 28.036 |
| .400          | 23.432          | 23.860 | 24.406 | 24.894 | 25.382 | 25.870 | 26.357 | 26.845 | 27.333 | 27.822 | 28.309 |
| .420          | 23.679          | 24.154 | 24.657 | 25.141 | 25.639 | 26.130 | 26.620 | 27.043 | 27.600 | 28.092 | 28.582 |
| .440          | 23.922          | 24.388 | 24.880 | 25.372 | 25.896 | 26.389 | 26.882 | 27.340 | 27.867 | 28.360 | 28.853 |
| .460          | 24.171          | 24.668 | 25.163 | 25.656 | 26.152 | 26.648 | 27.141 | 27.638 | 28.116 | 28.629 | 29.124 |
| .480          | 24.419          | 24.901 | 25.399 | 25.904 | 26.410 | 26.906 | 27.405 | 27.832 | 28.364 | 28.898 | 29.394 |
| .500          | 24.667          | 25.167 | 25.667 | 26.151 | 26.666 | 27.167 | 27.633 | 28.167 | 28.649 | 29.167 | 29.630 |
| .520          | 24.793          | 25.356 | 25.914 | 26.425 | 26.923 | 27.429 | 27.931 | 28.434 | 28.936 | 29.439 | 29.791 |
| .540          | 25.169          | 25.673 | 26.179 | 26.684 | 27.188 | 27.694 | 28.181 | 28.703 | 29.208 | 29.638 | 30.217 |
| .560          | 25.423          | 25.932 | 26.439 | 26.946 | 27.450 | 27.957 | 28.432 | 28.975 | 29.478 | 29.990 | 30.496 |
| .580          | 25.683          | 26.062 | 26.702 | 27.204 | 27.723 | 28.232 | 28.742 | 29.251 | 29.760 | 30.270 | 30.760 |
| .600          | 25.944          | 26.458 | 26.969 | 27.475 | 27.996 | 28.508 | 29.020 | 29.532 | 30.042 | 30.403 | 31.067 |
| .620          | 26.214          | 26.729 | 27.108 | 27.760 | 28.133 | 28.789 | 29.304 | 29.818 | 30.333 | 30.846 | 31.361 |
| .640          | 26.488          | 27.006 | 27.525 | 28.042 | 28.560 | 29.072 | 29.592 | 30.111 | 30.627 | 31.105 | 31.661 |
| .660          | 26.771          | 27.287 | 27.812 | 28.332 | 28.850 | 29.372 | 29.892 | 30.411 | 30.931 | 31.450 | 31.969 |
| .680          | 27.061          | 27.549 | 28.103 | 28.628 | 29.152 | 29.676 | 30.198 | 30.721 | 31.242 | 31.754 | 32.285 |
| .700          | 27.361          | 27.888 | 28.414 | 28.930 | 29.318 | 29.981 | 30.515 | 31.040 | 31.565 | 32.088 | 32.613 |
| .720          | 27.603          | 28.202 | 28.731 | 29.255 | 29.783 | 30.277 | 30.844 | 31.372 | 31.899 | 32.426 | 32.932 |
| .740          | 27.962          | 28.531 | 29.060 | 29.594 | 30.125 | 30.656 | 31.167 | 31.716 | 32.087 | 32.778 | 33.307 |
| .760          | 28.340          | 28.875 | 29.410 | 29.940 | 30.478 | 30.934 | 31.547 | 32.080 | 32.613 | 33.146 | 33.677 |
| .780          | 28.699          | 29.238 | 29.776 | 30.314 | 30.832 | 31.389 | 31.923 | 32.457 | 32.999 | 33.535 | 34.067 |
| .800          | 29.082          | 29.624 | 30.166 | 30.707 | 31.243 | 31.778 | 32.329 | 32.847 | 33.408 | 33.947 | 34.486 |
| .820          | 29.492          | 30.038 | 30.583 | 31.128 | 31.673 | 32.217 | 32.760 | 33.293 | 33.845 | 34.389 | 34.931 |
| .840          | 29.936          | 30.485 | 31.035 | 31.584 | 32.131 | 32.680 | 33.227 | 33.774 | 34.321 | 34.867 | 35.413 |
| .860          | 30.422          | 30.977 | 31.530 | 32.083 | 32.636 | 33.188 | 33.739 | 34.290 | 34.841 | 35.388 | 35.938 |
| .880          | 30.924          | 31.524 | 32.082 | 32.640 | 33.197 | 33.754 | 34.310 | 34.865 | 35.414 | 35.975 | 36.529 |
| .900          | 31.573          | 32.148 | 32.711 | 33.230 | 33.836 | 34.398 | 34.959 | 35.517 | 36.080 | 36.639 | 37.199 |
| .920          | 32.310          | 32.880 | 33.450 | 34.019 | 34.586 | 35.155 | 35.710 | 36.289 | 36.854 | 37.420 | 37.984 |
| .940          | 33.206          | 33.784 | 34.361 | 34.937 | 35.511 | 36.086 | 36.661 | 37.222 | 37.807 | 38.380 | 38.950 |
| .950          | 33.752          | 34.335 | 34.916 | 35.497 | 36.077 | 36.656 | 37.234 | 37.812 | 38.389 | 38.965 | 39.541 |
| .960          | 34.390          | 34.989 | 35.576 | 36.162 | 36.747 | 37.331 | 37.915 | 38.496 | 39.079 | 39.660 | 40.241 |
| .970          | 35.211          | 35.805 | 36.399 | 36.991 | 37.582 | 38.172 | 38.761 | 39.351 | 39.939 | 40.526 | 41.111 |
| .980          | 36.307          | 36.909 | 37.511 | 38.111 | 38.711 | 39.310 | 39.907 | 40.504 | 41.100 | 41.696 | 42.290 |
| .990          | 38.077          | 38.693 | 39.308 | 39.922 | 40.534 | 41.146 | 41.757 | 42.366 | 42.975 | 43.583 | 44.190 |
| .995          | 39.745          | 40.373 | 41.000 | 41.626 | 42.251 | 42.874 | 43.497 | 44.118 | 44.738 | 45.358 | 45.976 |
| .999          | 43.330          | 43.984 | 44.636 | 45.287 | 45.936 | 46.584 | 47.230 | 47.875 | 48.519 | 49.162 | 49.803 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 30.00           | 31.00  | 32.00  | 33.00  | 34.00  | 35.00  | 36.00  | 37.00  | 38.00  | 39.00  | 40.00  |
| .001          | 15.869          | 16.591 | 17.316 | 18.046 | 18.780 | 19.518 | 20.260 | 21.005 | 21.753 | 22.505 | 23.260 |
| .005          | 17.767          | 18.534 | 19.305 | 20.079 | 20.857 | 21.638 | 22.422 | 23.208 | 23.998 | 24.791 | 25.586 |
| .010          | 18.742          | 19.532 | 20.324 | 21.120 | 21.919 | 22.721 | 23.526 | 24.333 | 25.143 | 25.955 | 26.770 |
| .020          | 19.850          | 20.663 | 21.480 | 22.300 | 23.122 | 23.947 | 24.774 | 25.604 | 26.436 | 27.270 | 28.106 |
| .030          | 20.575          | 21.404 | 22.236 | 23.071 | 23.908 | 24.748 | 25.589 | 26.433 | 27.279 | 28.128 | 28.978 |
| .040          | 21.133          | 21.974 | 22.817 | 23.663 | 24.512 | 25.362 | 26.215 | 27.070 | 27.926 | 28.785 | 29.645 |
| .050          | 21.594          | 22.445 | 23.297 | 24.153 | 25.010 | 25.870 | 26.731 | 27.595 | 28.460 | 29.327 | 30.187 |
| .060          | 21.992          | 22.851 | 23.712 | 24.574 | 25.440 | 26.303 | 27.176 | 28.047 | 28.918 | 29.794 | 30.670 |
| .080          | 22.664          | 23.536 | 24.411 | 25.287 | 26.165 | 27.045 | 27.927 | 28.806 | 29.695 | 30.508 | 31.451 |
| .100          | 23.229          | 24.113 | 24.998 | 25.881 | 26.774 | 27.664 | 28.556 | 29.450 | 30.345 | 31.241 | 32.101 |
| .120          | 23.723          | 24.618 | 25.513 | 26.409 | 27.307 | 28.207 | 29.108 | 30.010 | 30.913 | 31.659 | 32.705 |
| .140          | 24.171          | 25.072 | 25.975 | 26.848 | 27.786 | 28.694 | 29.603 | 30.513 | 31.425 | 32.336 | 33.250 |
| .160          | 24.580          | 25.427 | 26.400 | 27.312 | 28.226 | 29.141 | 30.057 | 30.975 | 31.855 | 32.813 | 33.728 |
| .180          | 24.961          | 25.878 | 26.796 | 27.715 | 28.636 | 29.557 | 30.480 | 31.247 | 32.329 | 33.255 | 34.181 |
| .200          | 25.320          | 26.236 | 27.168 | 28.094 | 29.003 | 29.949 | 30.877 | 31.769 | 32.739 | 33.671 | 34.603 |
| .220          | 25.662          | 26.591 | 27.521 | 28.454 | 29.387 | 30.302 | 31.256 | 32.191 | 33.127 | 34.065 | 35.003 |
| .240          | 25.988          | 26.924 | 27.844 | 28.798 | 29.737 | 30.601 | 31.617 | 32.558 | 33.499 | 34.443 | 35.386 |
| .260          | 26.303          | 27.244 | 28.187 | 29.130 | 30.074 | 31.019 | 31.965 | 32.911 | 33.858 | 34.805 | 35.755 |
| .280          | 26.607          | 27.555 | 28.432 | 29.451 | 30.400 | 31.346 | 32.301 | 33.248 | 34.205 | 35.158 | 36.111 |
| .300          | 26.905          | 27.823 | 28.810 | 29.764 | 30.718 | 31.673 | 32.629 | 33.585 | 34.539 | 35.499 | 36.457 |
| .320          | 27.195          | 28.152 | 29.110 | 30.069 | 31.023 | 31.988 | 32.949 | 33.910 | 34.871 | 35.833 | 36.796 |
| .340          | 27.479          | 28.442 | 29.405 | 30.216 | 31.330 | 32.297 | 33.262 | 34.228 | 35.194 | 36.160 | 37.105 |
| .360          | 27.690          | 28.727 | 29.694 | 30.658 | 31.632 | 32.601 | 33.560 | 34.541 | 35.511 | 36.471 | 37.453 |
| .380          | 28.027          | 29.008 | 29.962 | 30.954 | 31.888 | 32.901 | 33.873 | 34.807 | 35.825 | 36.754 | 37.775 |
| .400          | 28.309          | 29.278 | 30.259 | 31.242 | 32.220 | 33.198 | 34.177 | 35.156 | 36.045 | 37.109 | 37.999 |
| .420          | 28.582          | 29.490 | 30.545 | 31.528 | 32.511 | 33.493 | 34.471 | 35.459 | 36.443 | 37.426 | 38.314 |
| .440          | 28.835          | 29.840 | 30.788 | 31.654 | 32.759 | 33.787 | 34.774 | 35.761 | 36.749 | 37.736 | 38.725 |
| .460          | 29.124          | 30.115 | 31.106 | 32.087 | 33.006 | 34.080 | 35.071 | 36.063 | 37.055 | 38.046 | 39.038 |
| .480          | 29.395          | 30.391 | 31.384 | 32.382 | 33.376 | 34.362 | 35.347 | 36.362 | 37.360 | 38.332 | 39.156 |
| .500          | 29.593          | 30.667 | 31.665 | 32.665 | 33.667 | 34.656 | 35.578 | 36.656 | 37.664 | 38.666 | 39.667 |
| .520          | 29.941          | 30.946 | 31.950 | 32.955 | 33.948 | 34.963 | 35.877 | 36.971 | 37.880 | 38.980 | 39.984 |
| .540          | 30.215          | 31.226 | 32.215 | 33.244 | 34.253 | 35.256 | 36.270 | 37.278 | 38.285 | 39.295 | 40.303 |
| .560          | 30.496          | 31.510 | 32.524 | 33.532 | 34.550 | 35.473 | 36.576 | 37.541 | 38.601 | 39.613 | 40.622 |
| .580          | 30.780          | 31.798 | 32.815 | 33.791 | 34.829 | 35.867 | 36.886 | 37.902 | 38.919 | 39.736 | 40.848 |
| .600          | 31.067          | 32.090 | 33.113 | 34.049 | 35.158 | 36.176 | 37.201 | 38.216 | 39.236 | 40.161 | 41.283 |
| .620          | 31.361          | 32.389 | 33.415 | 34.437 | 35.470 | 36.495 | 37.520 | 38.547 | 39.572 | 40.595 | 41.621 |
| .640          | 31.621          | 32.688 | 33.726 | 34.757 | 35.610 | 36.819 | 37.801 | 38.854 | 39.907 | 40.885 | 41.966 |
| .660          | 31.969          | 32.964 | 34.043 | 35.080 | 36.104 | 37.150 | 38.185 | 39.217 | 40.247 | 41.287 | 42.293 |
| .680          | 32.285          | 33.328 | 34.370 | 35.411 | 36.405 | 37.480 | 38.532 | 39.570 | 40.609 | 41.646 | 42.629 |
| .700          | 32.613          | 33.661 | 34.663 | 35.754 | 36.800 | 37.845 | 38.889 | 39.920 | 40.949 | 42.018 | 43.004 |
| .720          | 32.953          | 33.962 | 35.058 | 36.109 | 37.160 | 38.198 | 39.259 | 40.308 | 41.356 | 42.402 | 43.232 |
| .740          | 33.302          | 34.366 | 35.424 | 36.480 | 37.536 | 38.590 | 39.645 | 40.699 | 41.752 | 42.804 | 43.855 |
| .760          | 33.679          | 34.740 | 35.715 | 36.869 | 37.930 | 38.990 | 40.050 | 41.109 | 42.167 | 43.224 | 44.280 |
| .780          | 34.070          | 35.141 | 36.207 | 37.278 | 38.345 | 39.214 | 40.476 | 41.537 | 42.604 | 43.666 | 44.728 |
| .800          | 34.463          | 35.563 | 36.637 | 37.712 | 38.785 | 39.857 | 40.927 | 41.998 | 43.067 | 44.128 | 45.199 |
| .820          | 34.908          | 36.014 | 37.097 | 38.177 | 39.250 | 40.322 | 41.412 | 42.485 | 43.563 | 44.608 | 45.711 |
| .840          | 35.413          | 36.504 | 37.592 | 38.680 | 39.767 | 40.851 | 41.936 | 43.018 | 44.100 | 45.180 | 46.260 |
| .860          | 35.941          | 37.027 | 38.135 | 39.231 | 40.325 | 41.417 | 42.508 | 43.598 | 44.628 | 45.774 | 46.857 |
| .880          | 36.529          | 37.636 | 38.735 | 39.838 | 40.946 | 42.044 | 43.146 | 44.240 | 45.222 | 46.435 | 47.513 |
| .900          | 37.149          | 38.315 | 39.429 | 40.543 | 41.654 | 42.764 | 43.757 | 44.978 | 46.079 | 47.187 | 48.289 |
| .920          | 37.981          | 39.109 | 40.238 | 41.362 | 42.483 | 43.604 | 44.722 | 45.839 | 46.922 | 48.068 | 49.171 |
| .940          | 38.951          | 40.093 | 41.232 | 42.369 | 43.504 | 44.637 | 45.752 | 46.662 | 47.991 | 49.145 | 50.273 |
| .950          | 39.541          | 40.691 | 41.823 | 42.982 | 44.125 | 45.266 | 46.402 | 47.541 | 48.673 | 49.808 | 50.940 |
| .960          | 40.241          | 41.400 | 42.555 | 43.711 | 44.861 | 46.012 | 47.159 | 48.288 | 49.448 | 50.590 | 51.729 |
| .970          | 41.113          | 42.283 | 43.452 | 44.617 | 45.780 | 46.941 | 48.099 | 49.255 | 50.157 | 51.561 | 52.711 |
| .980          | 42.290          | 43.476 | 44.660 | 45.824 | 47.019 | 48.194 | 49.367 | 50.537 | 51.705 | 52.871 | 54.035 |
| .990          | 44.190          | 45.401 | 46.608 | 47.813 | 49.014 | 50.213 | 51.408 | 52.601 | 53.791 | 54.979 | 56.164 |
| .995          | 45.976          | 47.209 | 48.439 | 49.665 | 50.888 | 52.107 | 53.324 | 54.537 | 55.748 | 56.955 | 58.161 |
| .999          | 49.803          | 51.083 | 52.358 | 53.629 | 54.896 | 56.158 | 57.417 | 58.673 | 59.925 | 61.174 | 62.420 |

**Percentage Points of the Gamma Distribution with Unit Scale Parameter**

| Cum.<br>Prob. | Shape Parameter |        |        |        |        |        |        |        |        |        |        |
|---------------|-----------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
|               | 40.00           | 41.00  | 42.00  | 43.00  | 44.00  | 45.00  | 46.00  | 47.00  | 48.00  | 49.00  | 50.00  |
| .001          | 23.260          | 24.018 | 24.779 | 25.542 | 26.309 | 27.078 | 27.849 | 28.623 | 29.400 | 30.178 | 30.959 |
| .005          | 25.586          | 26.384 | 27.184 | 27.986 | 28.791 | 29.598 | 30.407 | 31.218 | 32.032 | 32.847 | 33.664 |
| .010          | 26.770          | 27.587 | 28.407 | 29.228 | 30.052 | 30.877 | 31.705 | 32.534 | 33.365 | 34.198 | 35.032 |
| .020          | 28.106          | 28.945 | 29.785 | 30.627 | 31.471 | 32.317 | 33.165 | 34.014 | 34.865 | 35.717 | 36.571 |
| .030          | 28.978          | 29.830 | 30.683 | 31.539 | 32.396 | 33.255 | 34.115 | 34.977 | 35.840 | 36.705 | 37.571 |
| .040          | 29.645          | 30.507 | 31.371 | 32.227 | 33.103 | 33.972 | 34.842 | 35.713 | 36.586 | 37.460 | 38.144 |
| .050          | 30.187          | 31.066 | 31.938 | 32.812 | 33.687 | 34.561 | 35.441 | 36.278 | 37.200 | 38.082 | 38.965 |
| .060          | 30.670          | 31.547 | 32.426 | 33.307 | 34.188 | 35.072 | 35.956 | 36.842 | 37.726 | 38.617 | 39.495 |
| .080          | 31.451          | 32.358 | 33.083 | 34.141 | 35.033 | 35.928 | 36.824 | 37.720 | 38.618 | 39.511 | 40.417 |
| .100          | 32.101          | 33.037 | 33.856 | 34.839 | 35.741 | 36.643 | 37.550 | 38.456 | 39.363 | 40.174 | 41.179 |
| .120          | 32.705          | 33.612 | 34.538 | 35.440 | 36.358 | 37.272 | 38.185 | 39.098 | 39.813 | 40.925 | 41.844 |
| .140          | 33.250          | 34.166 | 35.061 | 35.993 | 36.916 | 37.835 | 38.755 | 39.675 | 40.596 | 41.418 | 42.442 |
| .160          | 33.728          | 34.655 | 35.577 | 36.457 | 37.425 | 38.350 | 39.276 | 40.203 | 41.131 | 42.059 | 42.988 |
| .180          | 34.181          | 35.089 | 36.037 | 36.957 | 37.897 | 38.829 | 39.761 | 40.694 | 41.627 | 42.548 | 43.496 |
| .200          | 34.603          | 35.537 | 36.382 | 37.407 | 38.343 | 39.279 | 40.217 | 41.154 | 42.093 | 43.032 | 43.973 |
| .220          | 35.003          | 35.937 | 36.883 | 37.823 | 38.764 | 39.609 | 40.649 | 41.591 | 42.536 | 43.478 | 44.425 |
| .240          | 35.386          | 36.331 | 37.276 | 38.221 | 39.120 | 40.114 | 41.060 | 42.010 | 42.958 | 43.907 | 44.857 |
| .260          | 35.755          | 36.698 | 37.652 | 38.604 | 39.555 | 40.505 | 41.446 | 42.412 | 43.365 | 44.305 | 45.273 |
| .280          | 36.111          | 37.043 | 38.020 | 38.975 | 39.930 | 40.786 | 41.843 | 42.800 | 43.754 | 44.716 | 45.674 |
| .300          | 36.457          | 37.416 | 38.375 | 39.329 | 40.283 | 41.256 | 42.213 | 43.178 | 44.140 | 45.102 | 46.064 |
| .320          | 36.796          | 37.736 | 38.723 | 39.674 | 40.651 | 41.616 | 42.581 | 43.533 | 44.512 | 45.479 | 46.438 |
| .340          | 37.105          | 38.095 | 39.015 | 40.034 | 40.993 | 41.969 | 42.938 | 43.901 | 44.822 | 45.848 | 46.818 |
| .360          | 37.453          | 38.233 | 39.397 | 40.368 | 41.342 | 42.309 | 43.072 | 44.262 | 45.236 | 46.210 | 47.185 |
| .380          | 37.775          | 38.745 | 39.727 | 40.654 | 41.681 | 42.656 | 43.608 | 44.612 | 45.588 | 46.568 | 47.543 |
| .400          | 37.999          | 39.074 | 40.051 | 41.035 | 41.805 | 42.889 | 43.923 | 44.952 | 45.939 | 46.918 | 47.874 |
| .420          | 38.314          | 39.394 | 40.372 | 41.363 | 42.347 | 43.332 | 44.316 | 45.302 | 46.287 | 47.273 | 48.259 |
| .440          | 38.725          | 39.712 | 40.698 | 41.689 | 42.664 | 43.660 | 44.654 | 45.643 | 46.633 | 47.621 | 48.611 |
| .460          | 39.038          | 40.030 | 40.817 | 42.015 | 43.007 | 43.996 | 44.992 | 45.978 | 46.977 | 47.970 | 48.955 |
| .480          | 39.156          | 40.348 | 41.344 | 42.341 | 43.333 | 44.333 | 45.329 | 46.325 | 47.322 | 48.318 | 49.253 |
| .500          | 39.667          | 40.667 | 41.615 | 42.660 | 43.667 | 44.667 | 45.667 | 46.667 | 47.548 | 48.667 | 49.667 |
| .520          | 39.984          | 40.988 | 41.886 | 42.995 | 43.999 | 45.003 | 45.999 | 47.010 | 48.014 | 49.017 | 50.017 |
| .540          | 40.303          | 41.207 | 42.317 | 43.271 | 44.334 | 45.341 | 46.349 | 47.352 | 48.363 | 49.371 | 50.370 |
| .560          | 40.622          | 41.610 | 42.649 | 43.660 | 44.615 | 45.683 | 46.694 | 47.645 | 48.701 | 49.727 | 50.738 |
| .580          | 40.848          | 41.954 | 42.768 | 43.999 | 45.013 | 45.971 | 46.809 | 48.044 | 49.070 | 50.086 | 51.103 |
| .600          | 41.283          | 42.249 | 43.323 | 44.342 | 45.362 | 46.381 | 47.399 | 48.403 | 49.312 | 50.455 | 51.473 |
| .620          | 41.621          | 42.645 | 43.665 | 44.664 | 45.701 | 46.738 | 47.761 | 48.784 | 49.798 | 50.763 | 51.784 |
| .640          | 41.966          | 42.995 | 44.019 | 45.050 | 46.077 | 47.104 | 48.131 | 49.157 | 50.184 | 50.953 | 52.227 |
| .660          | 42.293          | 43.352 | 44.385 | 45.387 | 46.444 | 47.479 | 48.267 | 49.540 | 50.538 | 51.600 | 52.627 |
| .680          | 42.629          | 43.714 | 44.757 | 45.677 | 46.828 | 47.856 | 48.891 | 49.929 | 50.968 | 52.001 | 53.034 |
| .700          | 43.004          | 43.989 | 45.142 | 46.183 | 47.222 | 48.262 | 49.301 | 50.339 | 51.378 | 52.282 | 53.453 |
| .720          | 43.232          | 44.495 | 45.313 | 46.586 | 47.622 | 48.674 | 49.717 | 50.760 | 51.803 | 52.710 | 53.886 |
| .740          | 43.855          | 44.905 | 45.956 | 47.006 | 48.055 | 49.103 | 50.151 | 51.198 | 52.243 | 53.155 | 54.333 |
| .760          | 44.280          | 45.336 | 46.391 | 47.438 | 48.495 | 49.552 | 50.605 | 51.657 | 52.708 | 53.759 | 54.809 |
| .780          | 44.728          | 45.789 | 46.849 | 47.908 | 48.722 | 49.775 | 51.066 | 52.140 | 53.196 | 54.251 | 55.307 |
| .800          | 45.199          | 46.269 | 47.304 | 48.275 | 49.455 | 50.526 | 51.589 | 52.651 | 53.712 | 54.701 | 55.833 |
| .820          | 45.711          | 46.722 | 47.854 | 48.908 | 49.994 | 51.061 | 52.131 | 53.199 | 54.261 | 55.329 | 56.395 |
| .840          | 46.260          | 47.338 | 48.352 | 49.492 | 50.568 | 51.641 | 52.716 | 53.781 | 54.862 | 55.934 | 57.005 |
| .860          | 46.857          | 47.946 | 49.026 | 50.111 | 51.195 | 52.207 | 53.357 | 54.434 | 55.515 | 56.593 | 57.670 |
| .880          | 47.513          | 48.620 | 49.647 | 50.804 | 51.893 | 52.982 | 54.064 | 55.154 | 56.241 | 57.323 | 58.404 |
| .900          | 48.289          | 49.390 | 50.490 | 51.589 | 52.668 | 53.783 | 54.878 | 55.972 | 57.065 | 58.158 | 59.249 |
| .920          | 49.171          | 50.039 | 51.400 | 52.508 | 53.614 | 54.721 | 55.825 | 56.929 | 58.030 | 58.836 | 60.231 |
| .940          | 50.273          | 51.392 | 52.517 | 53.637 | 54.755 | 55.872 | 56.988 | 58.102 | 59.215 | 60.327 | 61.438 |
| .950          | 50.940          | 52.069 | 53.195 | 54.324 | 55.449 | 56.495 | 57.695 | 58.816 | 59.935 | 61.054 | 62.171 |
| .960          | 51.729          | 52.866 | 54.004 | 55.138 | 56.271 | 57.403 | 58.533 | 59.662 | 60.789 | 61.904 | 63.040 |
| .970          | 52.711          | 53.859 | 54.996 | 56.150 | 57.293 | 58.434 | 59.276 | 60.712 | 61.849 | 62.984 | 64.118 |
| .980          | 54.035          | 55.196 | 56.356 | 57.514 | 58.670 | 59.824 | 60.813 | 62.128 | 63.277 | 64.425 | 65.571 |
| .990          | 56.164          | 57.347 | 58.528 | 59.707 | 60.884 | 62.058 | 63.231 | 64.402 | 65.571 | 66.738 | 67.903 |
| .995          | 58.161          | 59.363 | 60.563 | 61.761 | 62.956 | 64.149 | 65.341 | 66.530 | 67.717 | 68.902 | 70.085 |
| .999          | 62.420          | 63.662 | 64.902 | 66.139 | 67.373 | 68.604 | 69.833 | 71.059 | 72.284 | 73.505 | 74.725 |

## NOTES



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